

Robust estimates of theoretical uncertainties at fixed-order in perturbation theory

Rene Poncelet



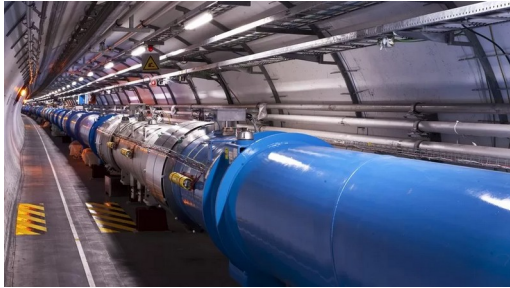
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Outline

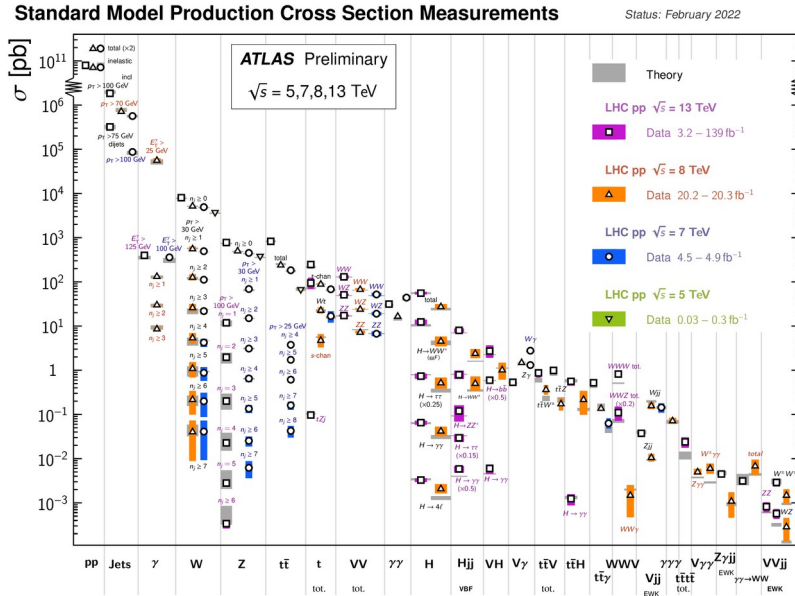
- Precision predictions at the LHC
- Missing Higher Order Uncertainties (MHOUs)
How to estimate the uncertainty of (truncated) perturbative expansions?
 - Scale variations for fixed-order and resummed cross sections
 - Bayesian methods
 - Theory Nuisance Parameters (TNPs)
- Application of TNPs to fixed-order perturbation theory
- Discussion/Summary/Outlook

Standard Model phenomenology at the LHC

Scattering experiments



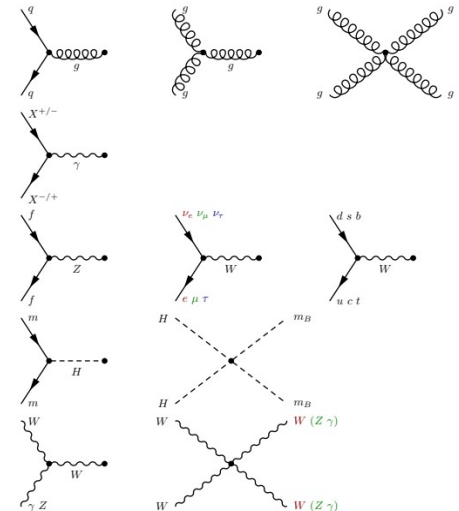
Credit: CERN



Credit: ATLAS



Theory/Model

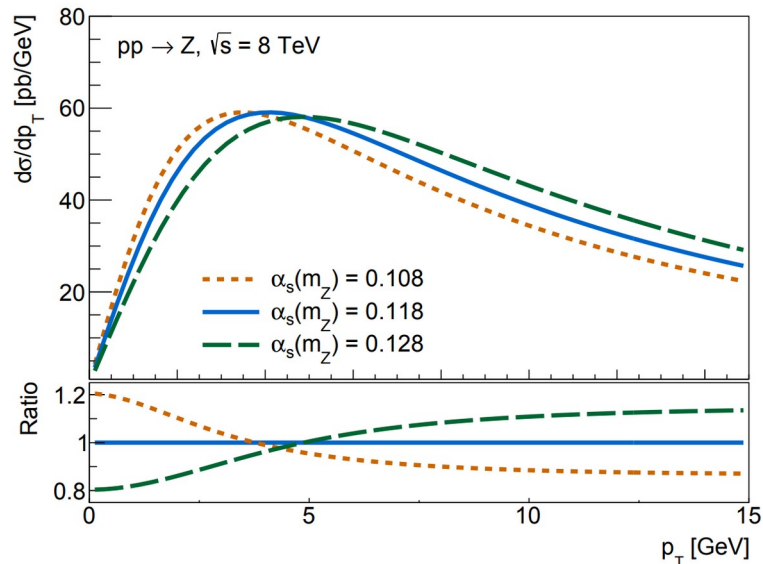


Credit: Jack Lindon, CERN

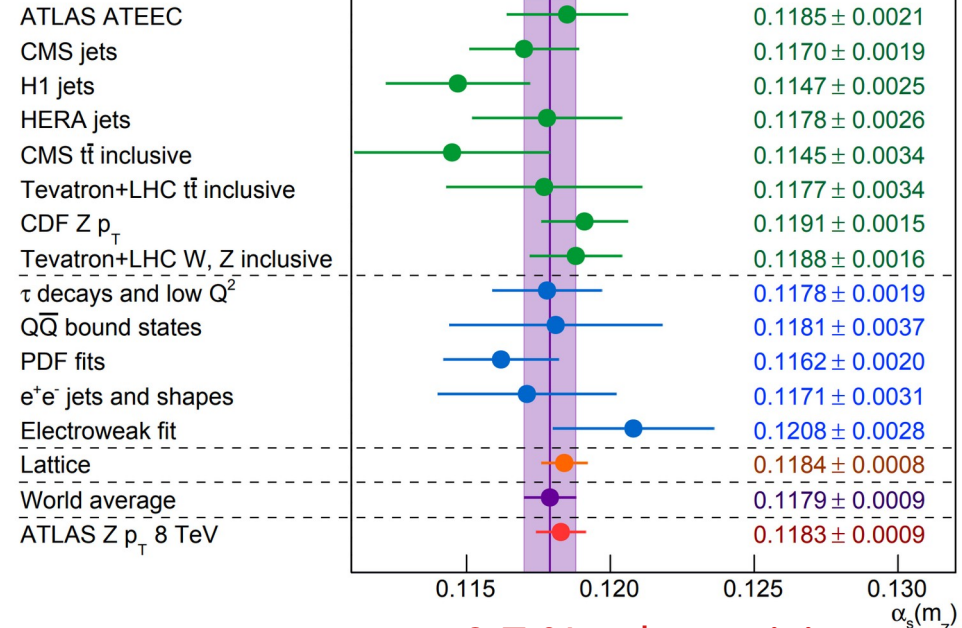
Precision example: strong coupling from pT(Z)

[ATLAS 2309.12986]

Sensitivity of Z-boson's recoil to the strong coupling constant:



→ at low pT resummation regime!
→ theory uncertainty?

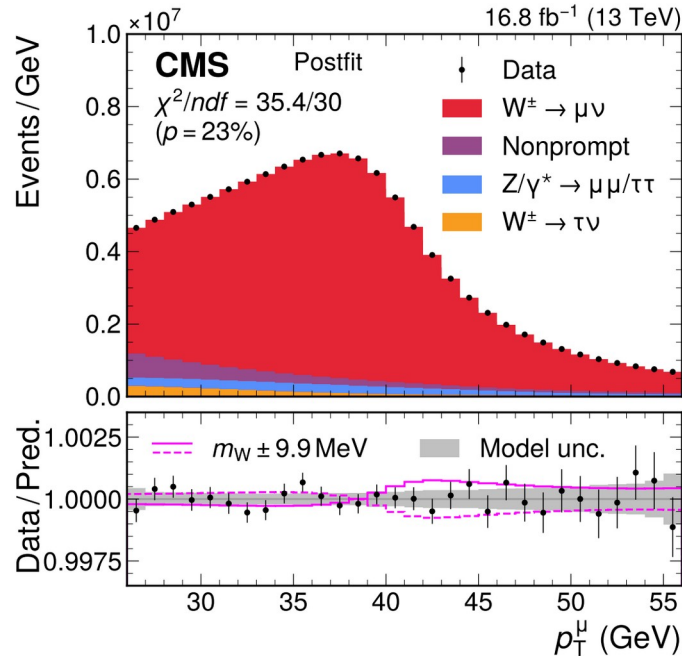


~0.7 % rel. precision

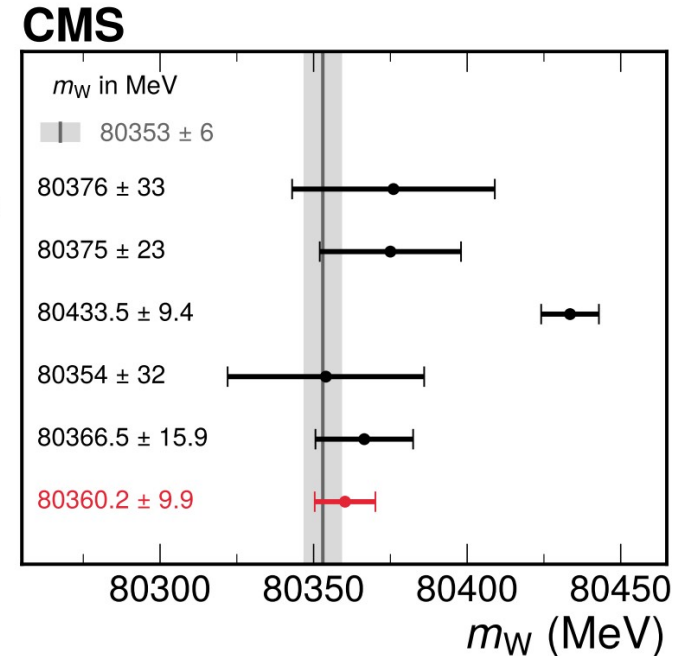
Precision example: W-mass measurement by CMS

[CMS 2412.13872]

Mass dependence of $p_T(l)$:



Electroweak fit
 PRD 110 (2024) 030001
LEP combination
 Phys. Rep. 532 (2013) 119
D0
 PRL 108 (2012) 151804
CDF
 Science 376 (2022) 6589
LHCb
 JHEP 01 (2022) 036
ATLAS
 arXiv:2403.15085
CMS
 This work

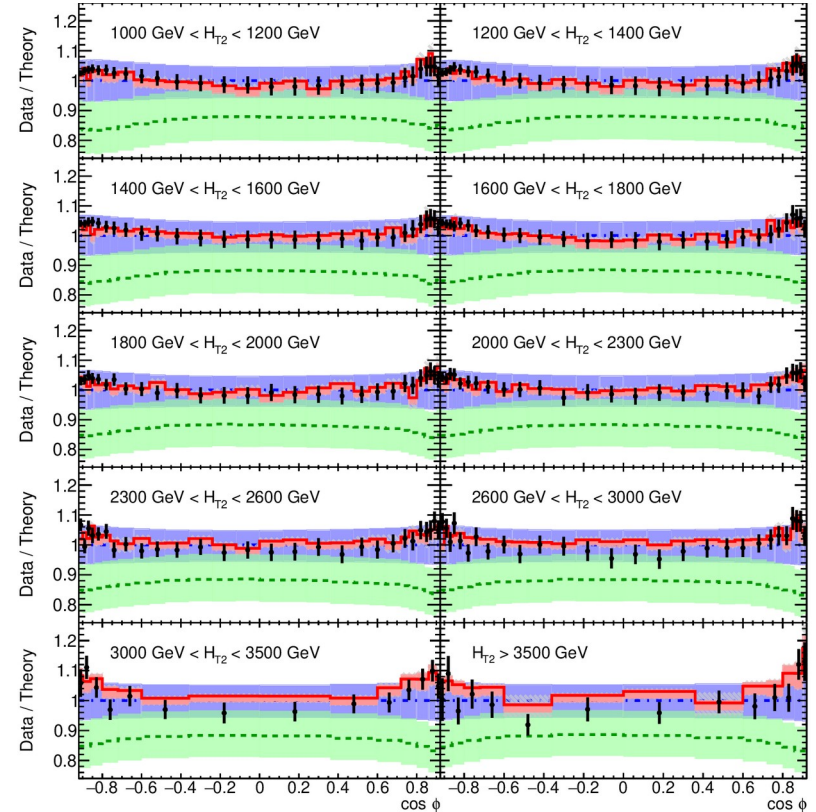
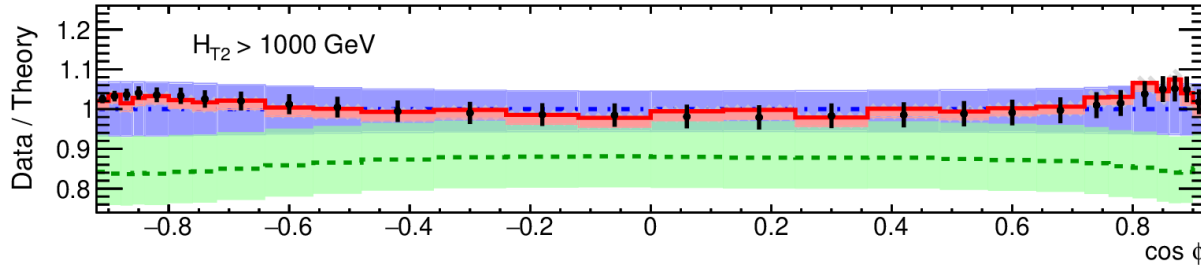


Jacobian peak position $\sim m(W)/2 \rightarrow$ resummation sensitive \rightarrow theory uncertainty?

