

Tasty jets at the LHC

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Outline

- Why are flavoured jets interesting?
- Fixed order flavoured jets beyond NLO
 - What is the issue?
 - Flavoured jet algorithms: flavour kT vs. **flavour anti-kT**
 - Tests IR safety of the proposed flavour anti-kT
- Phenomenology
 - Benchmark process: $pp \rightarrow Z+b\text{-jet}$
 - Top-quark pair production and decay
 - $pp \rightarrow W+ 2 b\text{-jets}$
 - $pp \rightarrow W+ c\text{-jet}$
- Closing remarks & alternatives

Why are flavoured jets interesting?

- Study of microscopic physics → Standard Model (SM) → Scattering amplitudes
- We need to identify the final states to relate them to specific scattering processes
- Here flavour comes into play:
 - **Flavoured (partonic) final states** allows to access specific “components” of the SM.
- Examples:
 - top-quark, Higgs (→ 2b-jets): using “b-tags” to identify candidate events
 - W/Z+flavoured jets: enhance sensitivity to certain PDFs
 - flavoured jet pairs: searches for new particles.
 - ...
- Precision measurements stress test theory and constrain parameters & content
 - Accurate and precise predictions for such final states required
 - higher order corrections essential (**this talk: fixed order QCD (+PS) and a tiny bit fragmentation**)
- We do not measure quarks and gluons in the detector → **jets**. We need to relate the partonic flavour structure to jet cross sections.

What are flavoured jets?

- Jets are a **tool** to connect QCD of quarks & gluons to actually strongly interacting particles, i.e. hadrons.
- They are **defined by a suitable algorithm**: experimentally and theoretically
- “Jet-substructure” reveals additional information:
 - Separation of quark and gluon initiated jets
 - Jets of definite flavour:

Experimentally	<i>Displayed vertices</i> of heavy intermediate particles: D/B mesons
MC Event Simulation	Similar objects due to hadronization and detector simulations
Partonic computations	<ul style="list-style-type: none">• Impose relation between quarks and hadrons• Massless quarks: emission of soft flavoured pairs → gluons<ul style="list-style-type: none">→ Implications for IR safety in FO computations beyond NLO→ Special flavour jet algorithms solve this problem

- Why are partonic computations for flavoured jets interesting?
 - Higher order perturbation theory (not necessarily available matched to PS)
 - Extraction of SM parameters or PDFs

The flavour kT algorithm

Problems with massless quarks:

1. Collinear gluon to $f \bar{f}$ splittings → count $f (+1)$ and $\bar{f} (-1)$ in a jet
2. Soft gluon to $f \bar{f}$ → need to be recombined for arbitrary angles

← NLO QCD

← NNLO QCD



Infrared safe definition of jet flavor,
Banfi, Salam, Zanderighi hep-ph/0601139

Jets at hadron colliders

Accurate QCD predictions for heavy-quark jets at the Tevatron and LHC,
Banfi, Salam, Zanderighi 0704.2999

Muon decays

Muon decay spin asymmetry
Caola, Czarnecki, Liang, Melnikov, Szafron 1403.3386

e^+e^- eventshapes

The Forward-backward asymmetry at NNLO revisited
Weinzierl hep-ph/0609021

Phenomenology of event shapes at hadron colliders,
Banfi, Salam, Zanderighi 1001.4082

The two-jet rate in e^+e^- at next-to-next-to-leading-logarithmic order
Banfi, McAslan, Monni, Zanderighi 1607.03111

LHC precision computations with flavoured jets

Associated Higgs production + decays in b-quarks:

Associated production of a Higgs boson decaying into bottom quarks at the LHC in full NNLO QCD

Ferrera, Somogyi, Tramontano 1705.10304

NNLO QCD corrections to associated WH production and $H \rightarrow b\bar{b}$ decay

Caola, Luisoni, Melnikov, Rötsch 1712.06954

Associated production of a Higgs boson decaying into bottom quarks and a weak vector boson decaying leptonically at NNLO in QCD

Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 1907.05836

Bottom quark mass effects in associated WH production with the $H \rightarrow b\bar{b}$ decay through NNLO QCD

Behring, Bizoń, Caola, Melnikov, Rötsch 2003.08321

VH + jet production in hadron-hadron collisions up to order α_s^3 in perturbative QCD

Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 2110.12992

+Partonshower:

NNLOPS accurate associated HZ production with $H \rightarrow b\bar{b}$ decay at NLO

Astill, Bizoń, Re, Zanderighi 1804.08141

NNLOPS description of the $H \rightarrow b\bar{b}$ decay with MiNLO

Bizoń, Re, Zanderighi 1912.09982

Next-to-next-to-leading order event generation for VH production with $H \rightarrow b\bar{b}$ decay

Zanoli, Chiesa, Re, Wiesemann, Zanderighi 2112.04168

LHC precision computations with flavoured jets

Vector + flavoured jet(s) production:

NLO QCD predictions for $Wbb\bar{b}$ production in association with up to three light jets at the LHC

Anger, Cordero, Ita, Sotnikov 1712.05721

Predictions for Z-Boson Production in Association with a b-jet at $O(\alpha_s^3)$

Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 2005.03016

NNLO QCD predictions for $W+c$ -jet production at the LHC,

Czakov, Mitov, Pellen, Poncelet 2011.01011

NNLO QCD corrections to $Wbb\bar{b}$ production at the LHC,

Hartanto, Poncelet, Popescu, Zoia 2205.01687

Top-quark pair final state modelling:

Modeling uncertainties of $t\bar{t}W^+$ - multilepton signatures

Bevilacqua, Bi, Cordero, Hartanto, Kraus, Nasufi, Reina, Worek 2109.15181

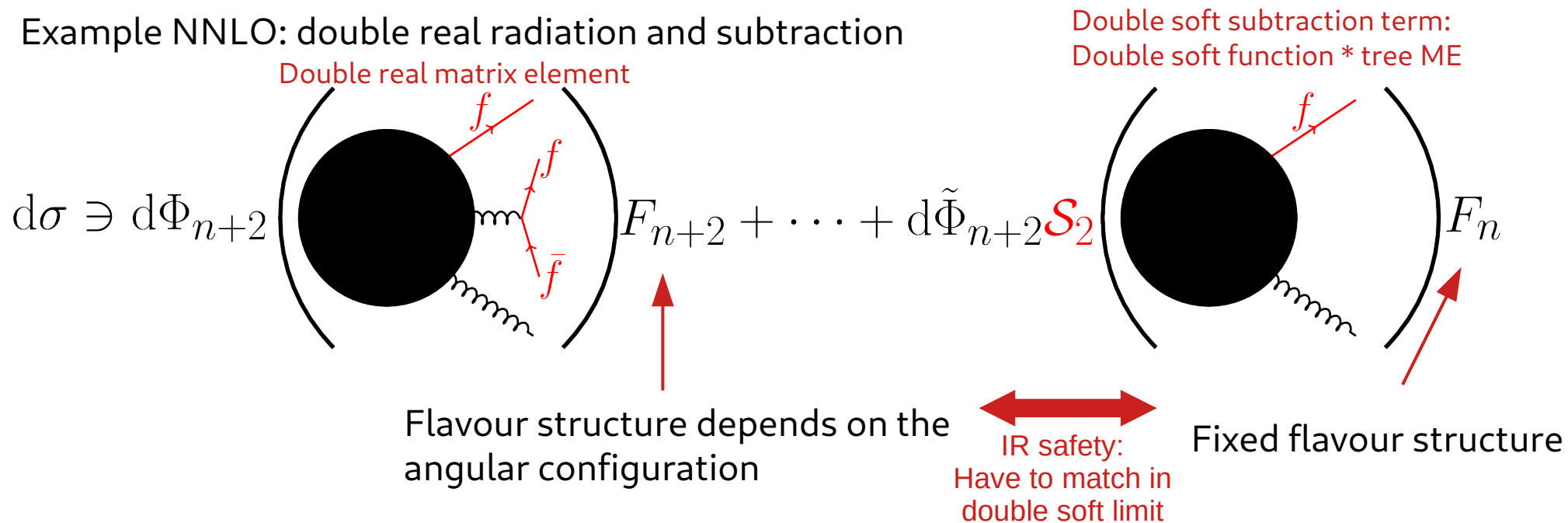
B-hadron production in NNLO QCD: application to LHC $t\bar{t}$ events with leptonic decays

