

Jet calculations with the Sector-improved residue subtraction scheme

Rene Poncelet

LEVERHULME
TRUST



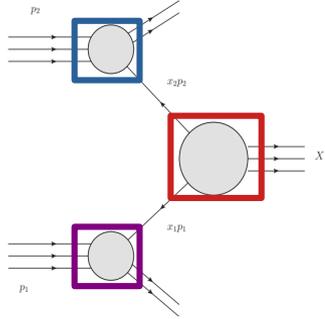
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Sector-improved residue subtraction scheme



$$\sigma_{h_1 h_2 \rightarrow X} = \sum_{ij} \int_0^1 \int_0^1 dx_1 dx_2 \underbrace{\phi_{i,h_1}(x_1, \mu_F^2)}_{\text{PDFs}} \underbrace{\phi_{j/h_2}(x_2, \mu_F^2)}_{\text{PDFs}} \underbrace{\hat{\sigma}_{ij \rightarrow X}(\alpha_s(\mu_R^2), \mu_R^2, \mu_F^2)}_{\text{hard part}}$$

$$\hat{\sigma}_{ab \rightarrow X} = \hat{\sigma}_{ab \rightarrow X}^{(0)} + \hat{\sigma}_{ab \rightarrow X}^{(1)} + \hat{\sigma}_{ab \rightarrow X}^{(2)} + \mathcal{O}(\alpha_s^3) \quad \text{NNLO: } \hat{\sigma}_{ab}^{(2)} = \hat{\sigma}_{ab}^{\text{RR}} + \hat{\sigma}_{ab}^{\text{RV}} + \hat{\sigma}_{ab}^{\text{VV}} + \hat{\sigma}_{ab}^{\text{C2}} + \hat{\sigma}_{ab}^{\text{C1}}$$

Divide and conquer IR singularities by sector decomposition:

$$\hat{\sigma}_{ab}^{\text{RR}} = \frac{1}{2\hat{s}} \int d\Phi_{n+2} \sum_{i,j} \left[\sum_k \mathcal{S}_{ij,k} + \sum_{k,l} \mathcal{S}_{i,k;j,l} \right] \langle \mathcal{M}_{n+2}^{(0)} | \mathcal{M}_{n+2}^{(0)} \rangle F_{n+2} \quad [\text{Czakon'10}]$$

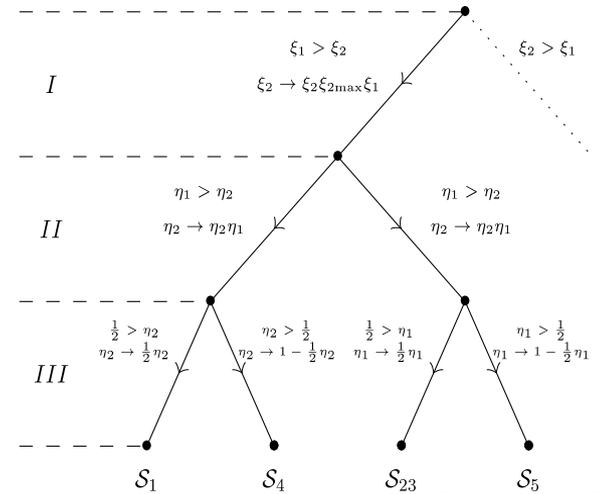
Sector parameterization: $\hat{\eta}_i = \frac{1}{2}(1 - \cos \theta_{ir}) \in [0, 1]$ $\hat{\xi}_i = \frac{u_i^0}{u_{\text{max}}^0} \in [0, 1]$

Overlapping triple collinear singularities: sub-sectors

Apply Master-formula: $x^{-1-b\epsilon} = \underbrace{\frac{-1}{b\epsilon}}_{\text{pole term}} + \underbrace{[x^{-1-b\epsilon}]_+}_{\text{reg. + sub.}}$

→ All contributions numerical finite integrals

→ Numerical ϵ – poles cancellation between real&virtual



[Caola'17]

Applications of sector-improved residue subtraction

Top-quark pairs + NWA decay

High-precision differential predictions for top-quark pairs at the LHC
Czakon, Heymes, Mitov 1511.00549

Higher order corrections to spin correlations in top quark pair production at the LHC
Behring, Czakon, Mitov, Papanastasiou, Poncelet 1901.05407
NNLO QCD corrections to leptonic observables in top-quark pair production and decay
Czakon, Mitov, Poncelet 2008.11133

Jets

Single-jet inclusive rates with exact color at $O(\alpha_s^4)$
Czakon, van Hameren, Mitov, Poncelet 1907.12911

Next-to-Next-to-Leading Order Study of Three-Jet Production at the LHC
Czakon, Mitov, Poncelet 2106.05331

Photons

NNLO QCD corrections to three-photon production at the LHC
Chawdhry, Czakon, Mitov, Poncelet 1911.00479

NNLO QCD corrections to diphoton production with an additional jet at the LHC
Chawdhry, Czakon, Mitov, Poncelet 2105.06940

Weak-bosons/Higgs

NNLO QCD study of polarised W+W- production at the LHC
Poncelet, Popescu 2102.13583

Exact Top-Quark Mass Dependence in Hadronic Higgs Production
Czakon, Harlander, Klappert, Niggetiedt 2105.04436

Weak-boson+jets

NNLO QCD predictions for W+c-jet production at the LHC
Czakon, Mitov, Pellen, Poncelet 2011.01011
Polarised W+j production at the LHC: a study at NNLO QCD accuracy
Pellen, Poncelet, Popescu 2109.14336
Angular coefficients in W+j production at the LHC with high precision
Pellen, Poncelet, Popescu, Vitos 2204.12394

Infrared-safe flavoured anti-kT jets,
Czakon, Mitov, Poncelet 2205.11879

NNLO QCD corrections to Wbb production at the LHC
Hartanto, Poncelet, Popescu, Zoia 2205.01687
Flavour anti-kT algorithm applied to Wbb production at the LHC
Hartanto, Poncelet, Popescu, Zoia 2209.03280

B-hadrons

B-hadron production in NNLO QCD: application to LHC ttbar events with leptonic decays,
Czakon, Generet, Mitov and Poncelet, 2102.08267

NNLO QCD for three jets

Next-to-Next-to-Leading Order Study of Three-Jet Production at the LHC

Czakon, Mitov, Poncelet 2106.05331

NNLO QCD prediction for three jet rates and three-to-two jet ratios:

$$R_{3/2}(X, \mu_R, \mu_F) = \frac{d\sigma_3(\mu_R, \mu_F)/dX}{d\sigma_2(\mu_R, \mu_F)/dX} \sim \alpha_s$$