Precision example: strong-coupling from TEEC

Next-to-Next-to-Leading Order Study of Three-Jet Production at the LHC
 Czakon, Mitov, Poncelet *Phys.Rev.Lett.* 127 (2021) 15, 152001

[ATLAS 2301.09351]



ATLAS

Particle-level TEEC

$\sqrt{s} = 13 \text{ TeV}; 139 \text{ fb}^{-1}$

anti- k_t $R = 0.4$

$p_T > 60 \text{ GeV}$

$|\eta| < 2.4$

$\mu_{R,F} = P_T$

$\alpha_s(m_Z) = 0.1180$

NNPDF 3.0 (NNLO)

— Data

--- LO

--- NLO

--- NNLO

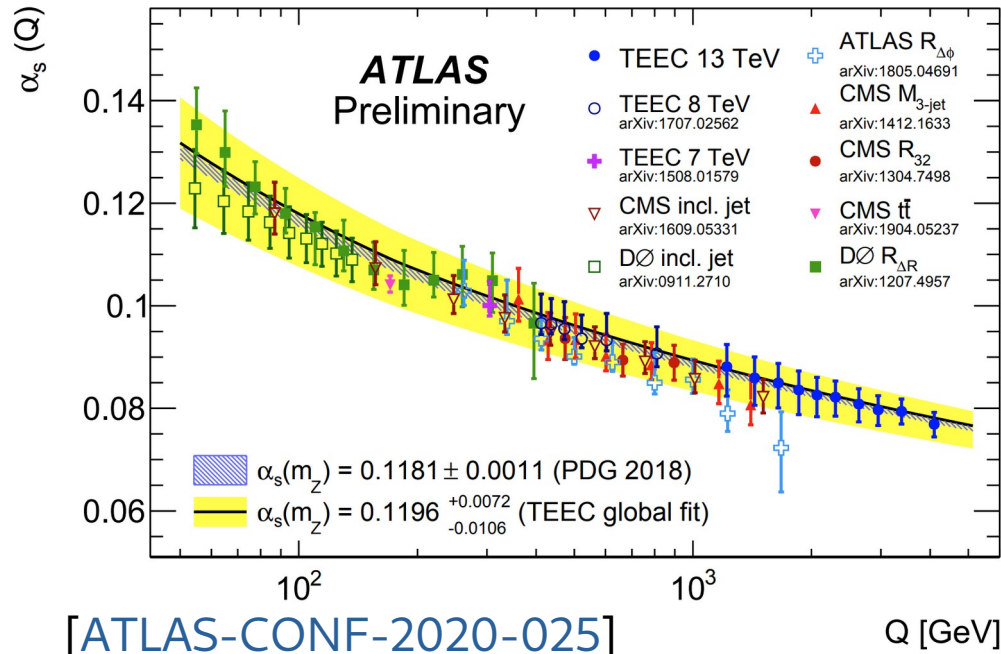
Multi-jet angular correlations

Uncertainties driven by
 fixed-order precision through ratio:

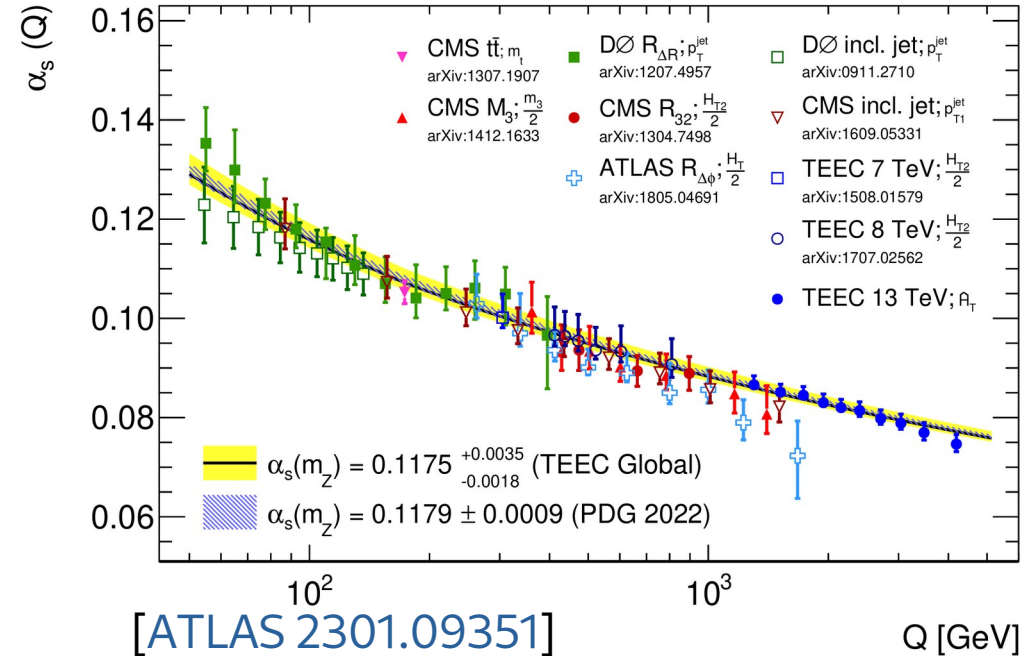
$$R^i(\mu_R, \mu_F, \text{PDF}, \alpha_{S,0}) = \frac{d\sigma_3^i(\mu_R, \mu_F, \text{PDF}, \alpha_{S,0})}{d\sigma_2^i(\mu_R, \mu_F, \text{PDF}, \alpha_{S,0})}$$

Precision example: strong-coupling from TEEC

NLO QCD

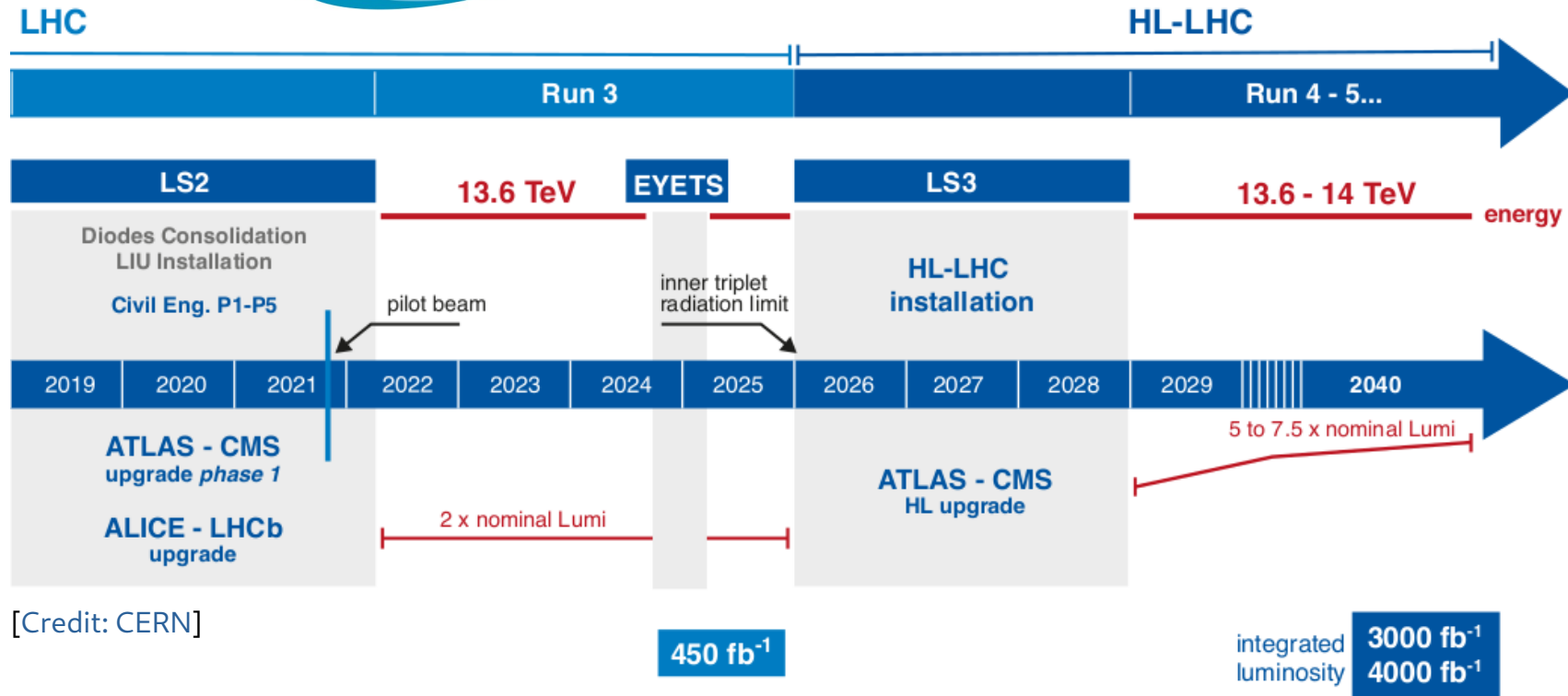


NNLO QCD



Theory uncertainty dominant effect!

LHC Precision era and future experiments



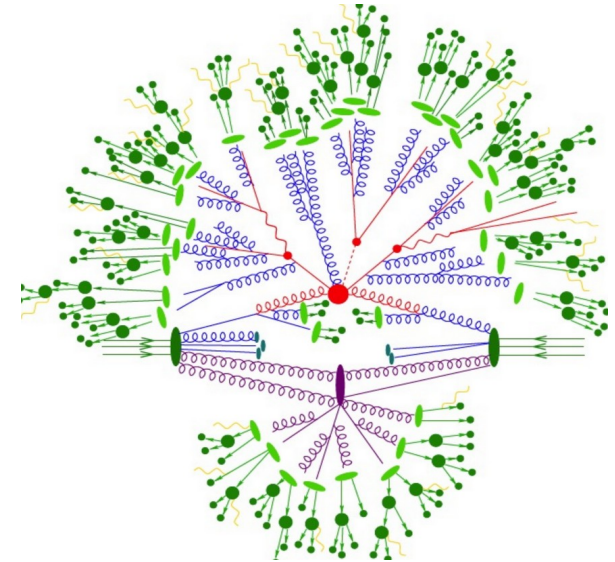
[Credit: CERN]

Uncertainties in precision phenomenology

Experiments are getting more precise → theory uncertainties matter!

Sources of theory uncertainties:

- parametric (values of coupling parameters etc.)
→ variation of parameters within their uncertainties
- parton distribution functions (PDFs)
→ different error propagation methods (fit parameter, replicas,...)
- non-perturbative parameters in Monte Carlo simulations.
→ needs data constraints by definition. Problematic if dominant effect...
- **missing higher orders in fixed-order and resummed predictions (MHOU)**
→ tricky because we are trying to estimate the unknown....