Czakov, Generet, Mitov, Poncelet, 2102.08267

Fixed order flavoured jets beyond NLO

What is the problem with FO flavoured jets?

Example NNLO: double real radiation and subtraction



- If $F(n+2)$ does not treat the flavour pair appropriately:
→ double soft singularity not subtracted
- **Implies correlated treatment of kinematics and flavour information**

Solution: Modified jet algorithms

→ Implies correlated treatment of kinematics and flavour information

Standard kT algorithm:

Pair distance:

$$d_{ij} = \min(k_{T,i}^2, k_{T,j}^2) R_{ij}^2$$

$$R_{ij}^2 = (\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2) / R^2$$

“Beam” distance for determination condition:

$$d_i = k_{T,i}^2$$

Flavour kT algorithm:

Infrared safe definition of jet flavor,
Banfi, Salam, Zanderighi hep-ph/0601139

Pair distance:

$$d_{ij} = R_{ij}^2 \begin{cases} \max(k_{T,i}, k_{T,j})^\alpha \min(k_{T,i}, k_{T,j})^{2-\alpha} & \text{softer of } i, j \text{ is flavoured} \\ \min(k_{T,i}, k_{T,j})^\alpha & \text{else} \end{cases}$$

Beam distance:

$$d_{i,B} = \begin{cases} \max(k_{T,i}, k_{T,B}(y_i))^\alpha \min(k_{T,i}, k_{T,B}(y_i))^{2-\alpha} & i \text{ is flavoured} \\ \min(k_{T,i}, k_{T,B}(y_i))^\alpha & \text{else} \end{cases}$$

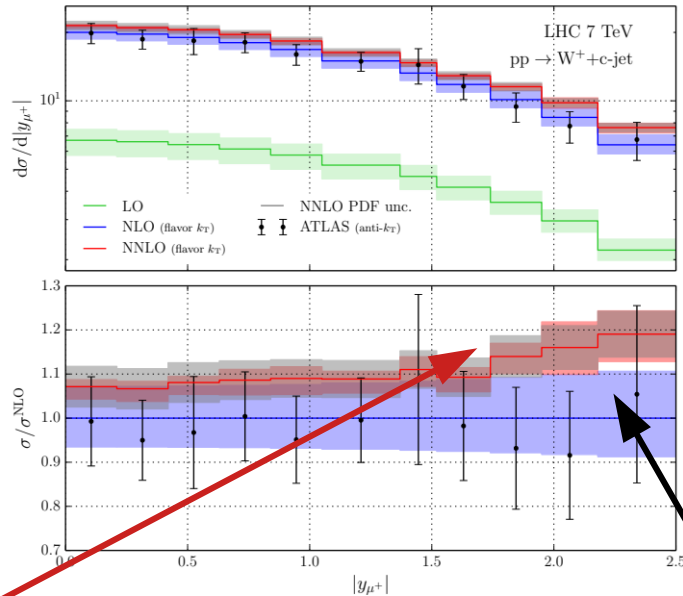
$$d_B(\eta) = \sum_i k_{T,i} (\theta(\eta_i - \eta) + \theta(\eta - \eta_i)) e^{\eta_i - \eta}$$

$$d_{\bar{B}}(\eta) = \sum_i k_{T,i} (\theta(\eta - \eta_i) + \theta(\eta_i - \eta)) e^{\eta - \eta_i}$$

Problem solved, isn't it?

Real world example: W+c-jet at NNLO QCD with flavour-kT

NNLO QCD predictions for W+c-jet production at the LHC,
Czakon, Mitov, Pellen, Poncelet 2011.01011



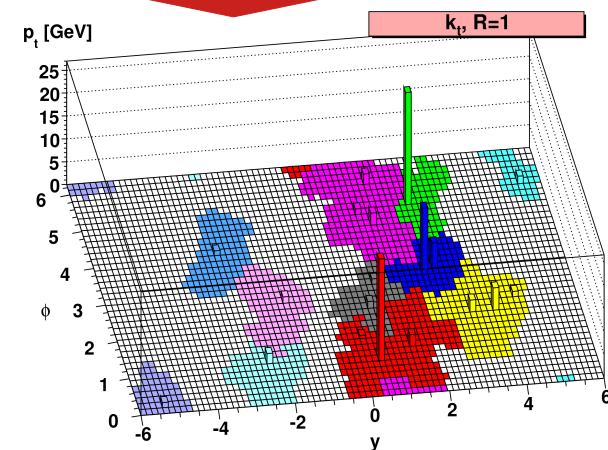
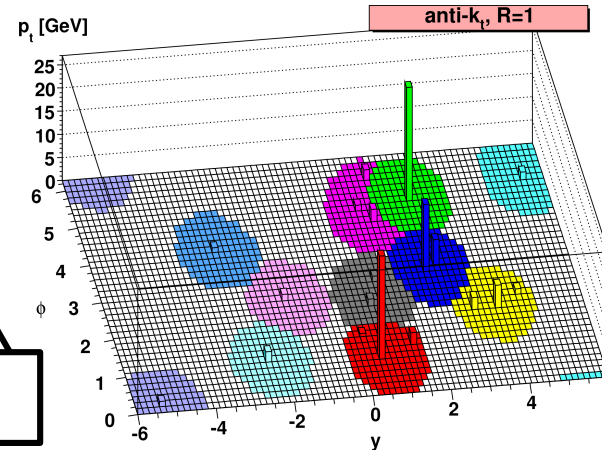
A proper comparison would require to
unfold experimental data

→ (flavour-) kT and anti-kT cluster partonic jets
differently → Non-trivial procedure.

Towards Jetography
Salam 0906.1833

NNLO QCD with flavour kT

ATLAS data with standard anti-kT



What about flavour anti-kT?

$$\text{Anti-kT: } d_{ij} = \min(k_{T,i}^{-2}, k_{T,j}^{-2}) R_{ij}^2 \quad d_i = k_{T,i}^{-2}$$

Infrared-safe flavoured anti-kT jets,
Czakon, Mitov, Poncelet 2205.11879

The energy ordering in anti-kT prevents correct recombination of flavoured pairs in the double soft limit.