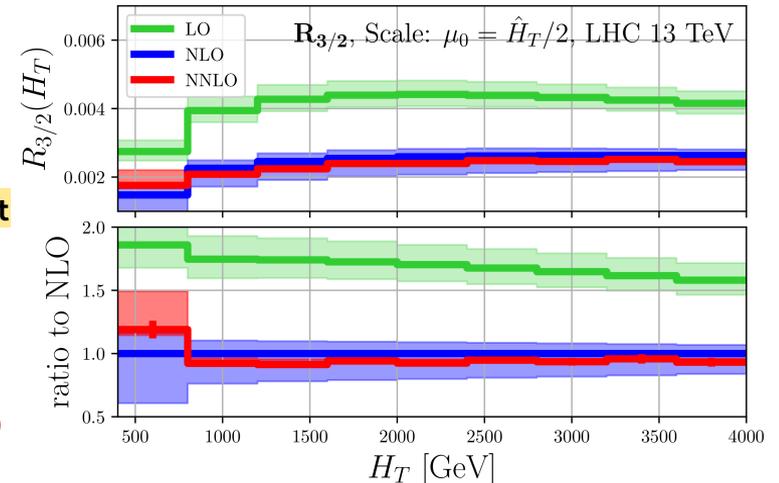
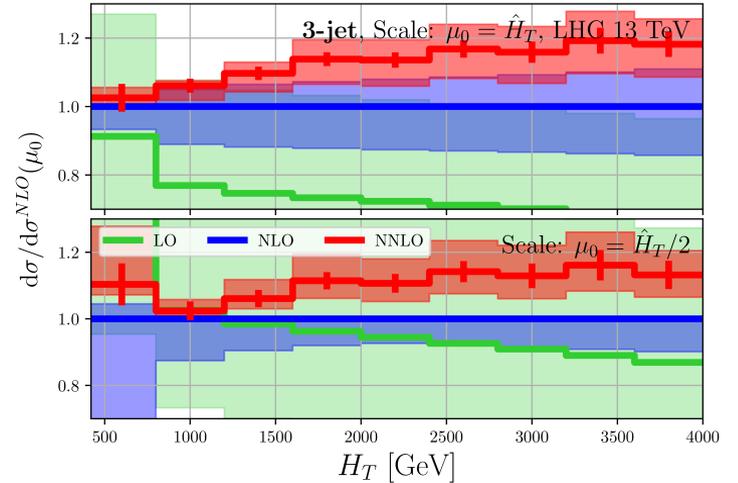
Full colour real radiation + LC double virtual

$$\mathcal{R}^{(2)}(\mu_R^2) = 2 \operatorname{Re} \left[\mathcal{M}^{\dagger(0)} \mathcal{F}^{(2)} \right] (\mu_R^2) + |\mathcal{F}^{(1)}|^2(\mu_R^2) \equiv \mathcal{R}^{(2)}(s_{12}) + \sum_{i=1}^4 c_i \ln^i \left(\frac{\mu_R^2}{s_{12}} \right)$$

$\mathcal{R}^{(2)}(s_{12}) \approx \mathcal{R}^{(2)l.c.}(s_{12})$ **Leading-color two-loop QCD corrections for three-jet production at hadron colliders**

Abreu, Cordero, Ita, Page, Sotnikov 2102.13609

Updated plots due to missing colour factor in VV:
 → VV sizable contribution ~10% → naive sub-leading ~1%



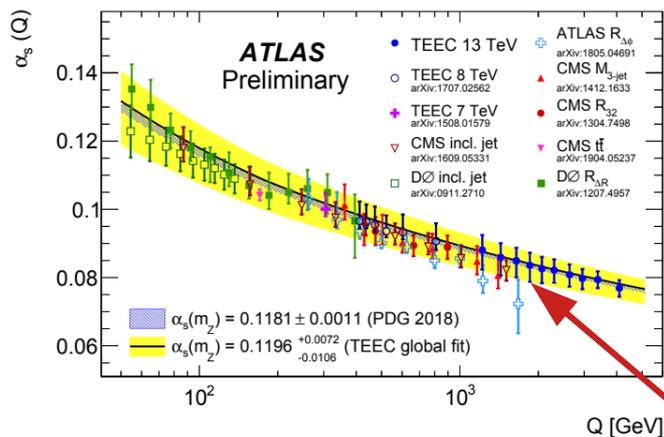
Transverse Energy-Energy Correlator @ LHC

TEEC: Transverse Energy-Energy Correlation

$$\frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} = \frac{1}{N} \sum_{A=1}^N \sum_{ij} \frac{E_{\perp,i}^A E_{\perp,j}^A}{\left(\sum_k E_{T,k}^A\right)^2} \delta(\cos \phi - \cos \phi_{ij})$$

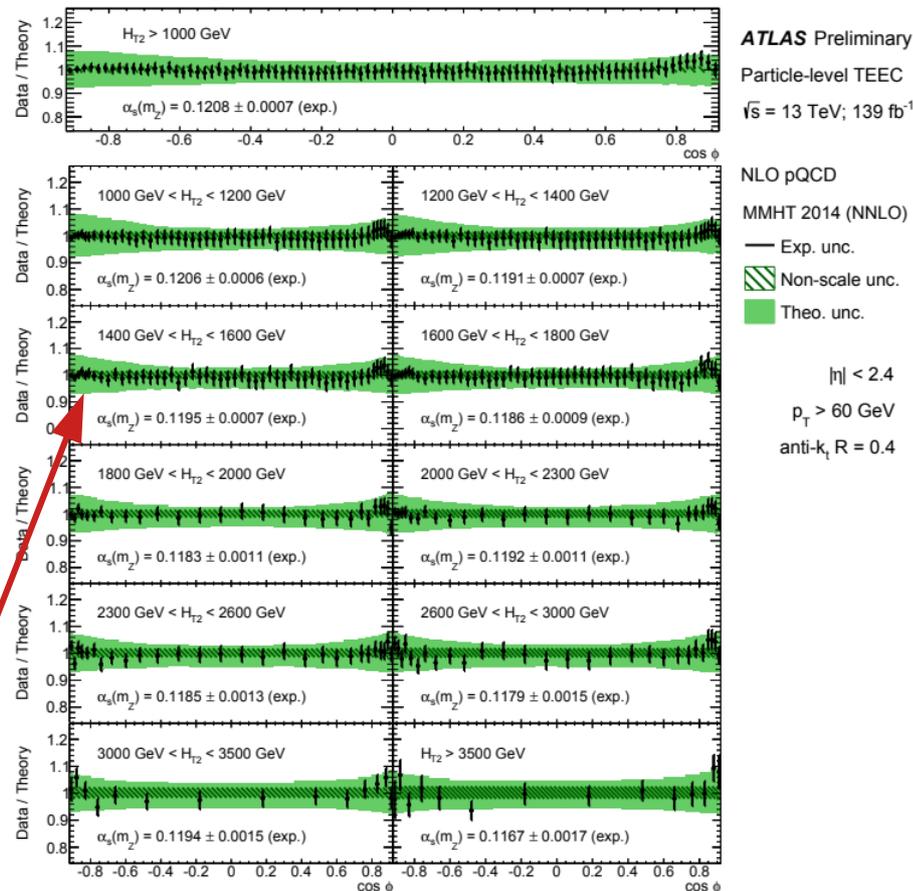
HT2 bins from 1000 GeV to 3500 GeV

→ α_s sensitivity at different energy scales



FO scale uncertainty limiting factor!