[Credit: SHERPA]

Theory uncertainties from scale variations

Lets focus on QCD as an example:

$$d\sigma = d\sigma^{(0)} + \alpha_s d\sigma^{(1)} + \alpha_s^2 d\sigma^{(2)} + \dots \xrightarrow{\text{RGE}} \mu \frac{d\sigma^{(n)}}{d\mu} = \mathcal{O}\left(\alpha_s^{(n_0+n+1)}\right)$$

Of same order as the next dominant term \rightarrow exploiting this to estimate size of $d\sigma^{(n+1)}$

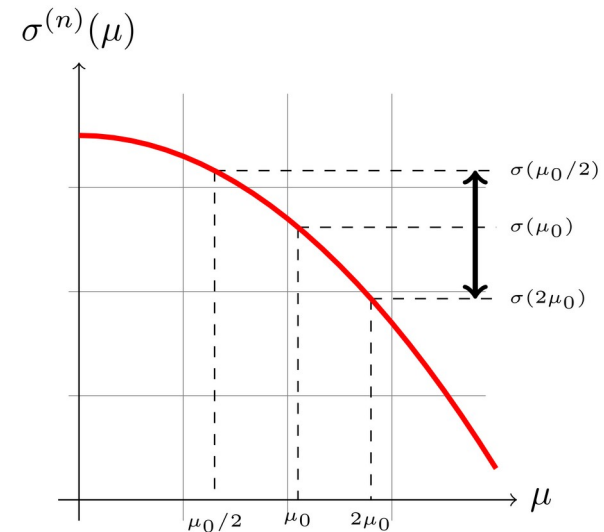
Scale variation prescription

- choose 'sensible' μ_0

$\sigma^{(n)}(\mu_{\text{FAC}}) = 0 \rightarrow$ principle of fastest apparent convergence

$\left. \mu \frac{d\sigma(\mu)}{d\mu} \right|_{\mu=\mu_{\text{PMC}}} = 0 \rightarrow$ principle of minimal sensitivity
 $\rightarrow \dots$

- vary with a factor (typically 2)
- take envelope as uncertainty
- ad-hoc and heuristic choice



Missing higher orders

Notation from:

Beyond Scale Variations: Perturbative Theory Uncertainties from Nuisance Parameters,
Frank Tackmann [2411.18606]

Generic perturbative expansion:

$$f(\alpha) = f_0 + f_1\alpha + f_2\alpha^2 + f_3\alpha^3 + \dots$$

For QCD: $\alpha = \alpha_s(\mu_0)$

f_i : the coefficient of the series, potentially unknown

We can compute the truncated series:

$$f^{\text{LO}}(\alpha) = \hat{f}_0 \quad f^{\text{NLO}}(\alpha) = \hat{f}_0 + \hat{f}_1\alpha \quad f^{\text{NNLO}}(\alpha) = \hat{f}_0 + \hat{f}_1\alpha + \hat{f}_2\alpha^2$$

\hat{f}_i : the true value, i.e. a value we actually computed

The missing terms are the source of uncertainty.

(assume convergence \rightarrow the first missing is the dominant one)

$$f^{\text{LO}+1}(\alpha) = \hat{f}_0 + f_1\alpha \quad f^{\text{NLO}+1}(\alpha) = \hat{f}_0 + \hat{f}_1\alpha + f_2\alpha^2 \quad f^{\text{NNLO}+1}(\alpha) = \hat{f}_0 + \hat{f}_1\alpha + \hat{f}_2\alpha^2 + f_3\alpha^3$$

Scale variation approach

Change of scale = change of renormalisation scheme: $\tilde{\alpha}(\alpha) = \alpha(1 + b_0\alpha + b_1\alpha^2 + b_2\alpha^3 + \dots)$

For QCD: $\alpha = \alpha_s(\mu_0)$ $\tilde{\alpha} = \alpha_s(\mu)$

$$b_0 = \frac{\beta_0}{2\pi} L \quad b_1 = \frac{\beta_0^2}{4\pi^2} L^2 + \frac{\beta_1}{8\pi^2} L \quad b_2 = \frac{\beta_0^3}{8\pi^3} L^3 + \frac{5\beta_0\beta_1}{32\pi^2} L^2 + \frac{\beta_2}{32\pi^3} L \quad L = \ln \frac{\mu_0}{\mu}$$

$$\tilde{f}^{\text{LO}}(\tilde{\alpha}) = \hat{f}_0$$

$$\tilde{f}^{\text{NLO}}(\tilde{\alpha}) = \hat{f}_0 + \hat{f}_1\tilde{\alpha} = \hat{f}_0 + \alpha\hat{f}_1 + \alpha^2 b_0 \hat{f}_1 + \mathcal{O}(\alpha^3)$$

$$\tilde{f}^{\text{NNLO}}(\tilde{\alpha}) = \hat{f}_0 + \hat{f}_1\tilde{\alpha} + \hat{f}_2\tilde{\alpha}^2 = \hat{f}_0 + \alpha\hat{f}_1 + \alpha^2\hat{f}_2 + \alpha^3(2b_0(\hat{f}_2 - b_0\hat{f}_1) + b_1\hat{f}_1) + \mathcal{O}(\alpha^4)$$

Scale variation approach

Change of scale = change of renormalisation scheme: $\tilde{\alpha}(\alpha) = \alpha(1 + b_0\alpha + b_1\alpha^2 + b_2\alpha^3 + \dots)$

For QCD: $\alpha = \alpha_s(\mu_0)$ $\tilde{\alpha} = \alpha_s(\mu)$

$$b_0 = \frac{\beta_0}{2\pi} L \quad b_1 = \frac{\beta_0^2}{4\pi^2} L^2 + \frac{\beta_1}{8\pi^2} L \quad b_2 = \frac{\beta_0^3}{8\pi^3} L^3 + \frac{5\beta_0\beta_1}{32\pi^2} L^2 + \frac{\beta_2}{32\pi^3} L \quad L = \ln \frac{\mu_0}{\mu}$$

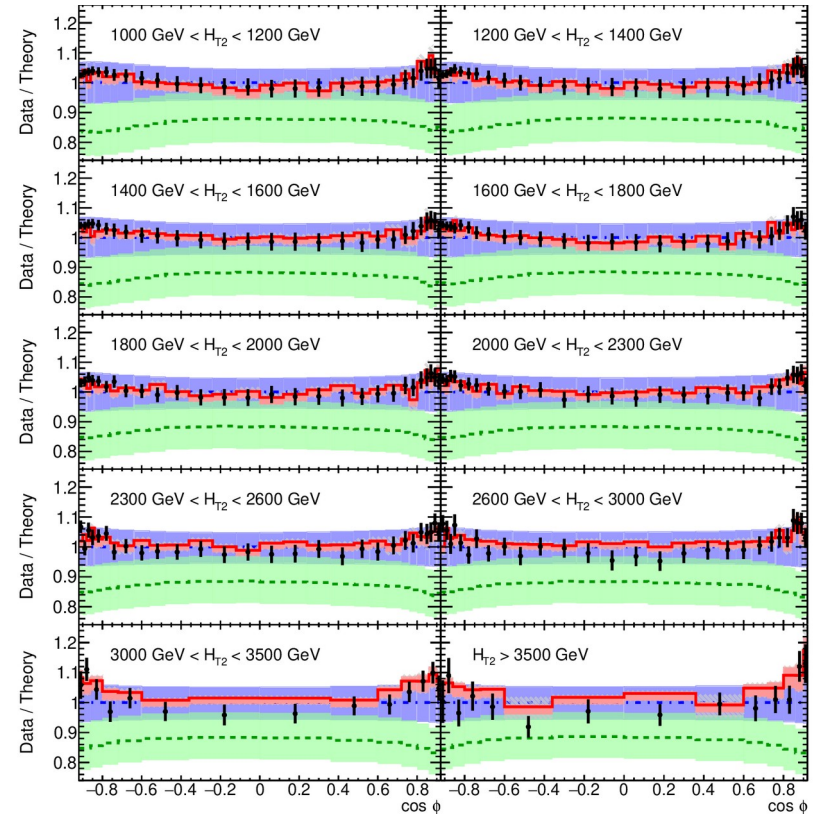
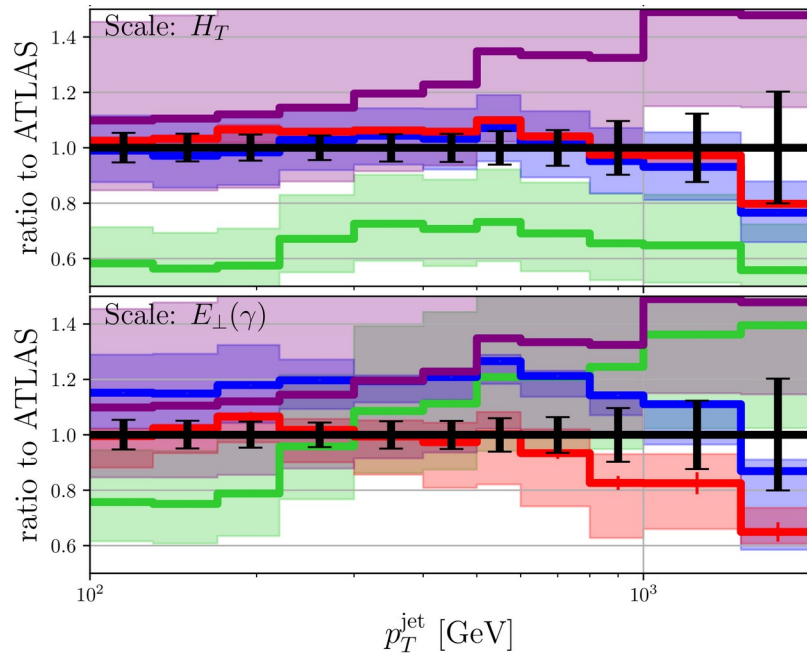
$$\Delta f^{\text{NLO}} = f^{\text{NLO}} - \tilde{f}^{\text{NLO}}(\tilde{\alpha}) = -\alpha^2 b_0 \hat{f}_1 + \mathcal{O}(\alpha^3)$$

$$\Delta f^{\text{NNLO}} = f^{\text{NNLO}} - \tilde{f}^{\text{NNLO}}(\tilde{\alpha}) = \alpha^3 (2b_0(\hat{f}_2 - b_0\hat{f}_1) + b_1\hat{f}_1) + \mathcal{O}(\alpha^4)$$

Issues:

- 1) There is no reason to believe that there is a value L (i.e. scale choice) that describes all \hat{f}_i
- 2) If f is not a scalar, correlations are unclear

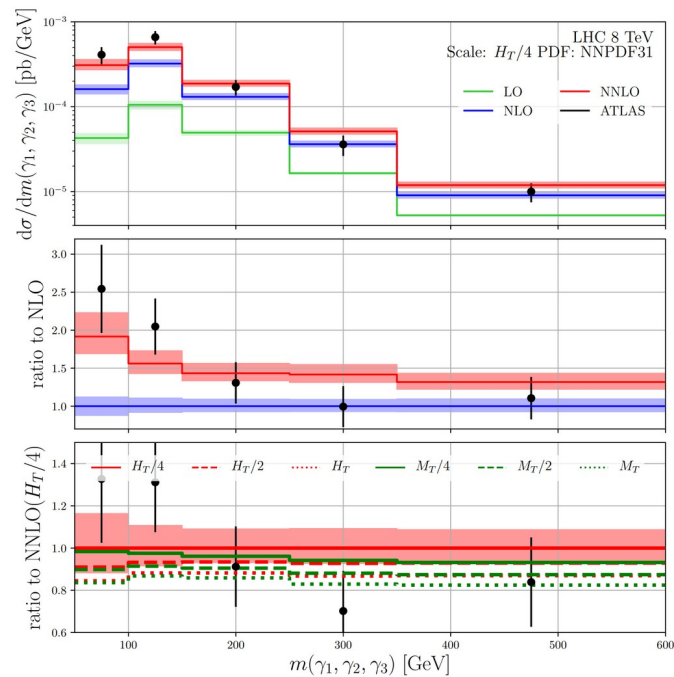
Still, scale variation works ...