Proposed modification:

A soft term designed to modify the distance of flavoured pairs.

$$d_{ij}^{(F)} = d_{ij} \begin{cases} \mathcal{S}_{ij} & \text{i,j is flavoured pair} \\ 1 & \text{else} \end{cases}$$

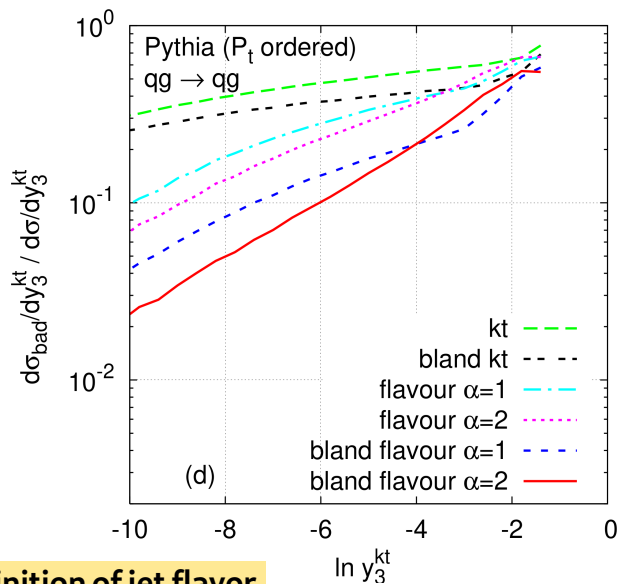
$$\mathcal{S}_{ij} = 1 - \theta(1 - x) \cos\left(\frac{\pi}{2}x\right) \quad \text{with} \quad x = \frac{k_{T,i}^2 + k_{T,j}^2}{2ak_{T,\max}^2}$$

Tests of IR safety with parton showers

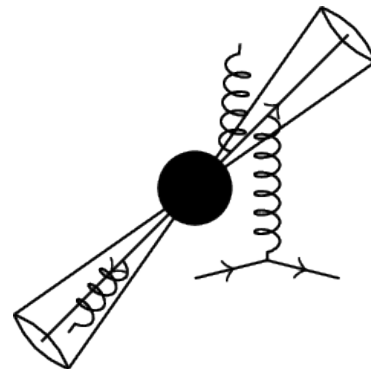
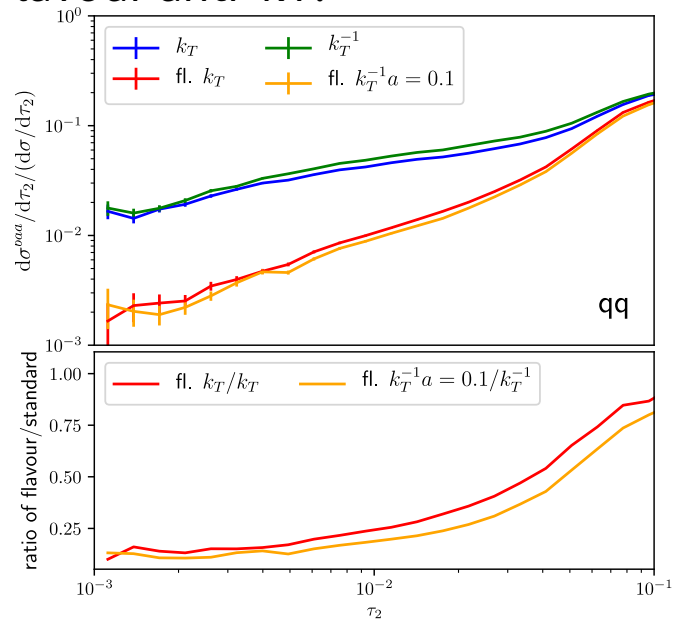
Dress tree-level di-jet events (definite flavour structure: "qq", "qg" or "gg") with radiation and study jet flavour (q or g) as function of kinematics.

In the di-jet limit the flavour needs to correspond to tree level flavours
 → misidentification rate needs to vanish in dijet back-to-back limit

Flavour kT vs. kT:



Flavour anti-kT:



Infrared safe definition of jet flavor,
 Banfi, Salam, Zanderighi hep-ph/0601139

Tests of IR safety with NNLO FO computations

IR sensitivity of jet cross sections on (technical) IR regulating parameter x

$$d\sigma \ni d\Phi_{n+2} \left(\text{diagram} \right) F_{n+2} + \dots + d\tilde{\Phi}_{n+2} \mathcal{S}_2 \left(\text{diagram} \right) F_n \theta(x - x_{\text{cut}})$$

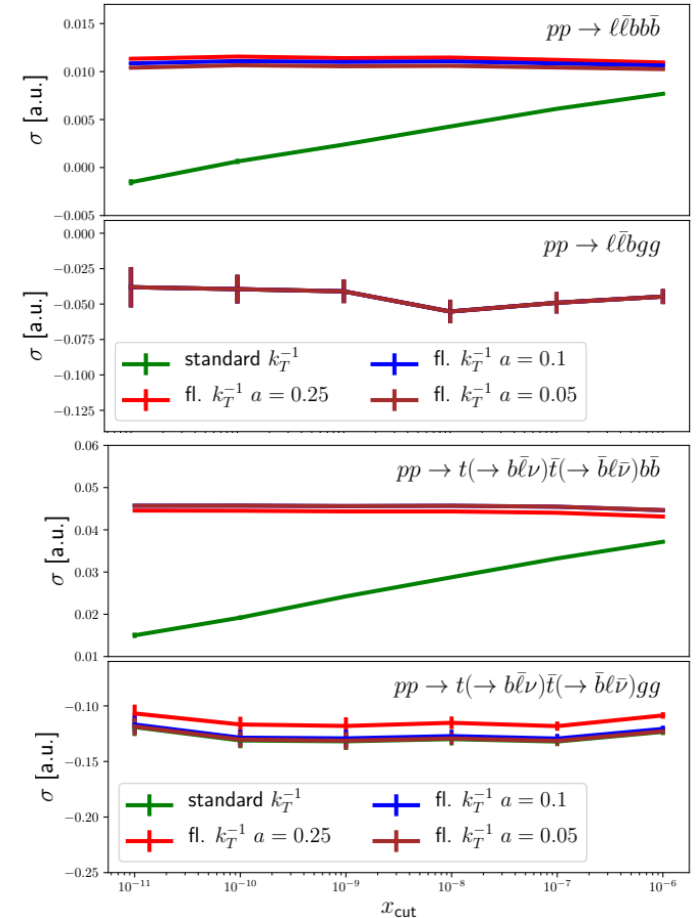
In the limit $x_{\text{cut}} \rightarrow 0$:

IR safe jet flavour

→ no dependence on x_{cut}

IR non-safe jet flavour

→ logarithmic divergent



IR-Safe? Yes. But is it useful?