ATLAS @ 13 TeV [ATLAS-CONF-2020-025]

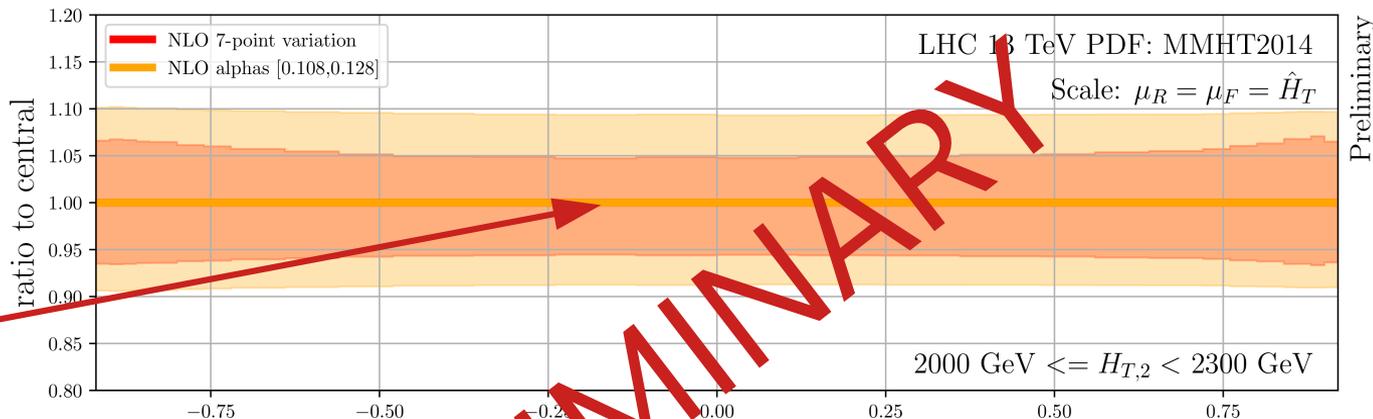


Rene Poncelet - Cambridge

NNLO QCD corrections to TEEC @ LHC

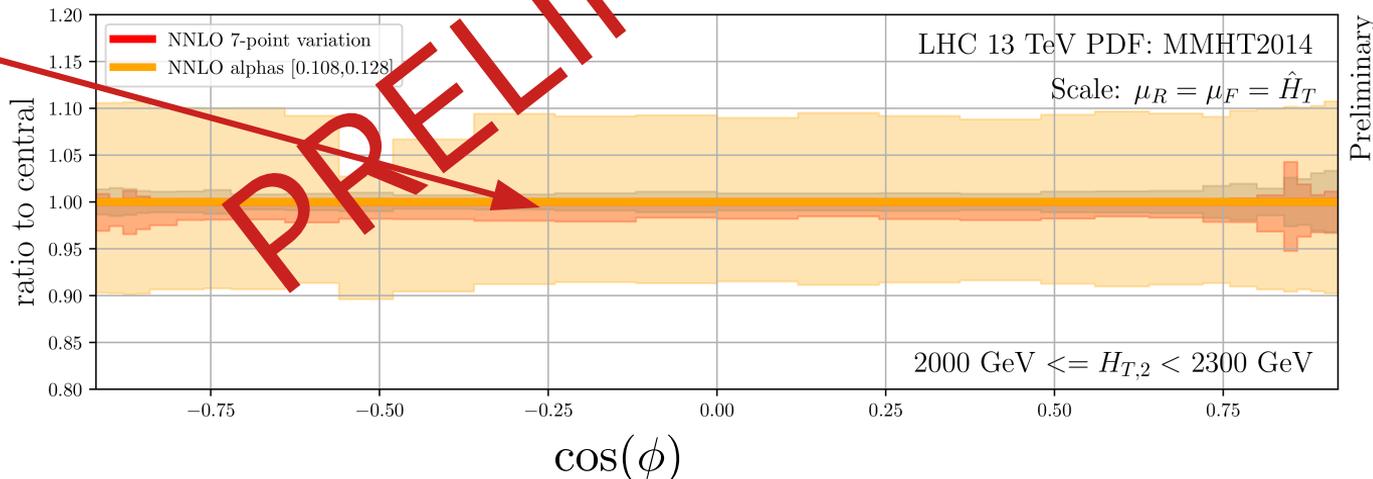
Massive thanks to Manuel Alvarez and Javier Llorente for computing support!

NLO



Reduction in
scale dependence
by factor 3-4

NNLO



Event shapes at the LHC

ATLAS measurement of event shapes @ 13 TeV using multi-jet events (139fb^{-1}) in HT2 bins and high p_T jets ($> 100\text{ GeV}$): [[ATLAS:2007.12600](#)]

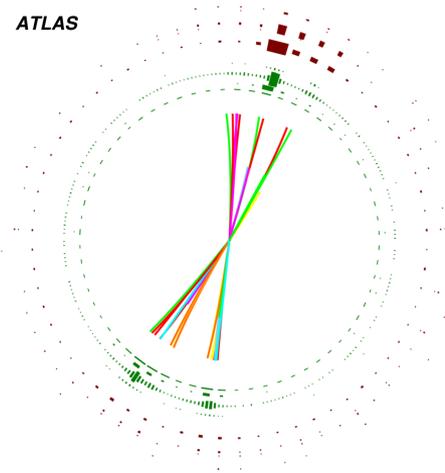
Jet-based
Transverse Thrust: $\tau_T = 1 - \frac{\sum_i^{\text{jets}} |\vec{p}_{T,i} \cdot \hat{n}|}{\sum_i^{\text{jets}} |\vec{p}_{T,i}|}$

Jet-based
Thrust Minor: $T_m = \frac{\sum_i^{\text{jets}} |\vec{p}_{T,i} \times \hat{n}|}{\sum_i^{\text{jets}} |\vec{p}_{T,i}|}$

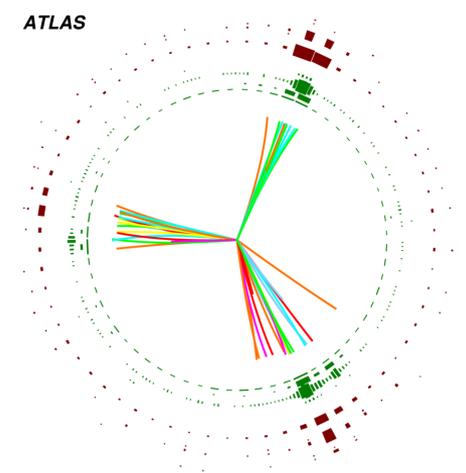
More quantities based on eigenvalues of (transverse) linearised sphericity tensor:

$$\mathcal{M}_{xyz} = \frac{1}{\sum_i^{\text{jets}} |\vec{p}_i|} \sum_i^{\text{jets}} \frac{1}{|\vec{p}_i|} \begin{pmatrix} p_{x,i}^2 & p_{x,i}p_{y,i} & p_{x,i}p_{z,i} \\ p_{y,i}p_{x,i} & p_{y,i}^2 & p_{y,i}p_{z,i} \\ p_{z,i}p_{x,i} & p_{z,i}p_{y,i} & p_{z,i}^2 \end{pmatrix}$$