Badger, Czakon, Hartanto, Moodie, Peraro, **Poncelet**, Zoia
[2304.06682]

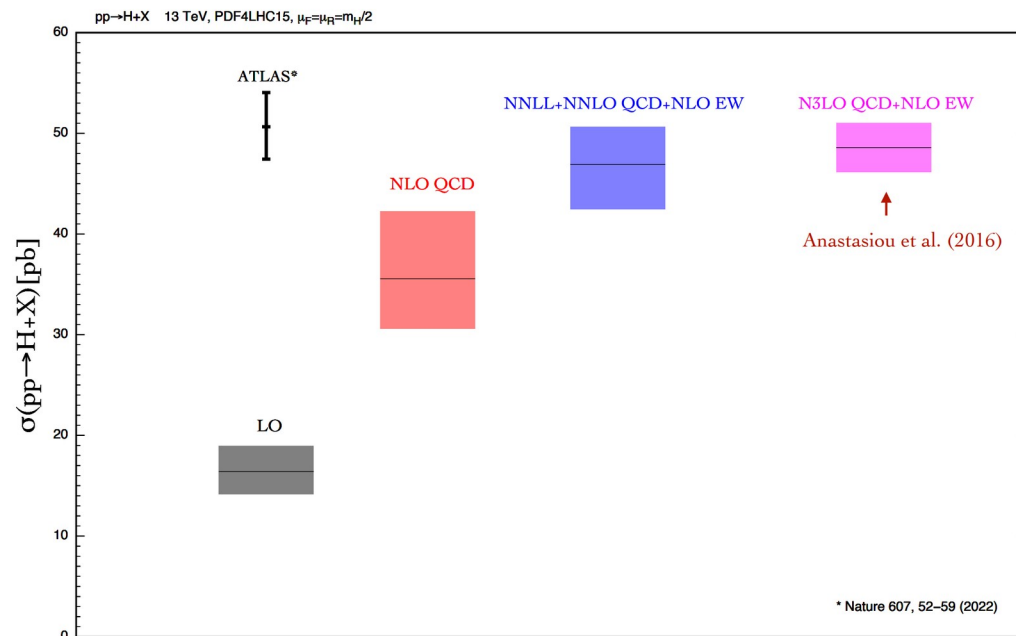
...sometimes :/

Three photon production



NNLO QCD corrections to three-photon production at the LHC, Chawdhry, Czakon, Mitov, Poncelet [JHEP 02 (2020) 057]

Higgs production



[talk by Grazzini]

Shortcomings of scale variations

- not always reliable
- ...but in most cases issues are understood/expected:
new channels, phase space constraints, etc.
→ workarounds
- however, some issues are more fundamental:
 - how to choose the central scale? → not a physical parameter, no 'true' value
(Principle of fastest apparent convergence, principle of minimal sensitivity,...)
 - how to propagate the estimated uncertainty, no statistical interpretation!
 - what about correlations? Based on 'fixed form' of the lower orders and RGE.

(At the moment) two alternative approaches under investigation:
"Bayesian" and "Theory Nuisance Parameter"

Bayesian approach I

→ Instead of ad-hoc fixed variation try to give some probabilistic interpretation

$$d\sigma = d\sigma^{(0)}(1 + \delta^{(1)} + \delta^{(2)} + \dots)$$

Probability to find coefficient $\delta^{(n+1)}$ given $\delta^{(n)}$: [\[Cacciari,Houdeau 1105.5152\]](#)

$$P(\delta^{(n+1)}|\delta^{(n)}) = \frac{P(\delta^{(n+1)})}{P(\delta^{(n)})} = \frac{\int da P(\delta^{(n+1)}|a)P_0(a)}{\int da P(\delta^{(n)}|a)P_0(a)}$$

Need to provide model and prior

Bayes: $P(A|B) = P(B|A)P(A)/P(B)$ with: $P(\delta^{(n)}|\delta^{(n+1)}) = 1$

CH model: $\delta_k = c_k \alpha_s^k$ c_k come from geometric series: $|c_k| \leq \bar{c} \quad \forall k$

Geometric model: $|\delta_k| \leq ca^k \quad \forall k$ [\[Bonvini 2006.16293\]](#)

abc model: $b - c \leq \frac{\delta_k}{a^k} \leq b + c \quad \forall k$ [\[Duhr, Huss, Mazeliauskas, Szafron 2106.04585\]](#)

Bayesian approach II

Inclusion of scale dependence: $P(\delta_{n+1}|\delta_n) = \int d\mu P(\delta_{n+1}|\delta_n; \mu)P(\mu|\delta_n)$

Scale marginalisation (the scale becomes a model parameter)

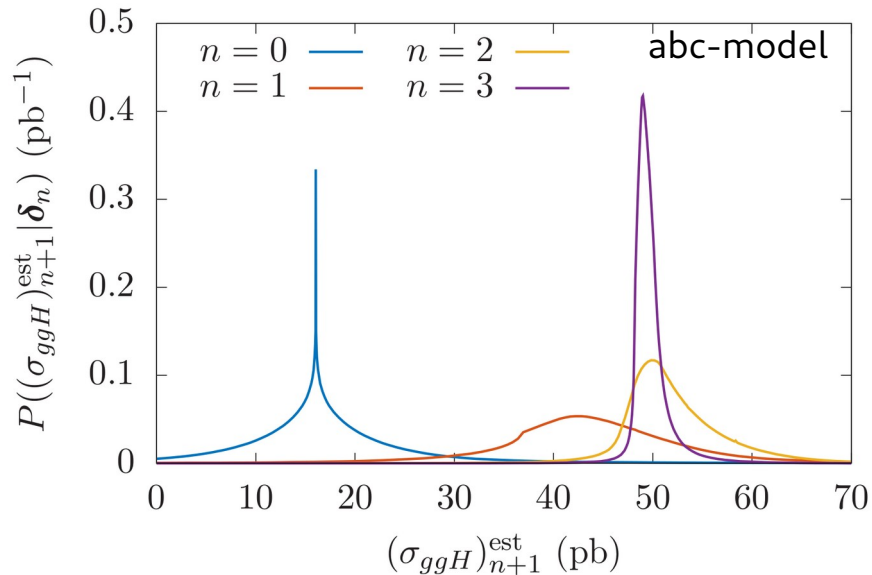
$$\mathcal{P}_{\text{sm}}(\Sigma|\Sigma_n) \approx \frac{\int d\mu P(\Sigma - \Sigma_n(\mu)|\Sigma_n(\mu)) P(\Sigma_n(\mu)) P_0(\mu)}{\int d\mu' P(\Sigma_n(\mu')) P_0(\mu')}. \quad \mu_{\text{FAC}}$$

Scale average (the results are averaged with weight function)

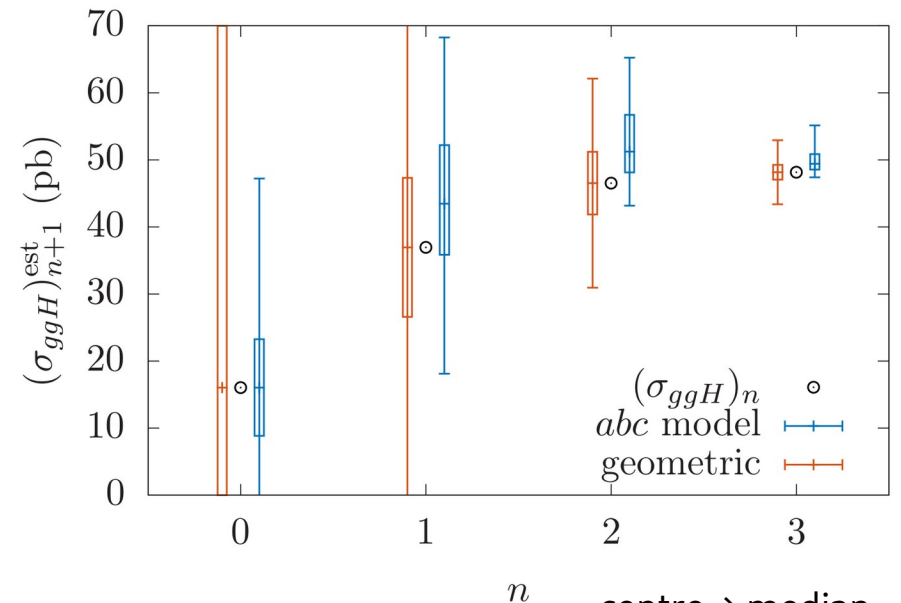
$$\mathcal{P}_{\text{sa}}(\Sigma|\Sigma_n) \approx \int d\mu w(\mu) P(\Sigma - \Sigma_n(\mu)|\Sigma_n(\mu)) \quad \mu_{\text{PMS}}$$

Bayesian approach III

Example: Higgs production in gluon - fusion



Comparison of different unc. estimates:



centre \rightarrow median
 error box \rightarrow 68% CI
 error bar \rightarrow 95% CI

Introducing theory nuisance parameters (TNPs)

Generic perturbative expansion:

$$f(\alpha) = f_0 + f_1\alpha + f_2\alpha^2 + f_3\alpha^3 + \dots$$

Beyond Scale Variations: Perturbative Theory Uncertainties from Nuisance Parameters, Frank Tackmann [2411.18606]

$$f^{\text{LO}+1}(\alpha) = \hat{f}_0 + f_1(\theta)\alpha$$

$$f^{\text{NLO}+1}(\alpha) = \hat{f}_0 + \hat{f}_1\alpha + f_2(\theta)\alpha^2$$

$$f^{\text{NNLO}+1}(\alpha) = \hat{f}_0 + \hat{f}_1\alpha + \hat{f}_2\alpha^2 + f_3(\theta)\alpha^3$$

Introduce a parametrisation of unknown coefficients in terms of

"Theory nuisance parameters" θ

- The parametrization such that there is a true value: $f_i(\hat{\theta}) = \hat{f}_i$
- Distributions of θ "known" (for example from already existing computations)
- Expert knowledge to construct such a parametrisation

Example: TNPs in resummed cross sections

Transverse momentum resummation:

$$\frac{d\sigma}{dp_T} = \underbrace{[H \times B_a \times B_b \times S]}_{\text{hard, beam, and soft functions}}(\alpha_s, \ln\left(\frac{p_T}{Q}\right)) + \mathcal{O}\left(\frac{p_T}{Q}\right)$$

$$X(\alpha_s, L) = X(\alpha_s) \exp \int_0^L dL' \{ \Gamma(\alpha_s(L')) L' + \gamma_X(\alpha_s(L')) \}$$

Perturbative expansion of resummation ingredients:

$$X(\alpha_s) = X_0 + \alpha_s X_1 + \alpha_s^2 X_2 + \dots$$

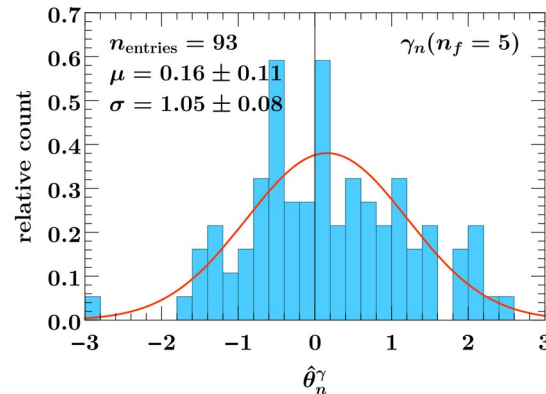
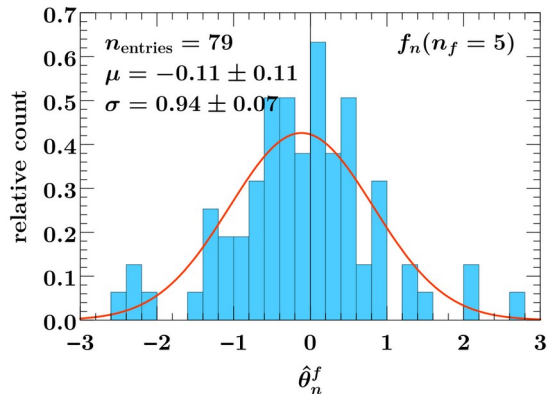
$$\Gamma(\alpha_s) = \alpha_s [\Gamma_0 + \alpha_s \Gamma_1 + \alpha_s^2 \Gamma_2 + \dots]$$

$$\gamma(\alpha_s) = \alpha_s [\gamma_0 + \alpha_s \gamma_1 + \alpha_s^2 \gamma_2 + \dots]$$