Phenomenology

Processes:

- $pp \rightarrow Z + b\text{-jet}$
- top-quark pair production and decay
- $pp \rightarrow W + c\text{-jet}$
- $pp \rightarrow W + 2 b\text{jets}$

Benchmark process: Z+b-jet

Well studied up to $\mathcal{O}(\alpha_s^3)$:

Predictions for Z-Boson Production in Association with a b-jet at $\mathcal{O}(\alpha_s^3)$,

Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 2005.03016

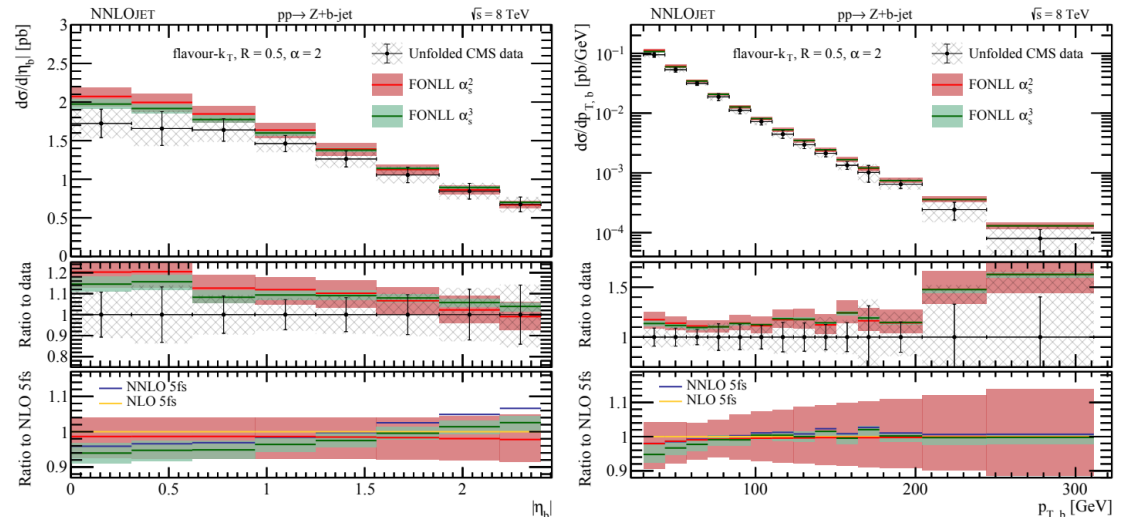
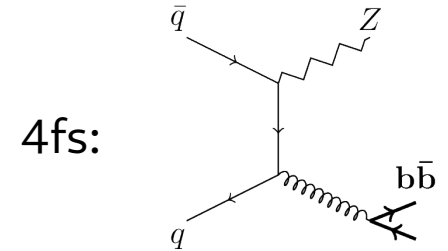
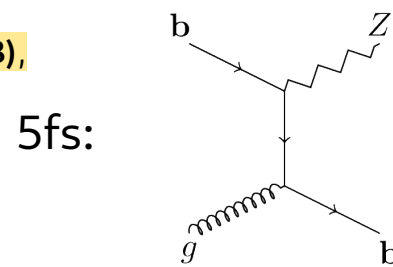
- Flavour-kT algorithm
- Unfolding of experimental data (RooUnfold, bin-by-bin unfolding)
- Matching between four- and five-flavour schemes (FONLL)

$$d\sigma^{\text{FONLL}} = d\sigma^{5\text{fs}} + (d\sigma_{m_b}^{4\text{fs}} - d\sigma_{m_b \rightarrow 0}^{4\text{fs}})$$

- CMS measurement @ 8 TeV

Measurements of the associated production of a Z boson and b jets in pp collisions at $\sqrt{s} = 8 \text{ TeV}$, CMS 1611.06507

pp \rightarrow Z(ll) + b-jet



Z+b-jet Phenomenology: Tunable parameter

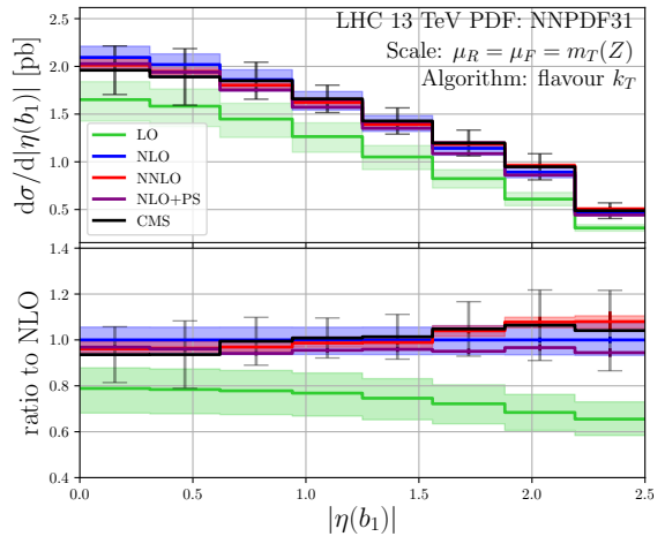
Benchmark process: $pp \rightarrow Z(\ell\ell) + b\text{-jet}$

Tunable parameter a :

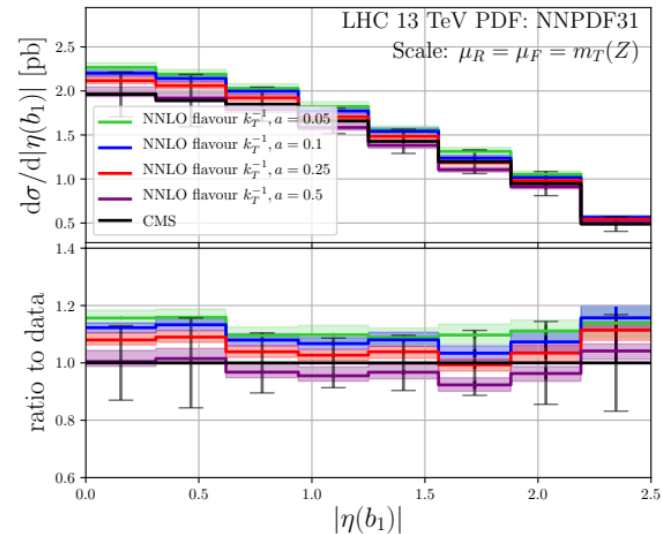
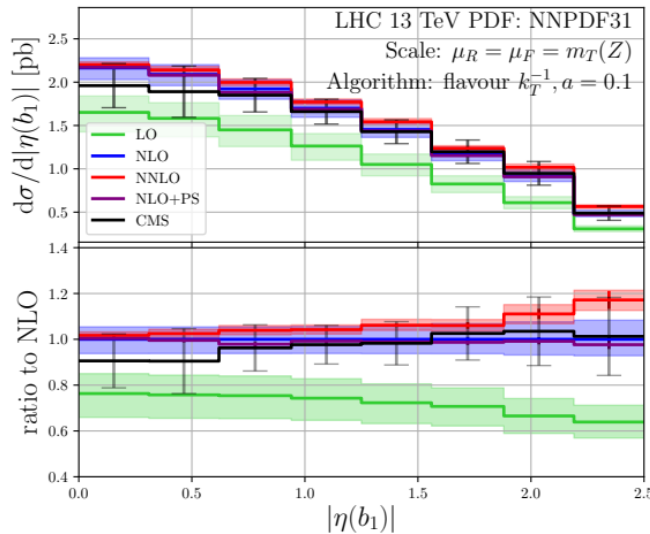
- Limit $a \rightarrow 0 \Leftrightarrow$ original anti-kT (IR unsafe)
- Large $a \Leftrightarrow$ large modification of cluster sequence

Comparison of different parameter a to data:

Flavour kT:

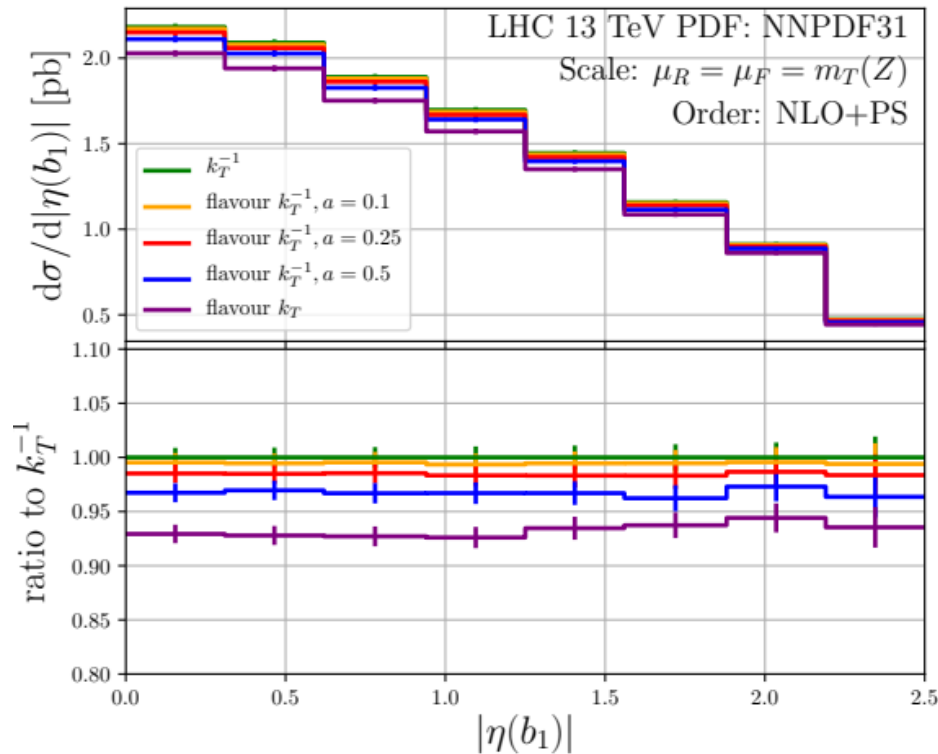


Flavour anti-kT: $a = 0.1$



Z+b-jet Phenomenology: Tunable parameter II

What happens in the presence of many flavoured partons? → NLO PS



Tunable parameter a:

- Small a: Flavour anti-kT results are more similar to standard anti-kT → **small unfolding factors**
- Larger a: Larger modification of clustering

Good FO perturbative convergence +
Small difference to standard anti-kT
→ $a \sim 0.1$ is a good candidate

b-jets in top-pair production & decay

NNLO QCD corrections to leptonic observables in top-quark pair production and decay,
Czakon, Mitov, Poncelet 2008.11133

$$pp \rightarrow t(\rightarrow b\bar{l}\nu)\bar{t}(\rightarrow \bar{b}l\bar{\nu}) + X$$

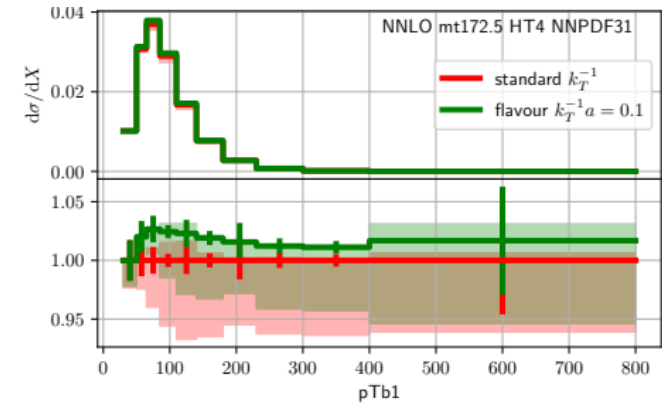
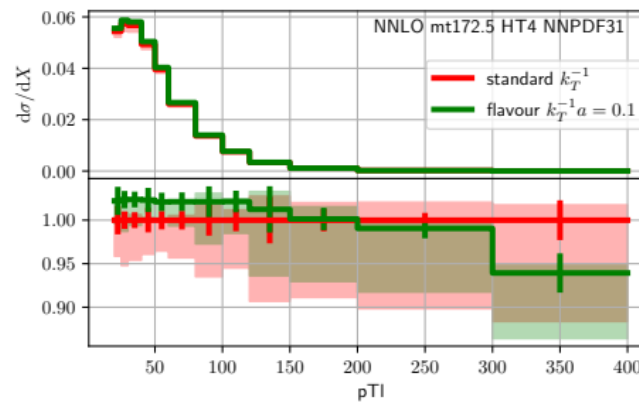
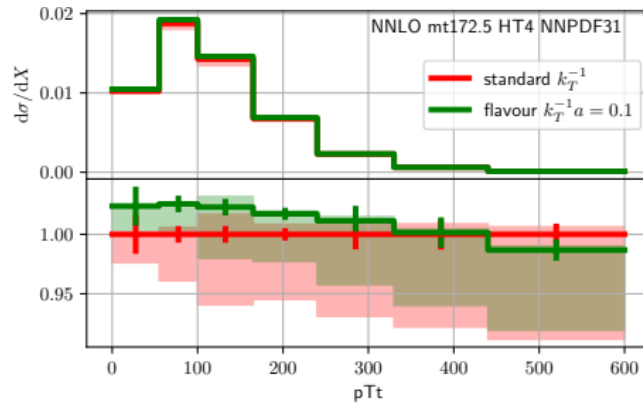
Flavour sensitive channels like: $pp \rightarrow t\bar{t}b\bar{b} \rightarrow \bar{l}\nu l\bar{\nu} \boxed{b\bar{b}b\bar{b}}$

Small numerical impact from extra $b\bar{b}$ emissions in $pp \rightarrow b\bar{b}$ and single-top production
→ naive treatment via cut-off procedure

Bottom-quark production at hadron colliders:
fully differential predictions in NNLO QCD,
Catani, Devoto, Grazzini, Kallweit, Mazzitelli 2010.11906

Differential Distributions for t-channel Single Top-Quark Production and Decay at Next-to-Next-to-Leading Order in QCD,
Berger, Gao, Zhu 1708.0940

Single-top-quark production in the t-channel at NNLO,
Campbell, Neumann, Sullivan 2012.01574



Naive 'cut-off' treatment vs. proposed IR safe flavour anti-kT

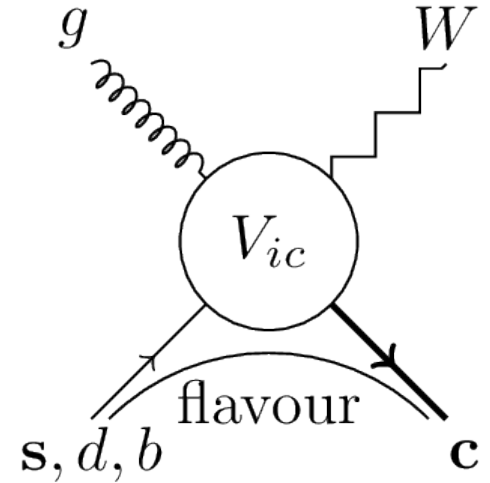
W+c-jet

Idea: Identify final state c-quarks to access **s-quark PDFs**.