Back-to-Back



Spherical



NNLO QCD corrections to event shapes

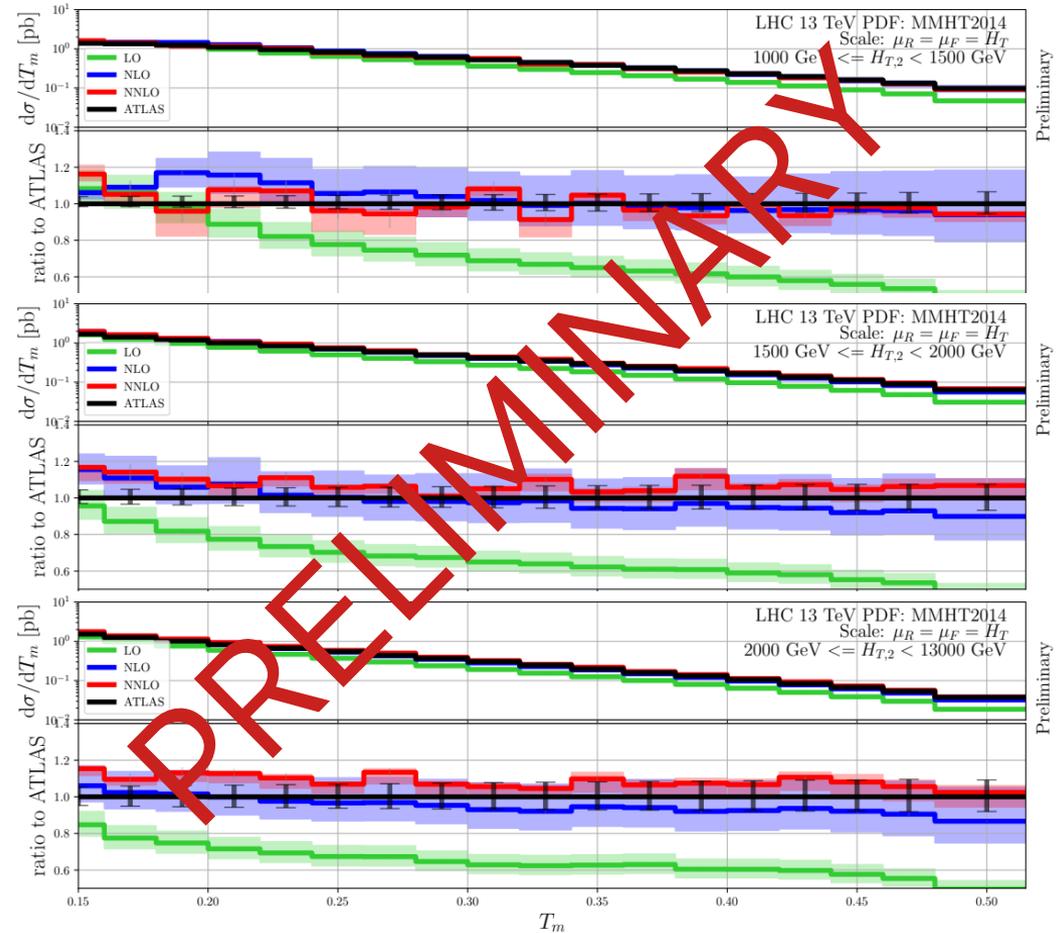
Comparison of public data from HEPdata

Example Thrust-Minor:

- Beautiful perturbative convergence
- Significant reduction of perturbative corrections

Question to be addressed:

- Resummation effects
- Non-perturbative corrections



IR-safety of flavour observables

NNLO QCD: $d\sigma \ni d\Phi_{n+2} \left(\text{Diagram} \right) F_{n+2} + \dots + d\tilde{\Phi}_{n+2} \mathcal{S}_2 \left(\text{Diagram} \right) F_n$

IR safety implies correlated treatment of kinematics and flavour information:

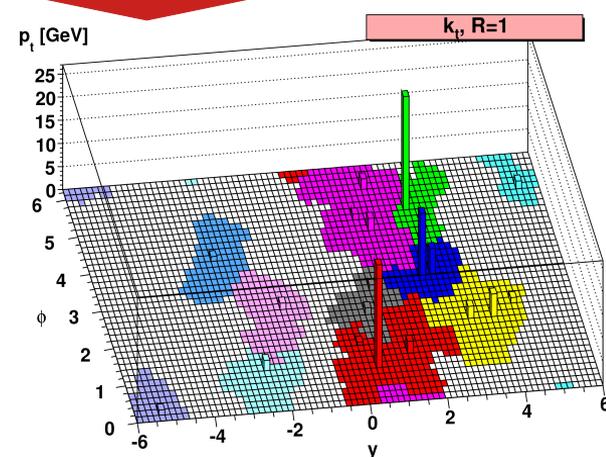
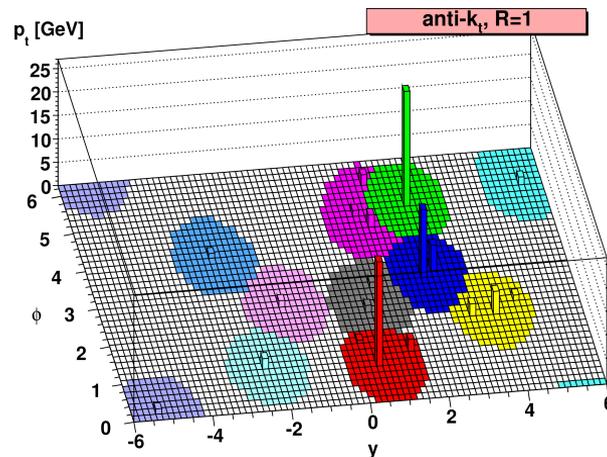
Infrared safe definition of jet flavor,
Banfi, Salam, Zanderighi hep-ph/0601139

Towards Jetography
Salam 0906.1833

Open issues:

- Requires flavour-information
- (flavour-) kT and anti-kT cluster partonic jets differently

A proper comparison requires to
unfold experimental data



Old problem, new approaches

Renewed interest:

- Anti-kT + flv.-kT flavour matching:

QCD-aware partonic jet clustering for truth-jet flavour labelling Buckley, Pollard 1507.00508

Practical Jet Flavour Through NNLO

Caletti, Larkoski, Marzani, Reichelt 2205.01109

A dress of flavour to suit any jet

Gauld, Huss, Stagnitto 2208.11138

- Fixed-order fragmentation:

B-hadron production in NNLO QCD: application to LHC ttbar events with leptonic decays, Czakon, Generet, Mitov and Poncelet, 2102.08267

A Fragmentation Approach to Jet Flavor

Caletti, Larkoski, Marzani, Reichelt 2205.01117

- Modified anti-kT algorithm:

Infrared-safe flavoured anti-kT jets, Czakon, Mitov, Poncelet 2205.11879

Proposed modification:

A soft term designed to modify the distance of flavoured pairs.

$$d_{ij}^{(F)} = d_{ij} \begin{cases} \mathcal{S}_{ij} & i,j \text{ is flavoured pair} \\ 1 & \text{else} \end{cases}$$