Normalisation:

$$f_n(\theta_n^f) = N_n^f \theta_n^f \quad \text{with} \quad N_n^f = 4^n C_r C_A^{n-1} (n-1)!$$

$$\gamma_n(\theta_n^\gamma) = N_n^\gamma \theta_n^\gamma \quad \text{with} \quad N_n^\gamma = 4^{n+1} C_r C_A^n$$



Higgs p_T spectrum

[Cal, Lim, Scott, Tackmann Waalewijn 2408.13301]

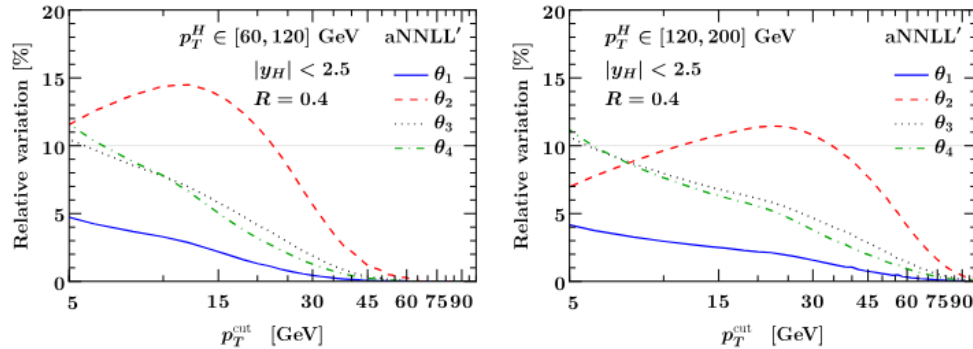
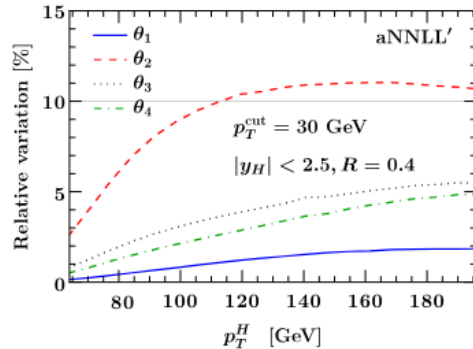


Figure 6: Relative uncertainty from varying each theory nuisance parameter as a function of p_T^{cut} for two different STXS bins.



Example: incomplete knowledge of NNLL resummation

→ some two-loop ingredients unknown

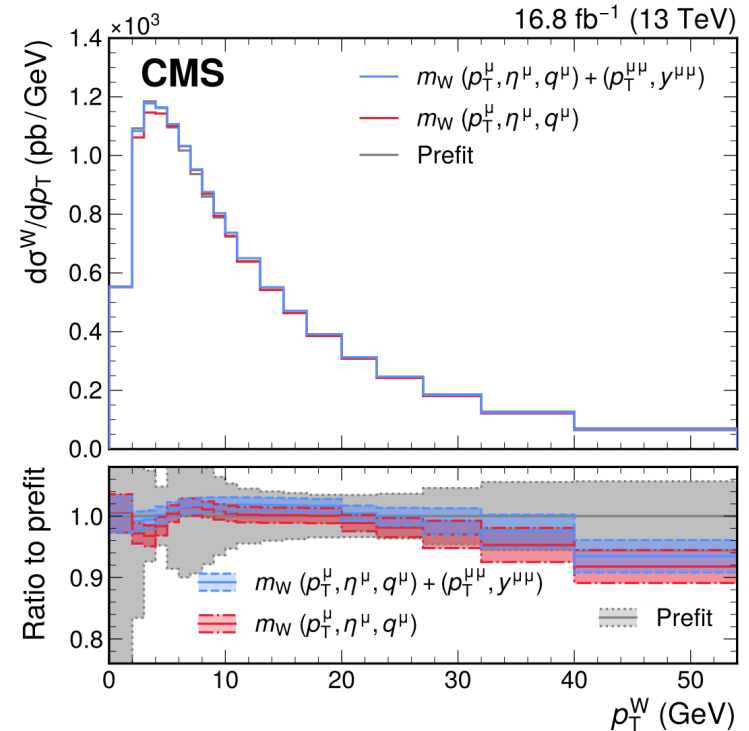
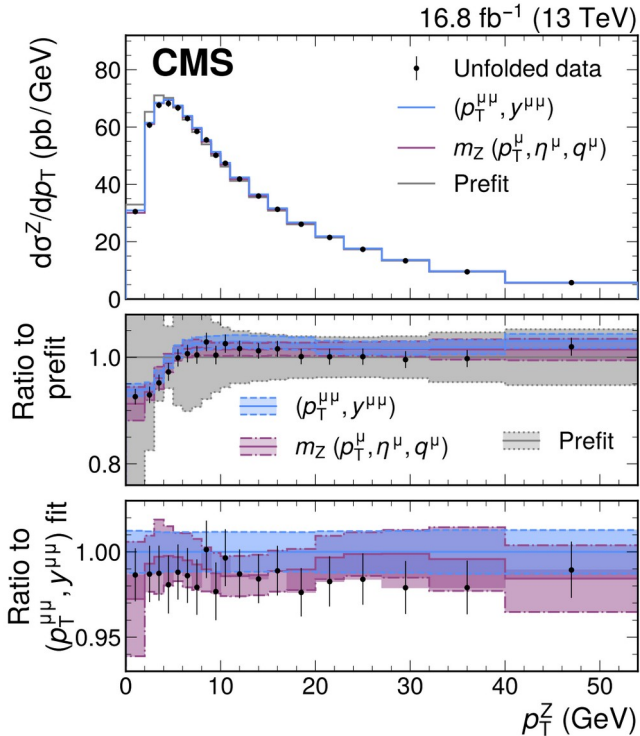
→ parametrise by TNPs

→ Make predictions and vary TNPs:

- correlated uncertainty for different bins!
- See impact of different missing ingredients

Constraint of TNPs from data \rightarrow W-mass extraction

Resummation ingredients the same for W or Z production
 \rightarrow constraint from precisely measured $p_T(Z)$ \rightarrow use for $p_T(W)$
 \rightarrow massive reduction of unc. with correct correlations!



Some remarks on TNPs in resummation

Picture: simple ingredients that enter different computations/processes etc.

→ ideal situation

But actually not that simple:

- Scheme dependence of ingredients? E.g. scales, IR subtraction, ...
→ might need modified parametrisations
- Some TNPs represent directly numbers: Γ , γ , H for simple processes
but others are functions → Beam functions, hard functions for more complicated processes
- Parametrisation works for the resummed spectrum. What about other observables?
- “Easy to implement” for use-cases so far
→ might be really expensive if each variation needs a full computations (Monte Carlos,...)

TNP approach for fixed-order computations

[Lim, Poncelet, 2412.14910]

$$d\sigma = \alpha_s^n N_c^m d\bar{\sigma}^{(0)} + \alpha_s^{n+1} N_c^{m+1} d\bar{\sigma}^{(1)} + \alpha_s^{n+2} N_c^{m+2} d\bar{\sigma}^{(2)} + \dots$$

$$= \alpha_s^n N_c^m d\bar{\sigma}^{(0)} \left[1 + \alpha_s N_c \left(\frac{d\bar{\sigma}^{(1)}}{d\bar{\sigma}^{(0)}} \right) + \alpha_s^2 N_c^2 \left(\frac{d\bar{\sigma}^{(2)}}{d\bar{\sigma}^{(0)}} \right) + \dots \right]$$

Observation, i.e. "expert knowledge": $\frac{d\bar{\sigma}^{(i)}}{d\bar{\sigma}^{(0)}} \sim \mathcal{O}(1)$

Use some knowledge about lower orders but introduce parametric dependence:

$$\frac{d\bar{\sigma}_{\text{TNP}}^{(N+1)}}{d\bar{\sigma}^{(0)}} = \sum_{j=1}^N f_k^{(j)}(\vec{\theta}, x) \left(\frac{d\bar{\sigma}^{(j)}}{d\bar{\sigma}^{(0)}} \right)$$

$x \rightarrow$ mapped kinematic variable

Approximation of original TNP philosophy

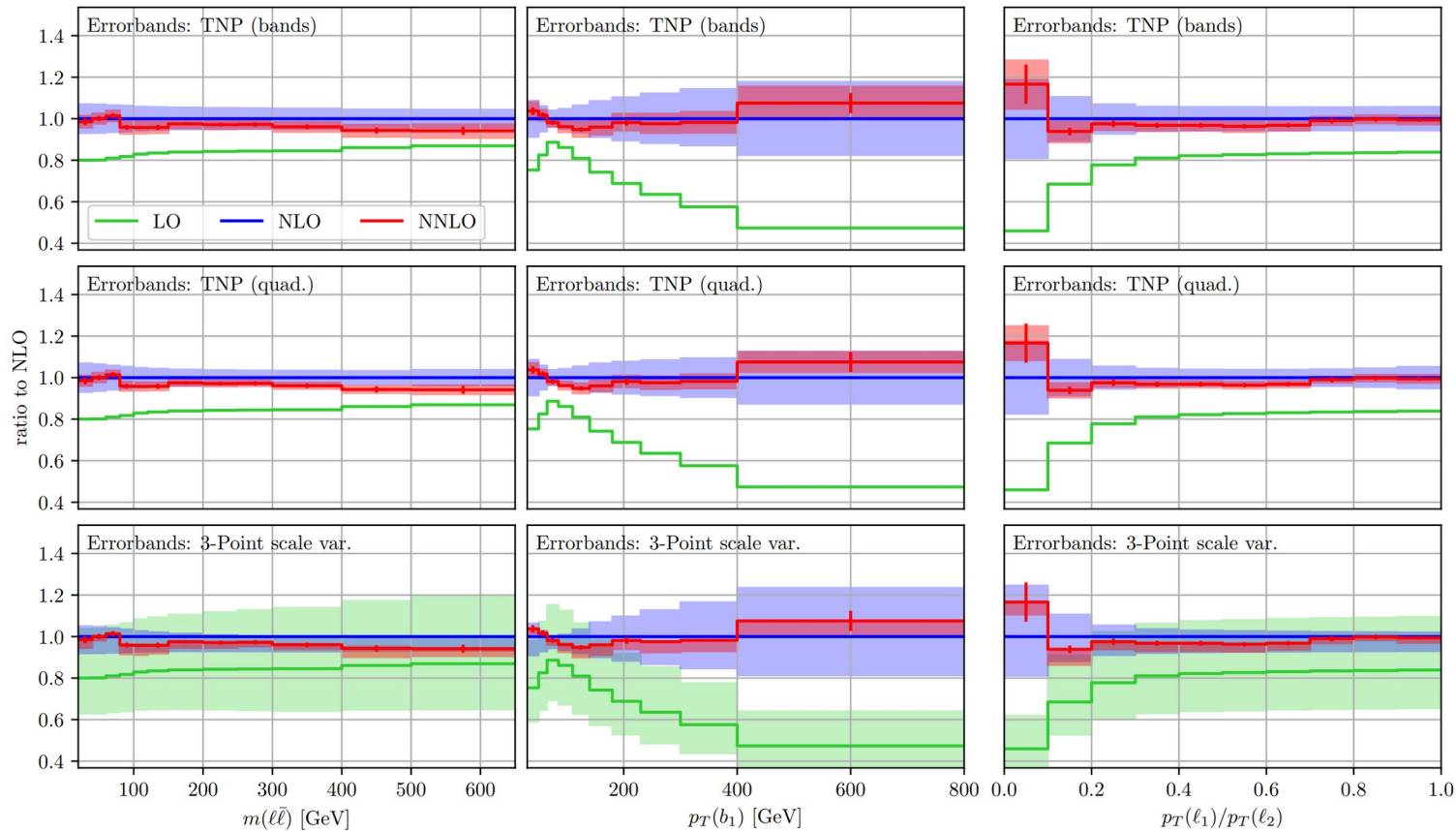
\rightarrow there is only $f_i(\hat{\theta}) \approx \hat{f}_i$

Bernstein: $f_k^B(\vec{\theta}, x) = \sum_{i=0}^k \theta_i \binom{k}{i} x^{k-i} (1-x)^i$
 $x \in [0, 1]$

Chebyshev: $f_k^C(\vec{\theta}, x) = \frac{1}{2} \sum_{i=0}^k \theta_i T_i(x)$
 $x \in [-1, 1]$