→ Reduction of PDF uncertainties

→ Shed light on $s\bar{s}$ asymmetry

- Non-diagonal CKM and $g \rightarrow c\bar{c}$ reduce s-PDF sensitivity
- Large NLO corrections → higher order corrections?
- Theoretical treatment:
 - Massive c (3-flavour scheme):
 - Resummation of mass logs at high $p_T \rightarrow$ PS
 - Higher order predictions?
 - Massless c:
 - c-quark part of the PDFs
 - NNLO QCD available
 - **Jet definition?**



$$V_{sc} > V_{dc} \gg V_{bc}$$

W+c-jet with flavour kT at NNLO QCD

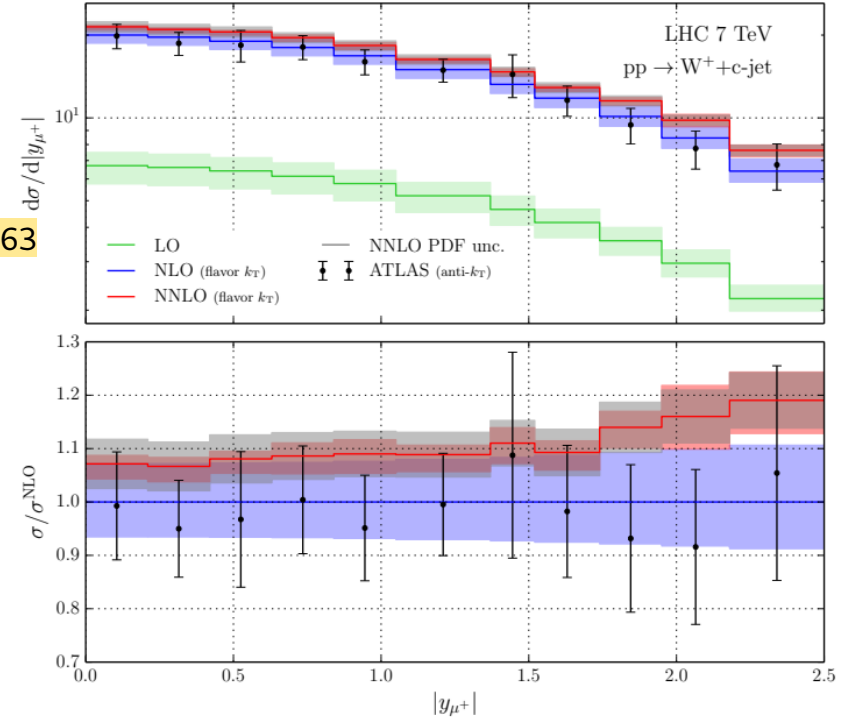
NNLO QCD 7 TeV results: **NNLO QCD predictions for W+c-jet production at the LHC,**
Czakon, Mitov, Pellen, Poncelet 2011.01011

- Full NNLO corrections for Vcs contribution
- Off-diagonal CKM only LO QCD
- Comparison flv. kT results vs. ATLAS

Measurement of the production of a W boson in association with a charm quark in pp collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector, 1402.6263

Update for 13 TeV measurement:

- **Full CKM** through NNLO QCD
- **Study of different jet-algorithms:**
 - Impact of beam-function d_{iB} in flv kT
 - New anti-kT algorithm
- Study of different flavour tag definitions/setups:
 - Modulus vs. absolute flv tag definition
 - OS minus SS
 - “Inclusive c-jet” rates



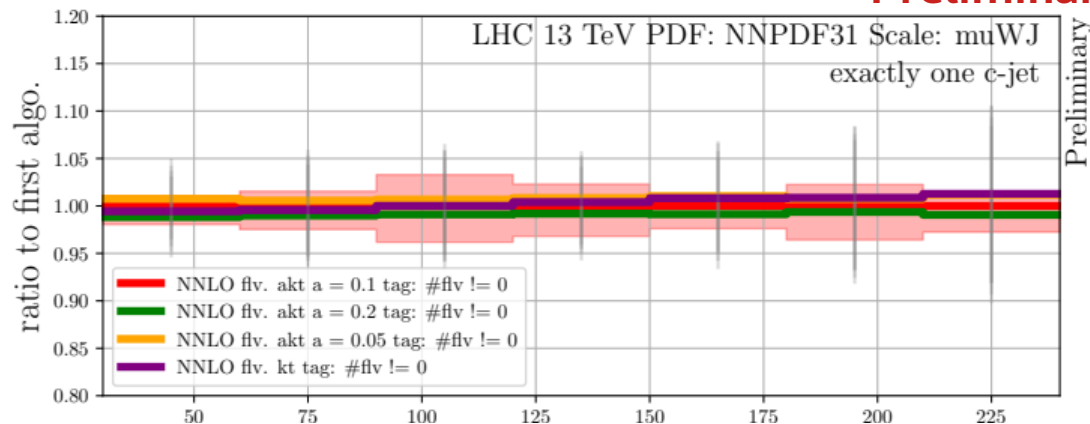
W+c-jet with flavour anti-kT

In collaboration with: Czakon, Mitov, Pellen

Preliminary

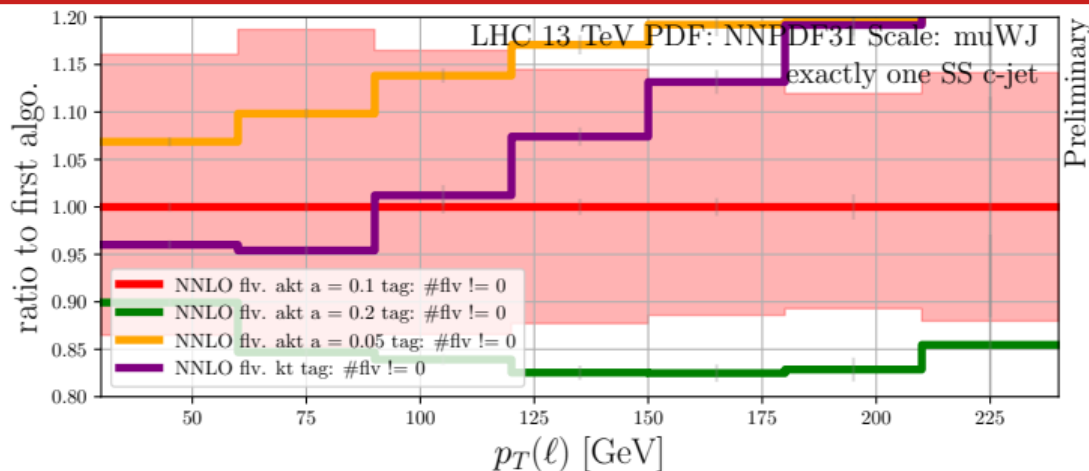
Exactly one c-jet requirement:

- Comparison of parameters a:
→ small dependence < 2%
- Comparison to flv kt:
→ small dependence @ NNLO < 2%



ONLY large effect in SS contribution

- Exactly one c-jet of SS type:
Larger dependence ~15%
(roughly size of NNLO scale band)
- BUT: SS contribution ~2-5%
- => OS ~0.2-0.5% dependence