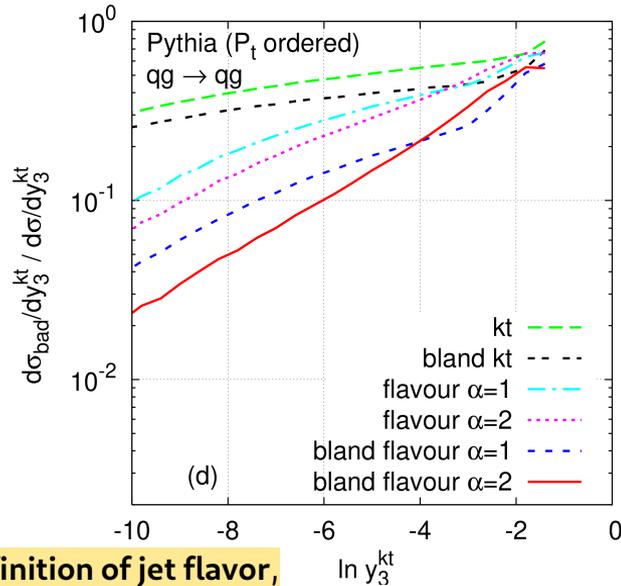
$$\mathcal{S}_{ij} = 1 - \theta(1 - x) \cos\left(\frac{\pi}{2}x\right) \quad \text{with} \quad x = \frac{k_{T,i}^2 + k_{T,j}^2}{2ak_{T,\max}^2}$$

Tests of IR safety with parton showers

Dress tree-level di-jet events (definite flavour structure: "qq", "qg" or "gg") with radiation and study jet flavour (q or g) as function of kinematics.

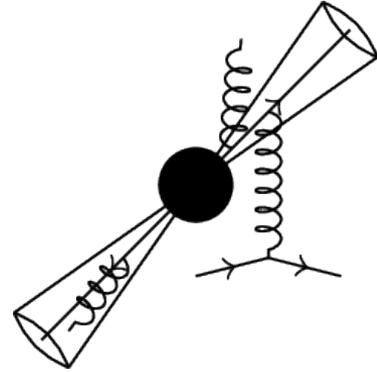
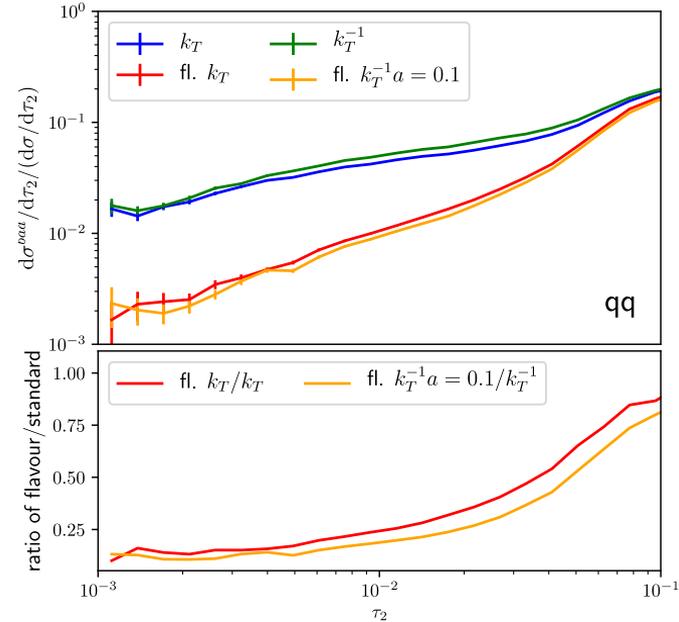
In the di-jet limit the flavour needs to correspond to tree level flavours
 → misidentification rate needs to vanish in di-jet back-to-back limit

Flavour k_T vs. k_T :



Infrared safe definition of jet flavor,
 Banfi, Salam, Zanderighi hep-ph/0601139

Flavour anti- k_T :



Tests of IR safety with NNLO FO computations

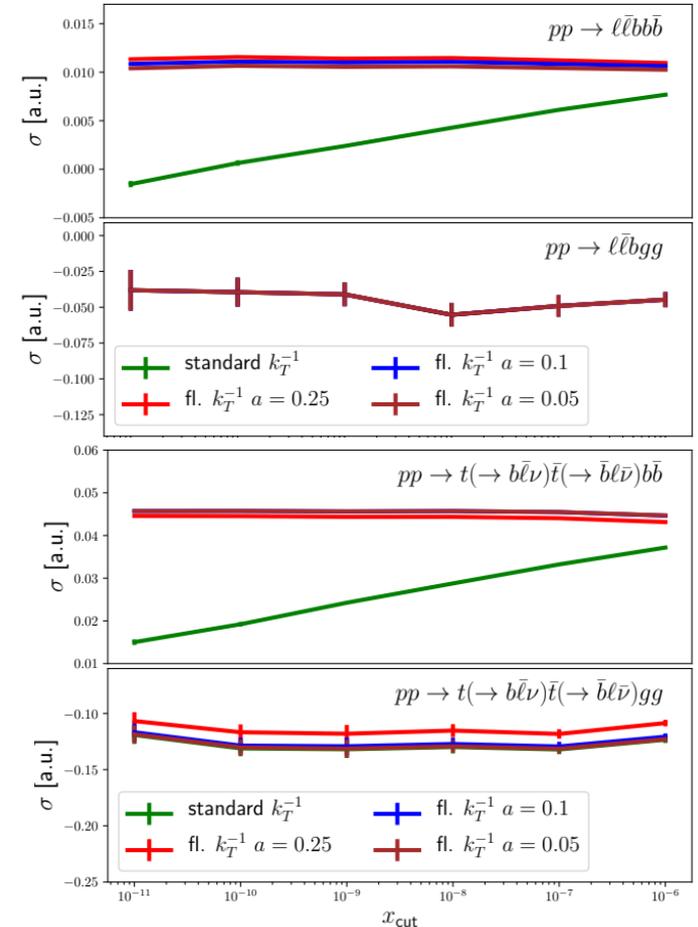
IR sensitivity of jet cross sections on (technical) IR regulating parameter x

$$d\sigma \ni d\Phi_{n+2} \left(\text{Diagram 1} \right) F_{n+2} + \dots + d\tilde{\Phi}_{n+2} \mathcal{S}_2 \left(\text{Diagram 2} \right) F_n \theta(x - x_{\text{cut}})$$

In the limit $x_{\text{cut}} \rightarrow 0$:

IR safe jet flavour \rightarrow no dependence on x_{cut}

IR non-safe jet flavour \rightarrow logarithmic divergent



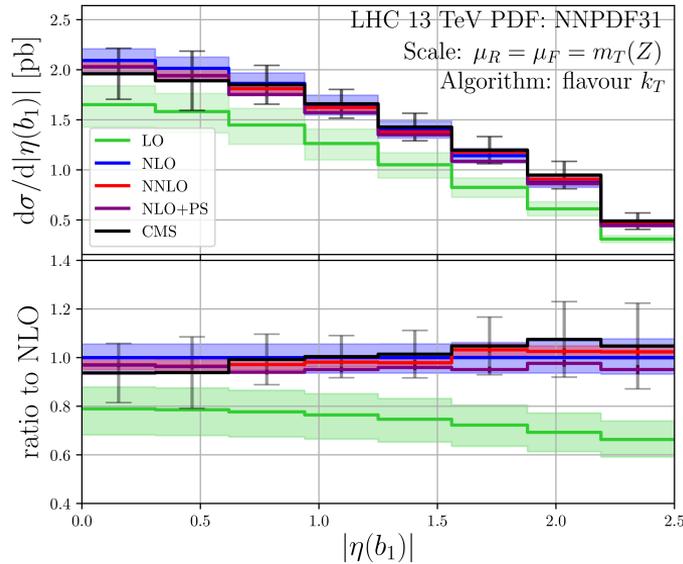
Z+b-jet Phenomenology: Tunable parameter