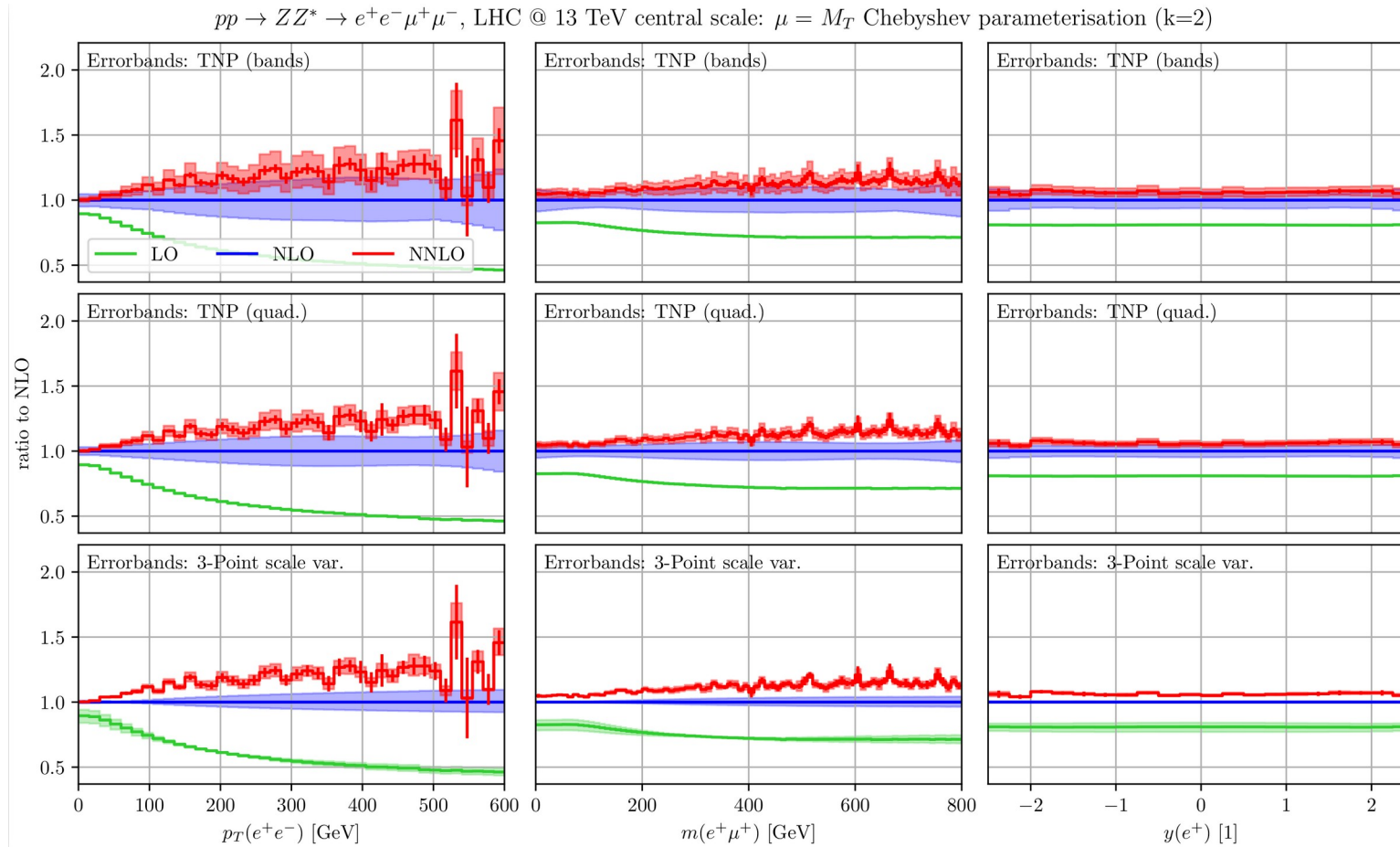
Uncertainties from TNP's - $t\bar{t}$ decays

$pp \rightarrow t\bar{t} \rightarrow \ell\bar{\ell} 2b$ -jets, LHC @ 13 TeV central scale: $\mu = H_T/4$ Bernstein parameterisation ($k=2$)



Band: sample
 $\theta \in [-1, 1]$
 Quad: add individual
 $\theta = \pm 1$
 in quadrature

Uncertainties from TNP's - ZZ

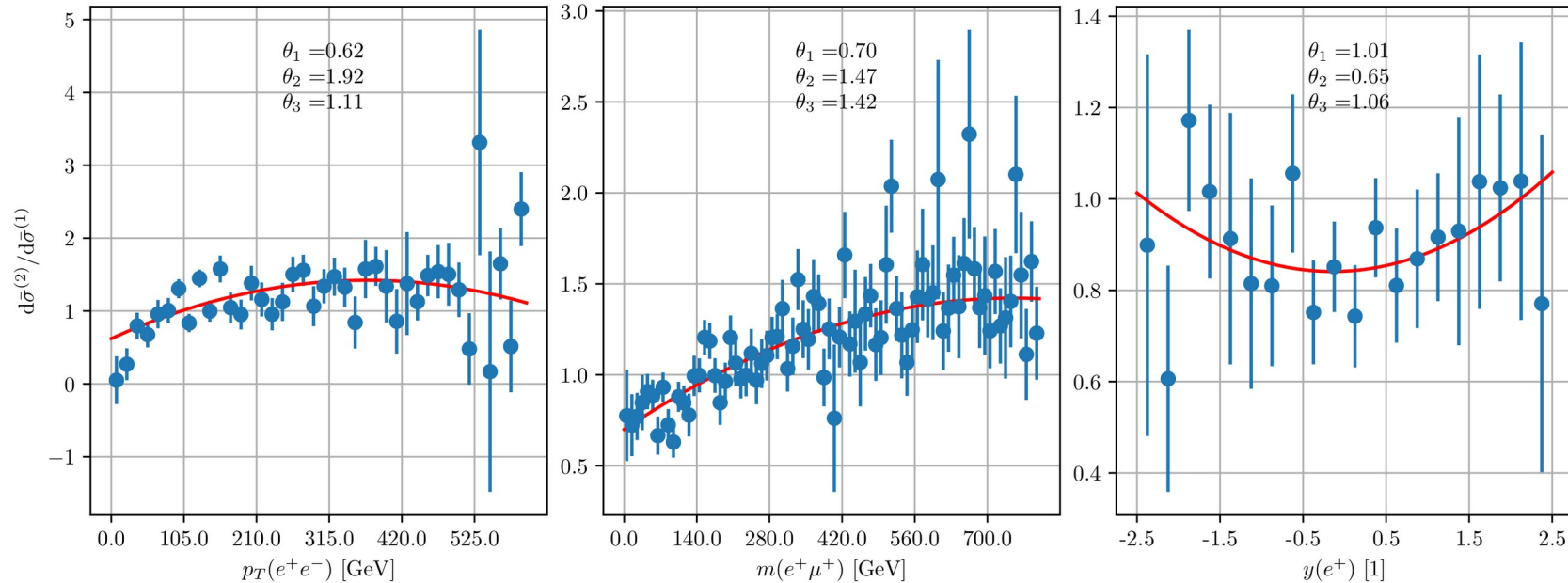


Example of TNP fit: $pp \rightarrow ZZ$

$$\frac{d\bar{\sigma}_{\text{TNP}}^{(N+1)}}{d\bar{\sigma}^{(0)}} = \sum_{j=1}^N f_k^{(j)}(\vec{\theta}, x) \left(\frac{d\bar{\sigma}^{(j)}}{d\bar{\sigma}^{(0)}} \right)$$

$$f_k^B(\vec{\theta}, x) = \sum_{i=0}^k \theta_i \binom{k}{i} x^{k-i} (1-x)^i$$

$pp \rightarrow ZZ^* \rightarrow e^+e^-\mu^+\mu^-$, LHC @ 13 TeV central scale: $\mu = M_T$

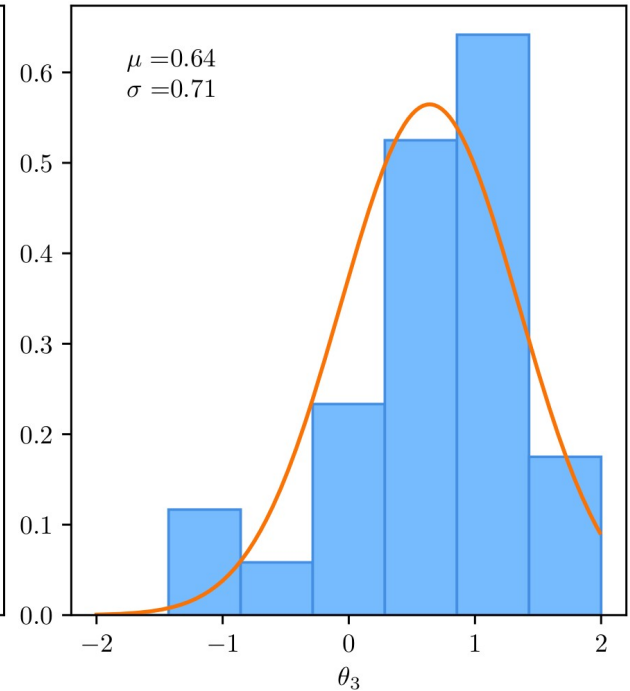
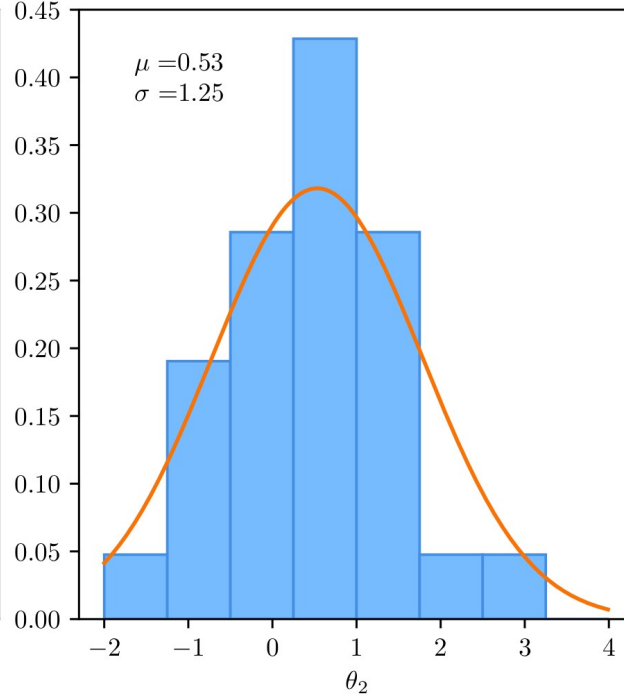
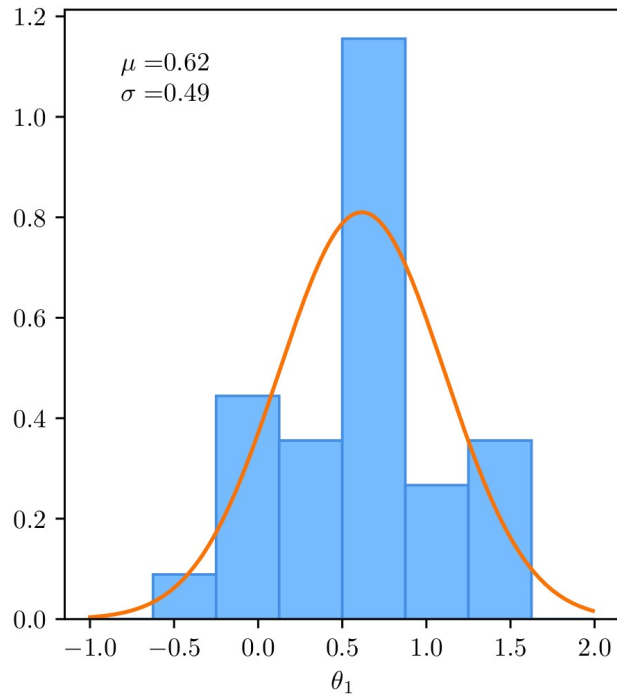