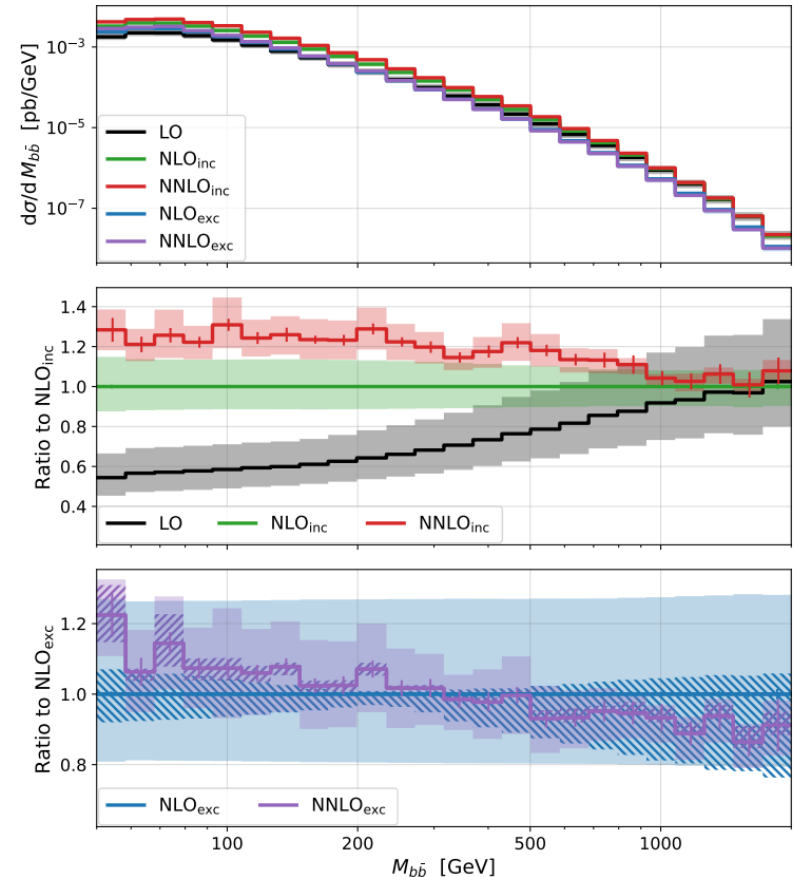
pp \rightarrow W + 2 b-jets

First NNLO QCD computation with a massive leg

$$pp \rightarrow \ell \bar{\nu} b \bar{b} + X$$

NNLO QCD corrections to Wbbbar production at the LHC,
Hartanto, Poncelet, Popescu, Zoia, 2205.01687

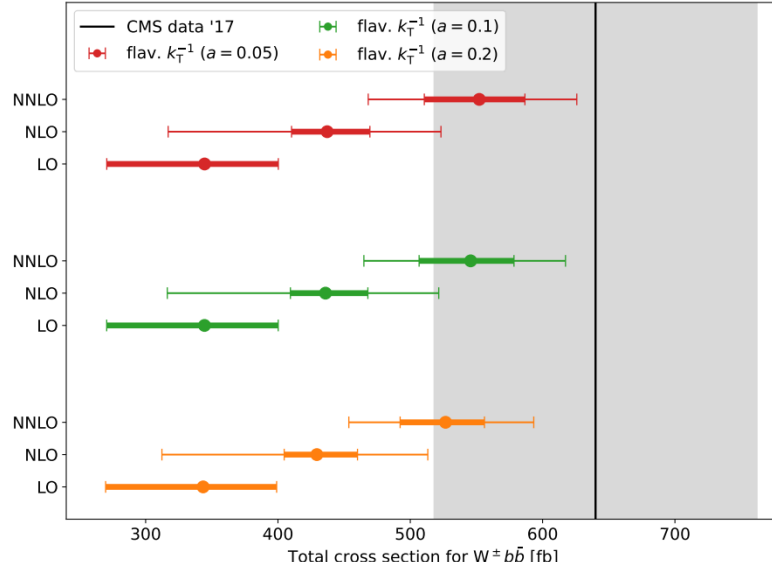
- Leading colour approximation for 2-loop amplitudes
- Massless b-quark \rightarrow flavour kT algorithm for IR safety



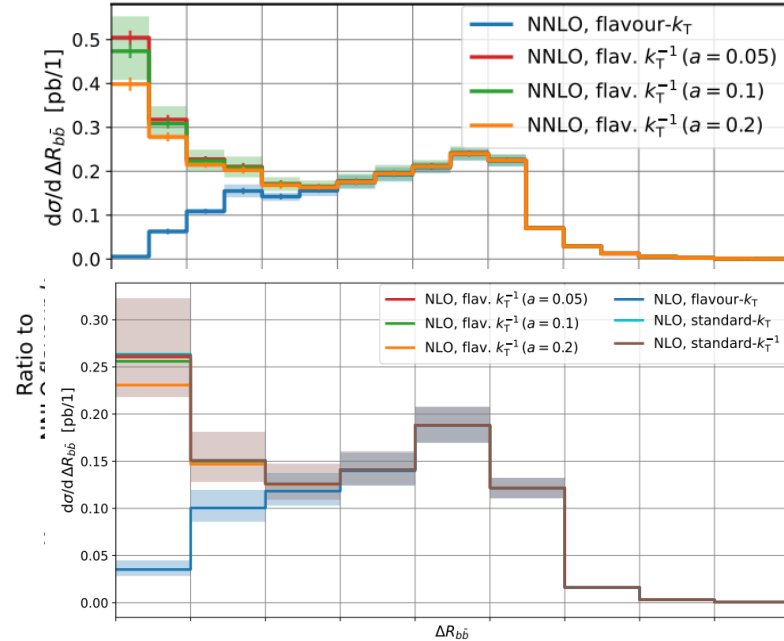
W+2bjets: flavour anti-kT

Preliminary

Fiducial cross section W+ and W- + 2 b-jets



Measurement of the production cross section of a W boson in association with two b jets in pp collisions at $\sqrt{s} = 8$ TeV, CMS 1608.07561



Significant differences between kT and anti-kT
In small $\Delta R(b\bar{b})$ region? Maybe Beam-function?

Remarks & Summary

Some final remarks

- What is that k_{T_max} parameter?

Some scale to define what **soft** means. Examples:

1. p_T of hardest pseudo jet or lepton at a clustering step
2. Some fixed dynamical scale, e.g. $p_T(Z)$, $p_T(\text{lep})$, ...
3. Some fixed hard scale: m_{top} , m_Z etc.
→ The choice impacts the clustering.

$$d_{ij}^{(F)} = d_{ij} \begin{cases} \mathcal{S}_{ij} & i,j \text{ is flavoured pair} \\ 1 & \text{else} \end{cases}$$

$$\mathcal{S}_{ij} = 1 - \theta(1 - x) \cos\left(\frac{\pi}{2}x\right) \quad \text{with} \quad x = \frac{k_{T,i}^2 + k_{T,j}^2}{2ak_{T,max}^2}$$

- Besides c/b jets: What about gluon/quark jet identification?

Conceptually not a problem. Not yet studied in detail.

But might introduce some more sensitivity to actual form of S_{ij} ??