Benchmark process: $pp \rightarrow Z(\ell\ell) + b\text{-jet}$

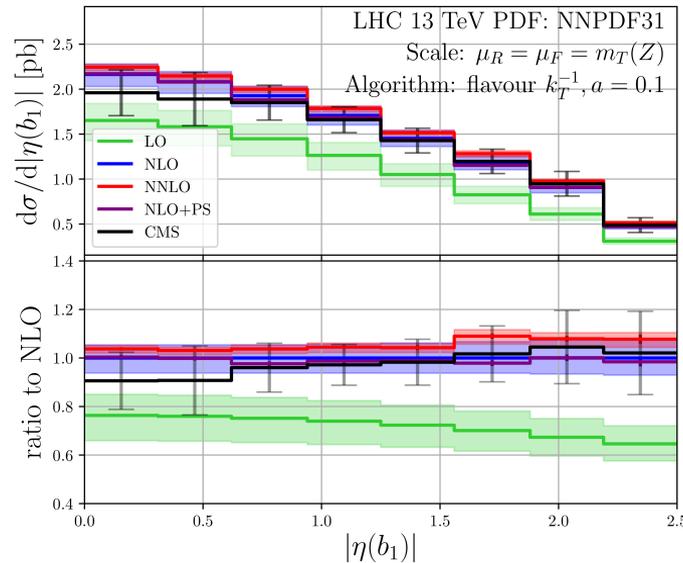
Tunable parameter a :

- Limit $a \rightarrow 0 \Leftrightarrow$ original anti-kT (IR unsafe)
- Large $a \Leftrightarrow$ large modification of cluster sequence

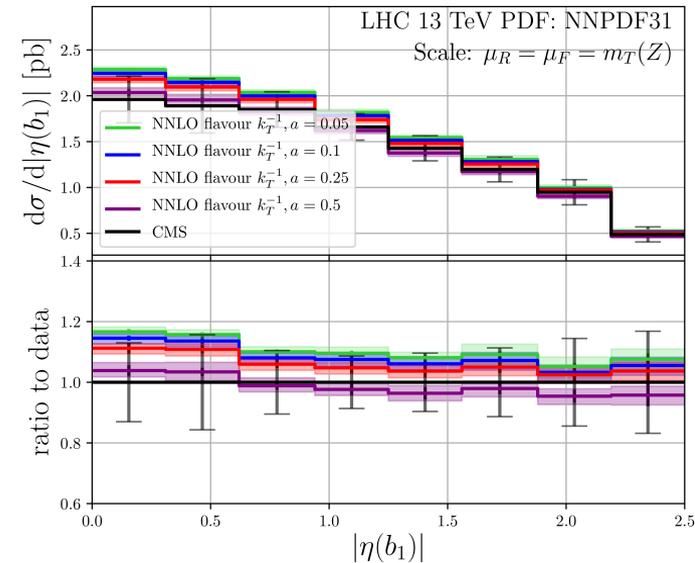
Flavour kT:



Flavour anti-kT: $a = 0.1$

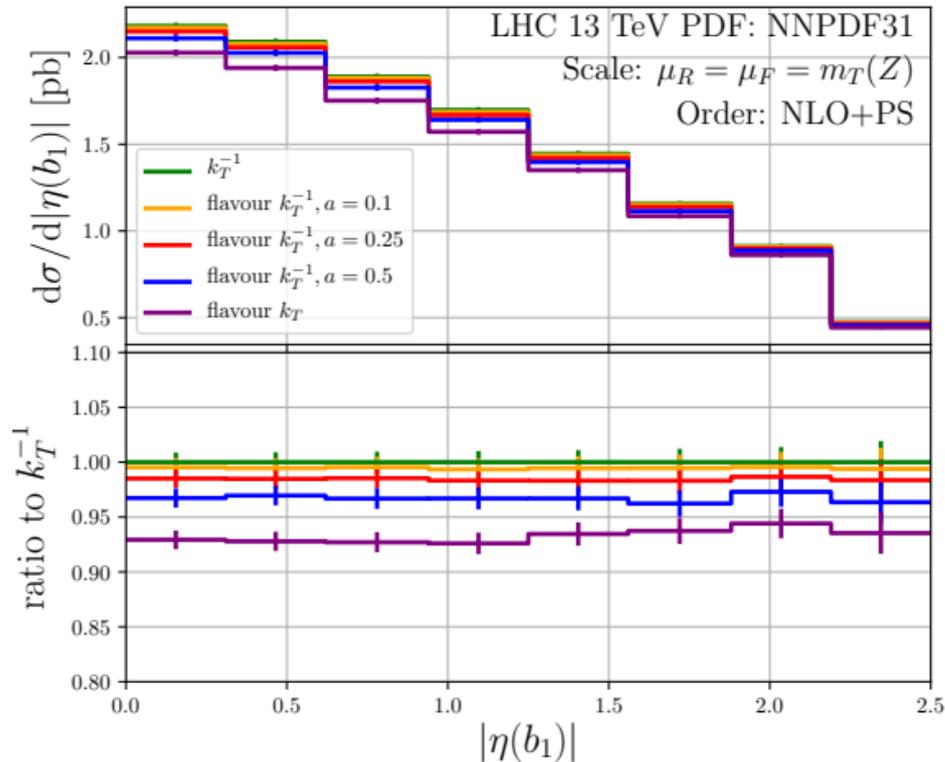


Comparison of different parameter a to data:



Z+b-jet Phenomenology: Tunable parameter II

What happens in the presence of many flavoured partons? → NLO PS



Tunable parameter a:

- Small a: Flavour anti-kT results are more similar to standard anti-kT → **small unfolding factors**
- Larger a: Larger modification of clustering

Good FO perturbative convergence +
Small difference to standard anti-kT
→ $a \sim 0.1$ is a good candidate