Process meta study

Process	\sqrt{s}/TeV	Scale	PDF	Distributions
$pp \rightarrow H$ (full theory)	13	$m_H/2$	NNPDF3.1	y_H
$pp \rightarrow ZZ^* \rightarrow e^+e^-\mu^+\mu^-$	13	M_T	NNPDF3.1	$M_{e^+\mu^+}, p_T^{e^+e^-}, y_{e^+}$
$pp \rightarrow WW^* \rightarrow e\nu_e\mu\nu_\mu$	13	m_W	NNPDF3.1	M_{WW}, p_T^μ, y_{W^-}
$pp \rightarrow (W \rightarrow \ell\nu) + c$	13	$E_T + p_T^c$	NNPDF3.1	$p_T^\ell, y_\ell ,$
$pp \rightarrow t\bar{t}$	13	$H_T/4$	NNPDF3.1	$M_{t\bar{t}}, p_T^t, y_t$
$pp \rightarrow t\bar{t} \rightarrow b\bar{b}\ell\bar{\ell}$	13	$H_T/4$	NNPDF3.1	$M_{\ell\bar{\ell}}, p_T^{b_1}, p_{T,\ell_1}/p_{T,\ell_2}$
$pp \rightarrow \gamma\gamma$	8	$M_{\gamma\gamma}$	NNPDF3.1	$M_{\gamma\gamma}, p_T^{\gamma_1}, y_{\gamma\gamma}$
$pp \rightarrow \gamma\gamma j$	13	$H_T/2$	NNPDF3.1	$M_{\gamma\gamma}, p_T^{\gamma\gamma}, \cos\phi_{CS}, y_{\gamma_1} , \Delta\phi_{\gamma\gamma}$
$pp \rightarrow jjj$	13	\hat{H}_T	MMHT2014	TEEC with $H_{T,2} \in [1000, 1500), [1500, 2000), [3500, \infty)$ GeV
$pp \rightarrow \gamma jj$	13	H_T	NNPDF3.1	$M_{\gamma jj}, p_T^j, y_{\gamma\text{-jet}} , E_{T,\gamma}$

Fits - Bernstein parametrisation

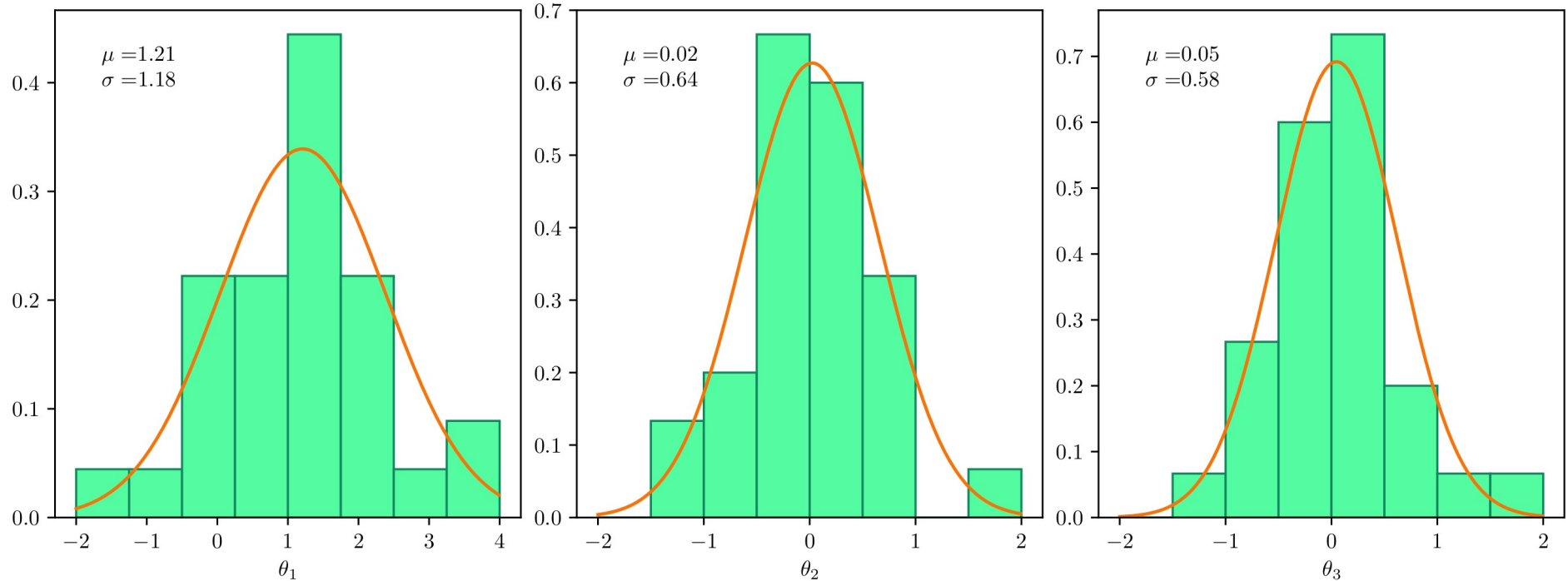
TNPs in Bernstein parameterisation



$$f_k^B(\vec{\theta}, x) = \sum_{i=0}^k \theta_i \binom{k}{i} x^{k-i} (1-x)^i$$

Fits - Chebyshev parametrisation

TNPs in Chebyshev parameterisation

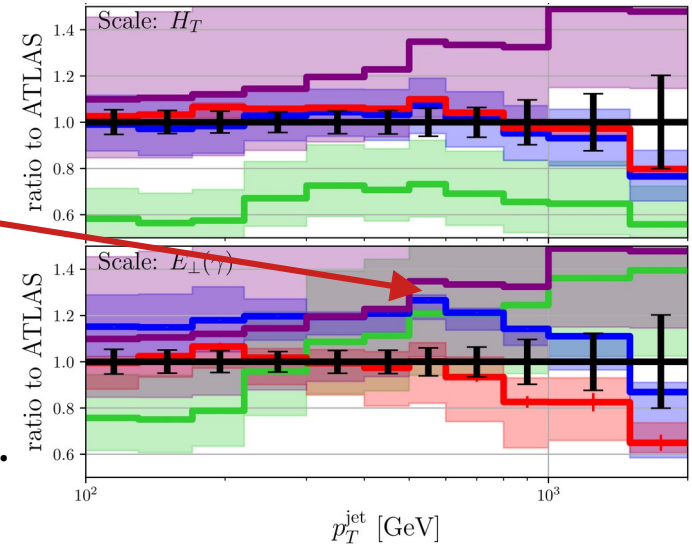


$$f_k^C(\vec{\theta}, x) = \frac{1}{2} \sum_{i=0}^k \theta_i T_i(x)$$

Caveats and open questions

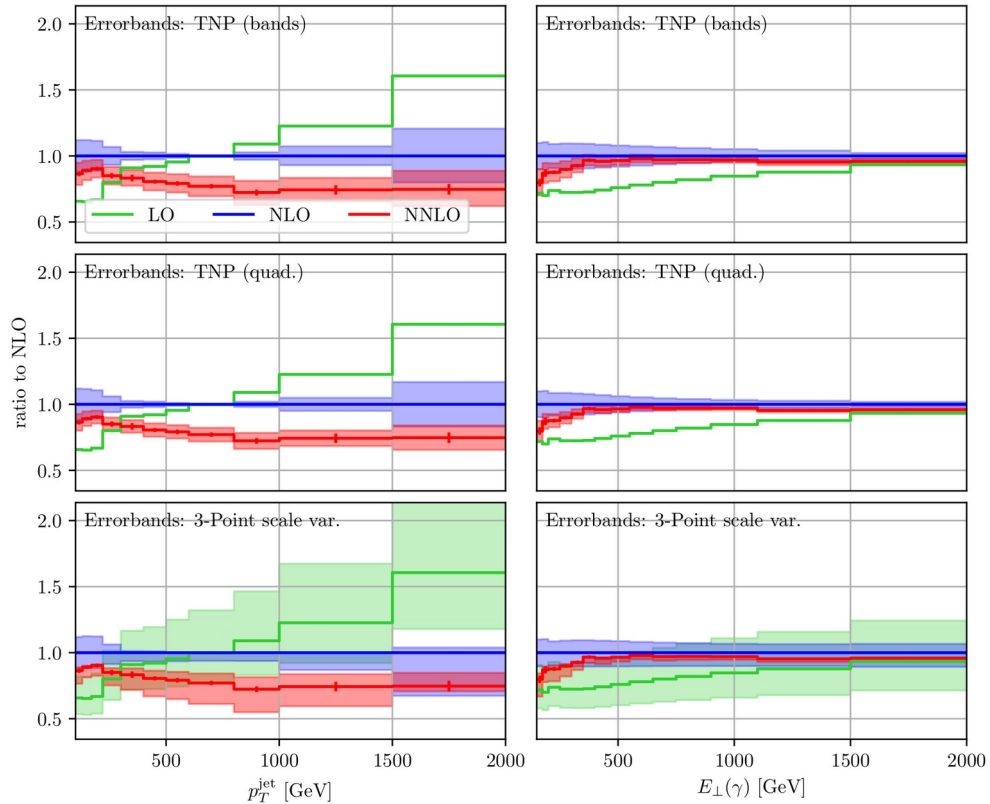
Some arising questions regarding fixed-order model:
$$\frac{d\bar{\sigma}_{\text{TNP}}^{(N+1)}}{d\bar{\sigma}^{(0)}} = \sum_{j=1}^N f_k^{(j)}(\vec{\theta}, x) \left(\frac{d\bar{\sigma}^{(j)}}{d\bar{\sigma}^{(0)}} \right)$$

- How does the uncertainty estimate depend on the central scale choice?
 - **bad scale choices lead to large uncertainties by construction due to large corrections.**
- What about NLO uncertainty if $d\bar{\sigma}^{(1)} = 0$ for given scale?
 - **amend parametrisation by $j = 0$ term.**
- How sensitive are we to the parametrisation? How many terms?
 - **two quite general parametrisations tested, increase degree by demand.**

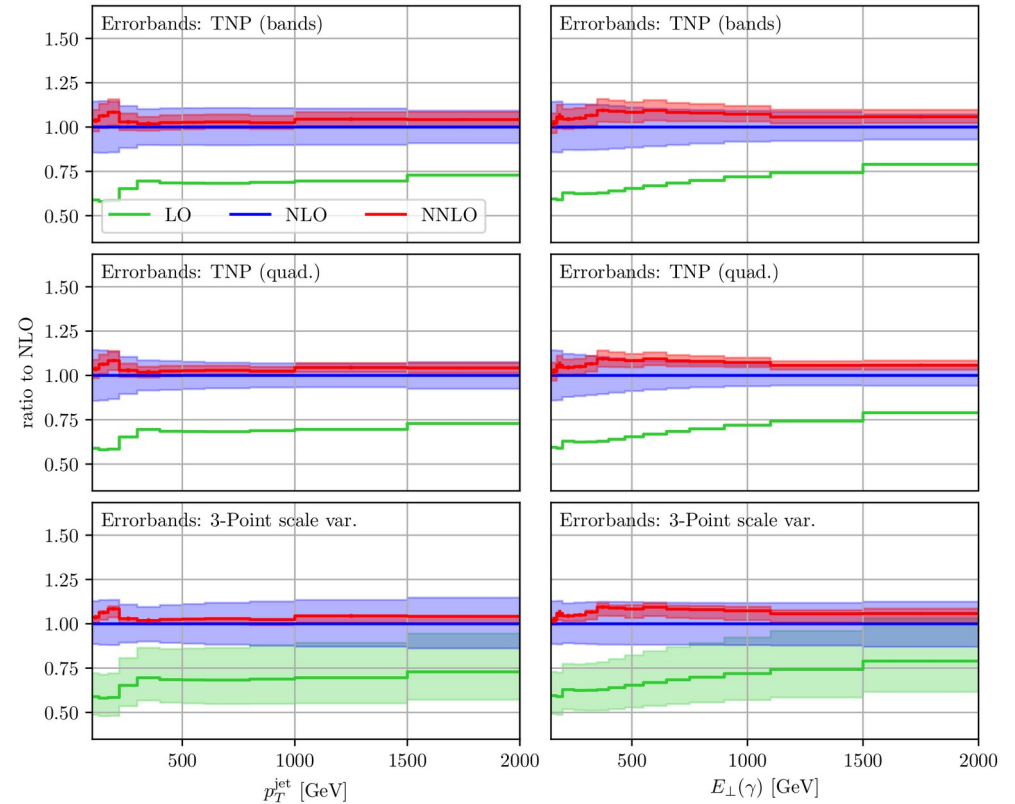


Challenging case

“Bad” scale choice $\mu = E_T$ no $j=0$ term

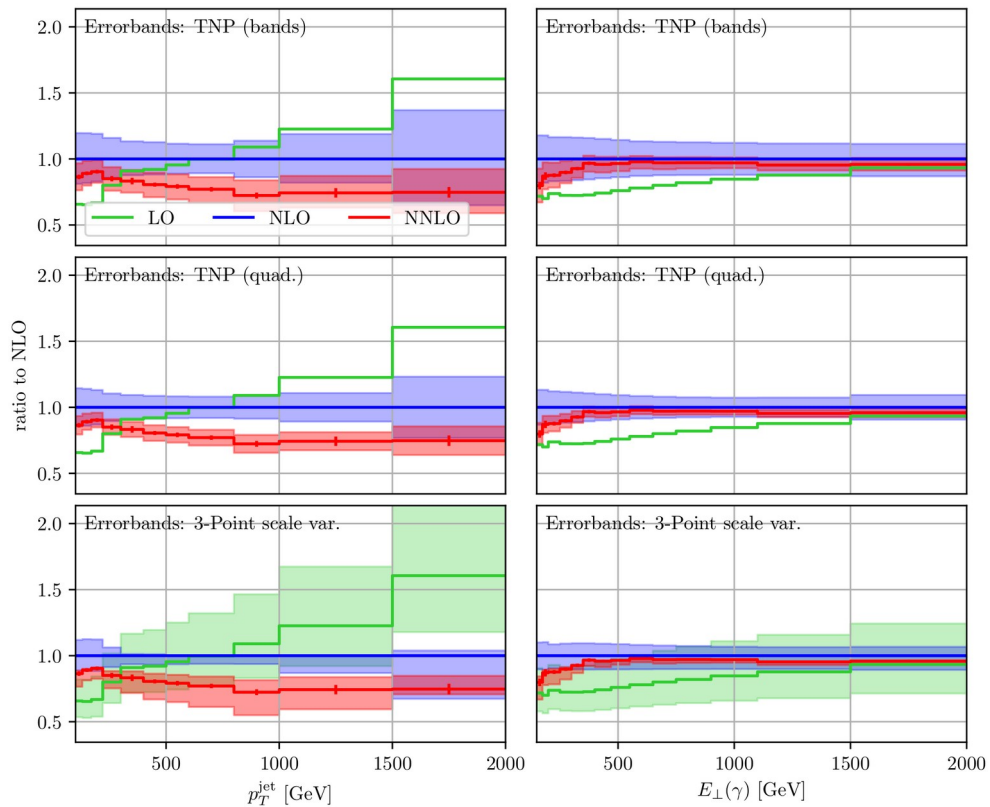


“Good” choice $\mu = H_T$ no $j=0$ term

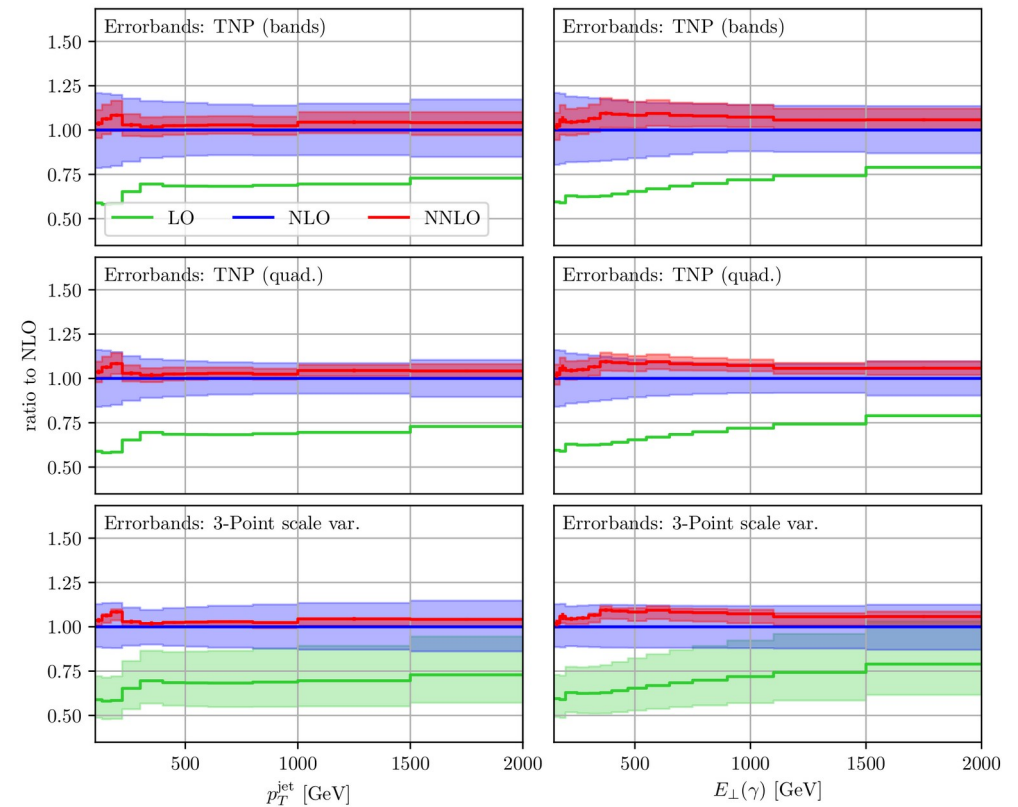


Challenging case \rightarrow extended parametrisations

“Bad” scale choice $\mu = E_T$ with $j=0$ term

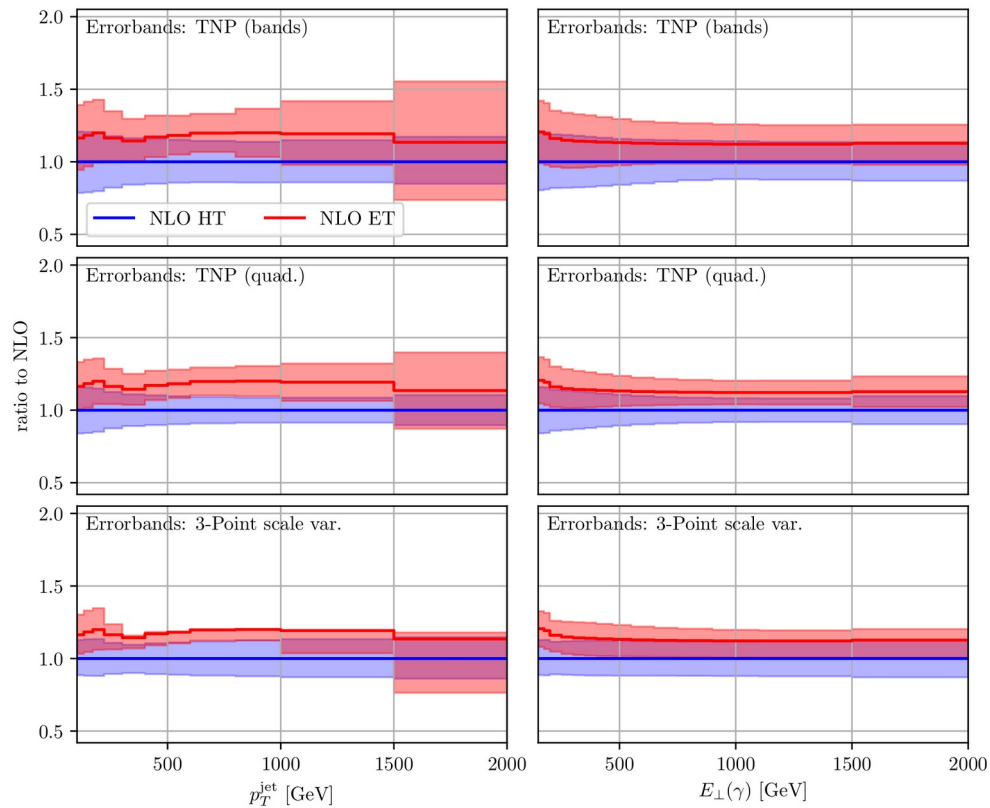


“Good” choice $\mu = H_T$ with $j=0$ term

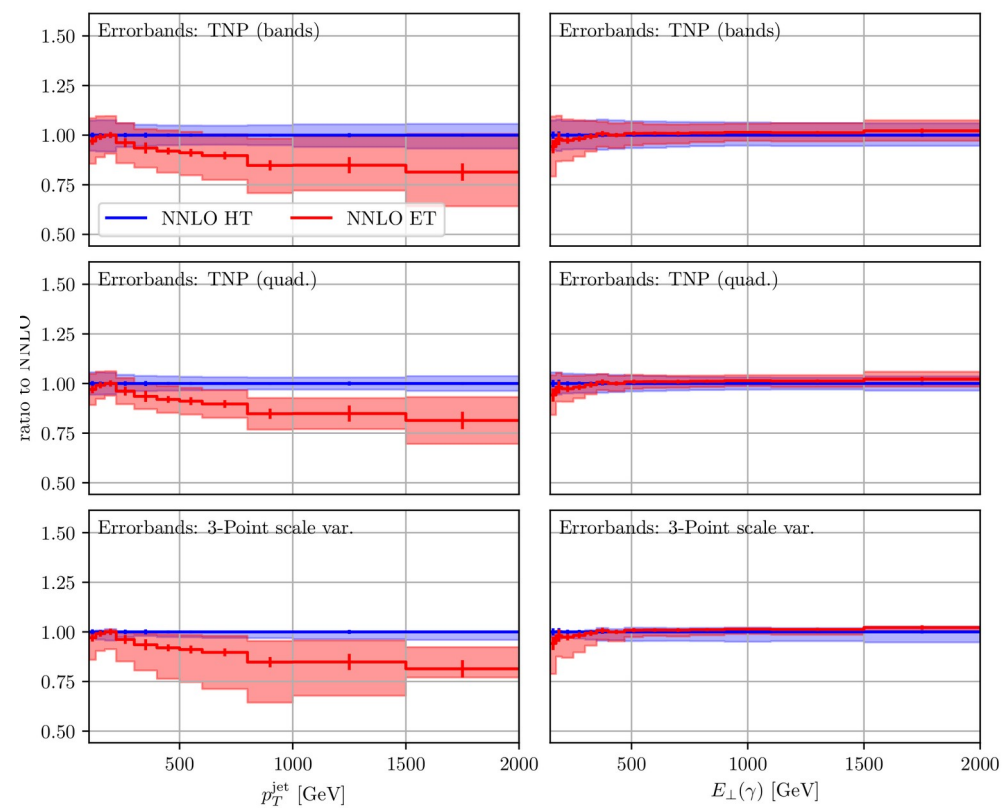


Challenging case → comparisons

NLO QCD



NNLO QCD



More caveats and open questions

Some arising questions regarding fixed-order model: $\frac{d\bar{\sigma}_{\text{TNP}}^{(N+1)}}{d\bar{\sigma}^{(0)}} = \sum_{j=1}^N f_k^{(j)}(\vec{\theta}, x) \left(\frac{d\bar{\sigma}^{(j)}}{d\bar{\sigma}^{(0)}} \right)$

- Each parametrisation is for one observable at a time
 - How to deal with higher dimensional distributions?
 - Consistency upon integration?

→ work in progress

- What about EW corrections?
 - here the approach should work well for Sudakov logs!
 - Radiation from resonances more difficult.
- How to correlate different processes?
 - that's tricky...

$$d\bar{\sigma}^{(n)}(\theta) = d\Phi \langle M^0 | \mathcal{P}(\theta) | M^0 \rangle$$

$\mathcal{P}(\theta)$ → process-independent “operator”

Discussion/Summary/Outlook

- Theory precision is more and more relevant → needs accurate uncertainty estimates
- De-facto standard: scale variations
→ various short-comings: robustness, no statistical interpretation, correlations,...
- Alternative approaches to scale variations: Bayesian and TNP approach
- Theory Nuisance Parameters
 - In principle less biased → does not depend on any “known” orders
 - Statistical interpretation
 - Needs “expert knowledge”
 - Resummed computations are well-suited scenario
 - Fixed-order more difficult: not much knowledge about higher-order terms
Proposed TNP parametrisation shows promising results
→ applications to fits