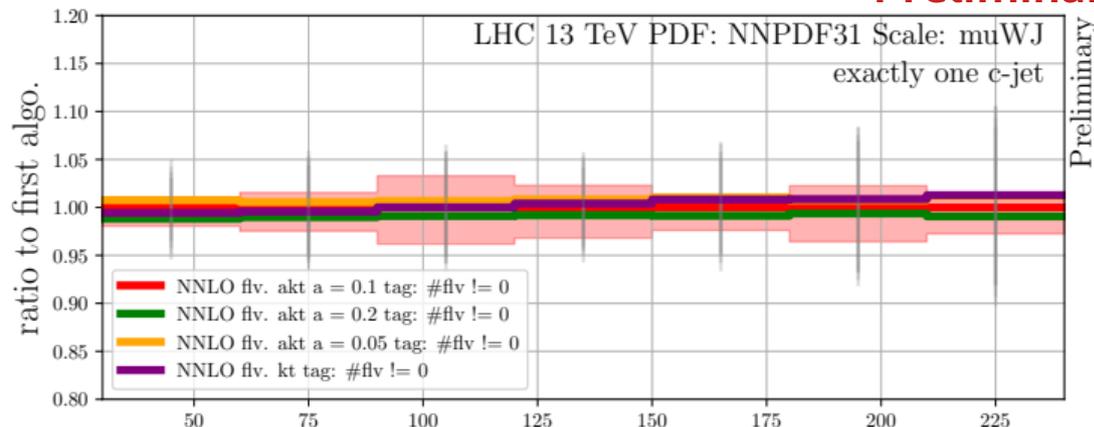
W+c-jet with flavour anti-kT

In collaboration with: Czakon, Mitov, Pellen

Preliminary

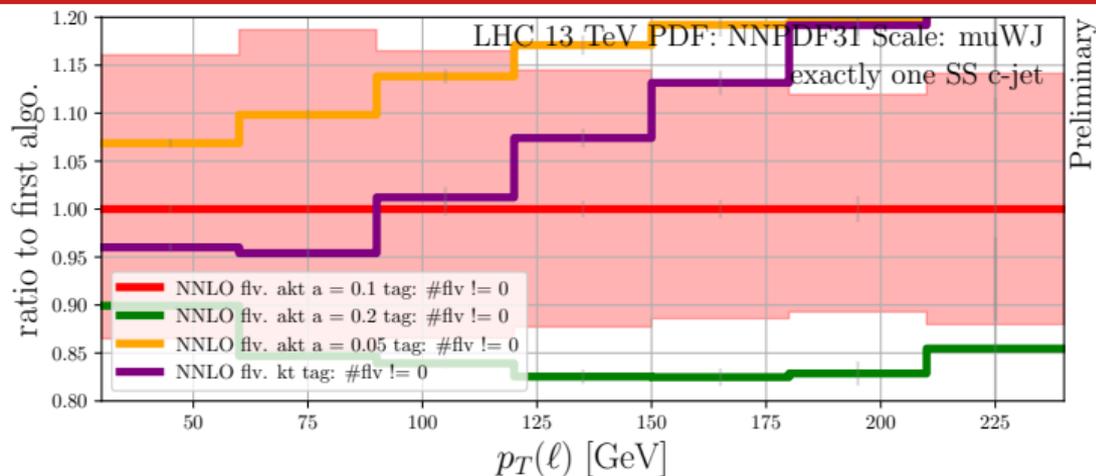
Exactly one c-jet requirement:

- Comparison of parameters a:
→ small dependence < 2%
- Comparison to flv kT:
→ small dependence @ NNLO < 2%



ONLY large effect in SS contribution

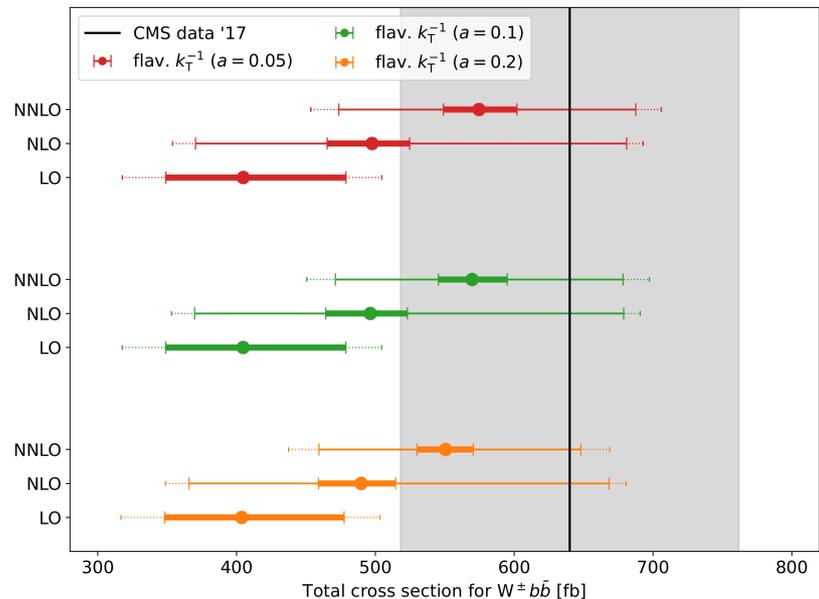
- Exactly one c-jet of SS type:
Larger dependence ~15%
(roughly size of NNLO scale band)
- BUT: SS contribution ~2-5%
- => OS ~0.2-0.5% dependence



W+2 bjets: flavour anti-kT

Flavour anti-kT algorithm applied to Wbb production at the LHC

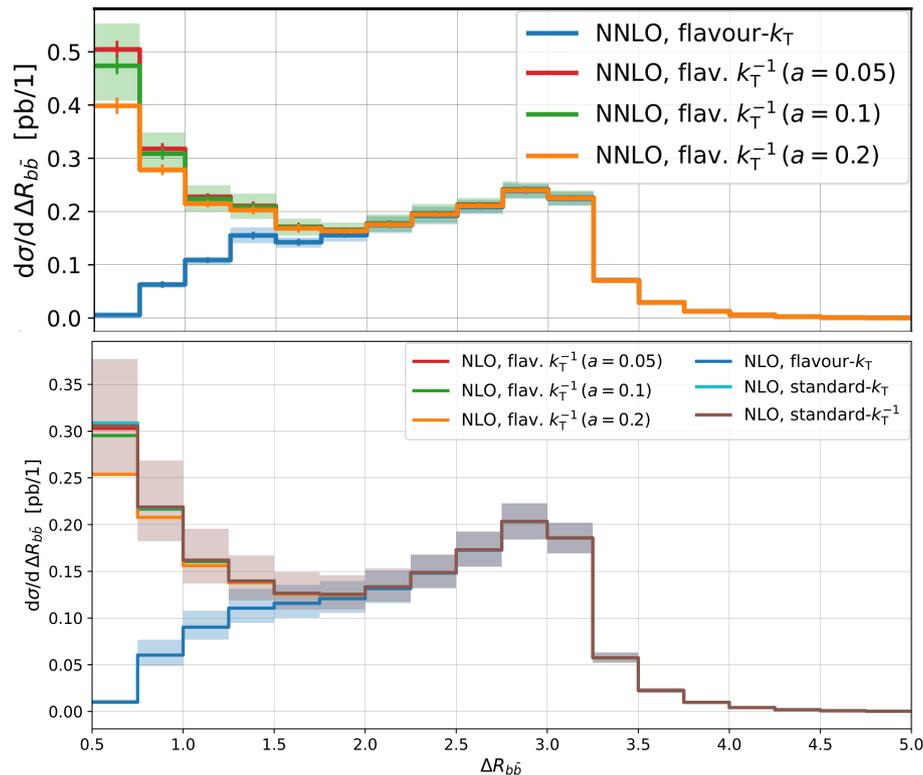
Hartanto, Poncelet, Popescu, Zoia 2209.03280



Comparison to data

Measurement of the production cross section of a W boson in association with two b jets in pp collisions at $\sqrt{s} = 8$ TeV, CMS 1608.07561

(assumes small unfolding corrections → wip)



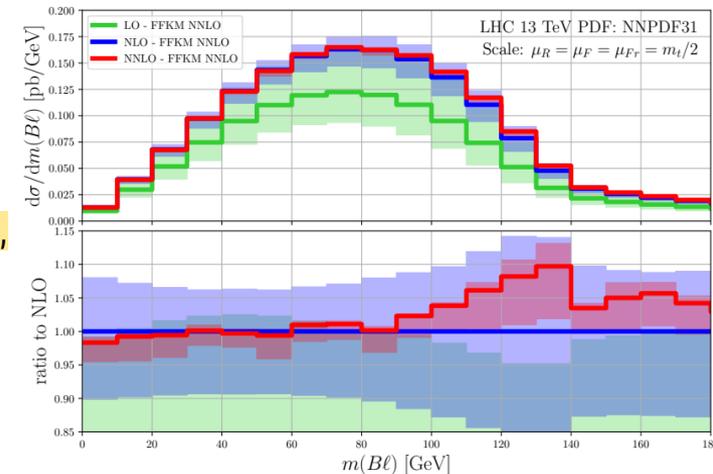
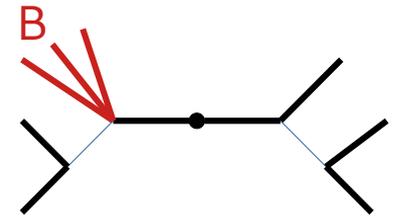
Significant differences between kT and anti-kT
In small DeltaR(bb) region? Beam-function?!

Flavour tagging and fixed order fragmentation

- Fixed order QCD predictions with a final state hadron
- Partonic computation + transition of parton to hadron (collinear fragmentation of massless partons)
- Non-perturbative fragmentation function (similar to PDFs): Probability to find a hadron with a fraction x of a parton
- Advantage is that the hadrons momentum is measurable
→ usage as b-tag?
- Implementation in the STRIPPER framework through NNLO QCD:

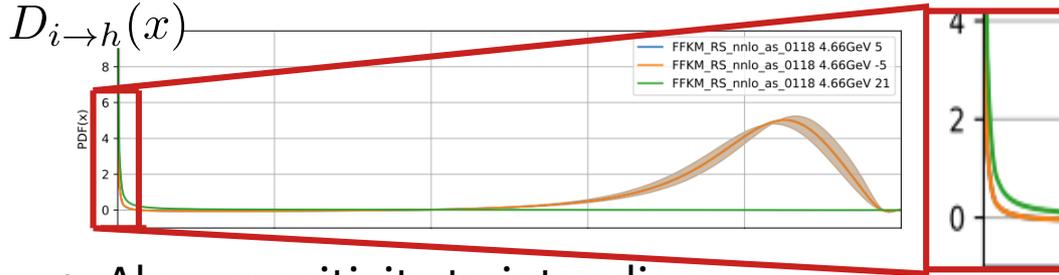
B-hadron production in NNLO QCD: application to LHC $t\bar{t}$ events with leptonic decays,
Czakon, Generet, Mitov and Poncelet, 2102.08267

$$pp \rightarrow t\bar{t} \rightarrow B\ell\bar{\ell}\nu\bar{\nu}b + X$$



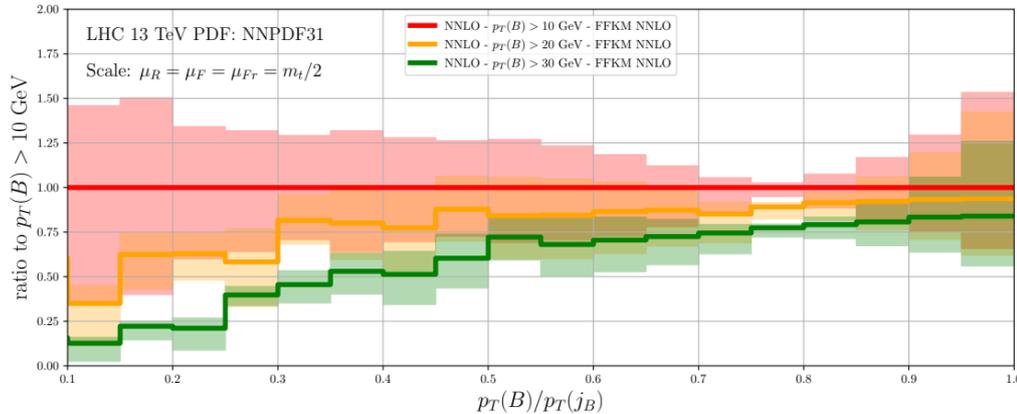
Subtleties

- $p_T(B)$ requirement necessary since NNLO fragmentation function divergent for $x \rightarrow 0$ due to $g \rightarrow b\bar{b}$ splitting:

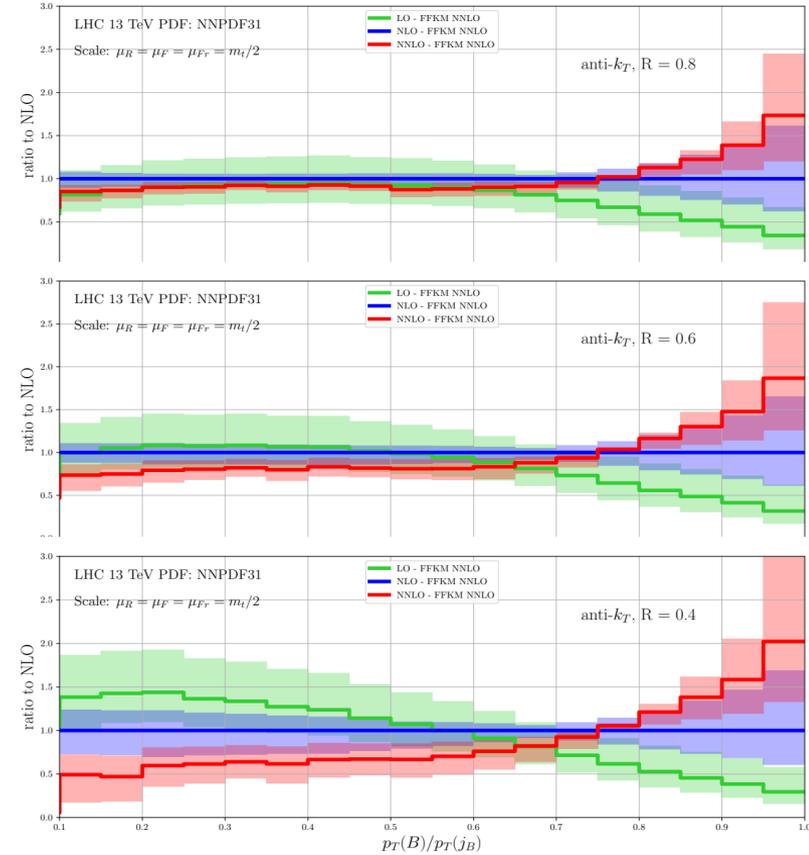


- Also: sensitivity to jet radius

→ Usage as b-tag needs tuning



Jet radius variation $R = 0.8, 0.6, 0.4$



Summary & Outlook

Summary:

- Many phenomenological applications of the sector-residue subtraction scheme
- NNLO QCD predictions for three-jet observables
- Flavoured jets → proposal for modified anti-kT algorithm

Outlook:

- More three jet pheno results: TEEC, eventshapes
- More applications to $2 \rightarrow 3$ processes with 1 external mass
- More studies of flavoured jet algorithms