- Is it realizable in experiment? → Would require detailed experimental flavour information... :/

- Alternatives:

- Reclustering with flavour safe algorithm + matching:

QCD-aware partonic jet clustering for truth-jet flavour labelling

Buckley, Pollard 1507.00508

Practical Jet Flavour Through NNLO

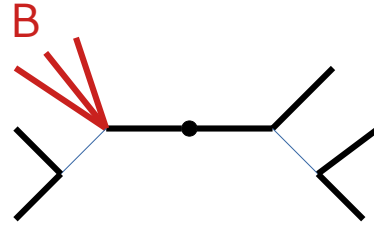
Caletti, Larkoski, Marzani, Reichelt 2205.01109

- Using fixed order fragmentation for jet-tagging

A Fragmentation Approach to Jet Flavor

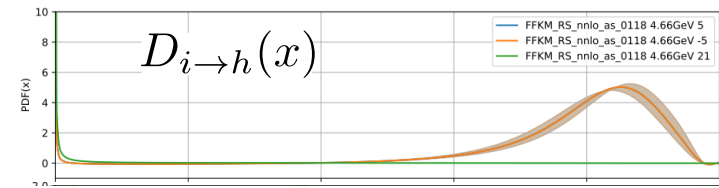
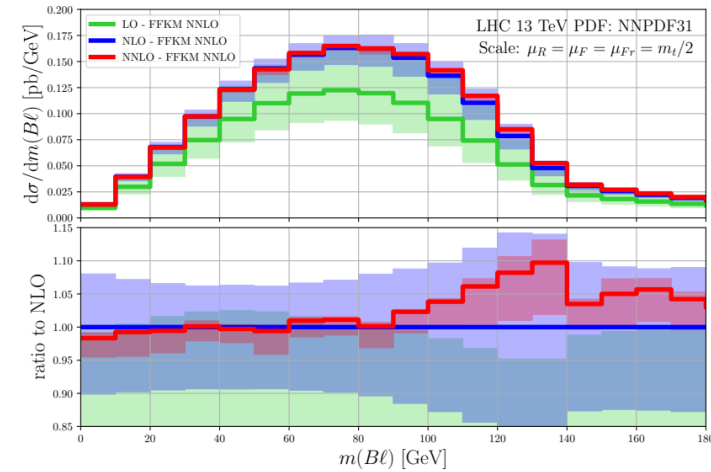
Caletti, Larkoski, Marzani, Reichelt 2205.01117

$$pp \rightarrow t\bar{t} \rightarrow B\ell\bar{\ell}\nu\bar{\nu}b + X$$

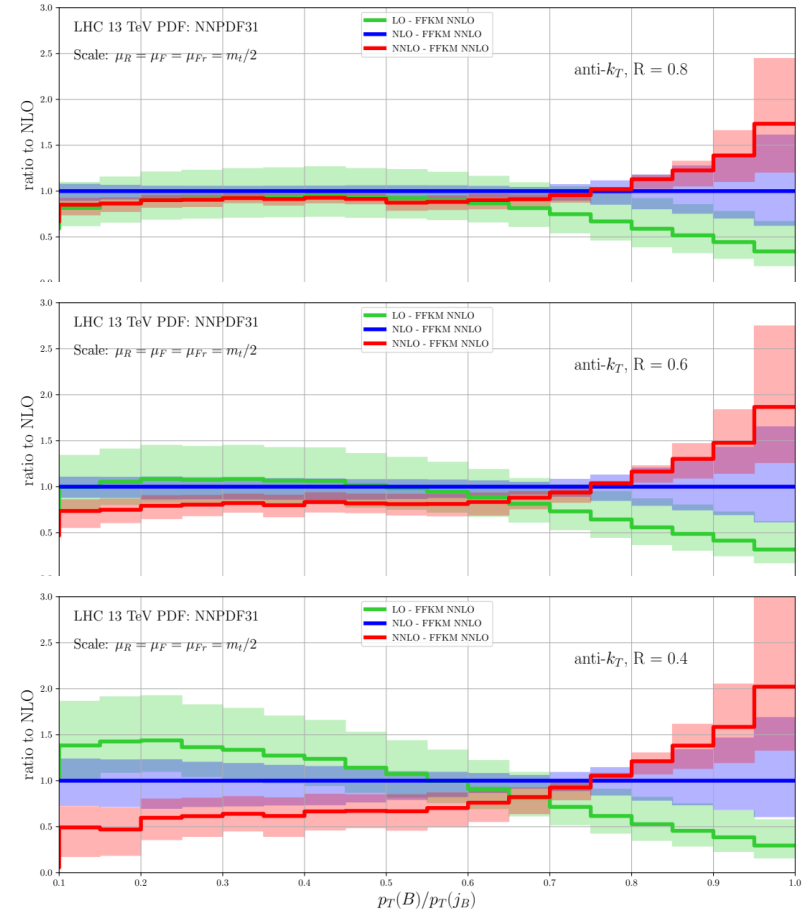
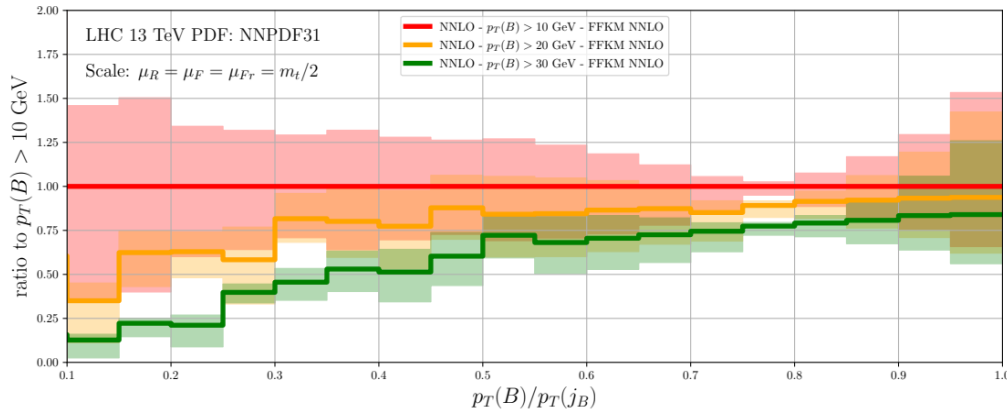


- Fixed order QCD predictions with a final state hadron
- Considering partonic computation + transition of parton to hadron (collinear fragmentation of massless partons)
- Advantage is that the hadrons momentum is measurable while the quark's is not
- Fragmentation function (similar to PDFs): Probability to find a hadron with a fraction x of the quarks momentum:
- No Parton-shower needed
- Implementation in the STRIPPER framework through NNLO QCD

B-hadron production in NNLO QCD: application to LHC $t\bar{t}$ events with leptonic decays,
Czakon, Generet, Mitov and Poncelet, 2102.08267



- $p_T(B)$ requirement necessary since NNLO fragmentation function divergent for $x \rightarrow 0$ due to $g \rightarrow b\bar{b}$ splitting
- Predictions depend on this choice!
- Also: sensitivity to jet radius
 → Usage as b-tag needs tuning



Summary and Outlook

New proposal for flavour safe anti-kT algorithm

- Numerical checks of IR safety
- Introduction of tunable parameter a
- Phenomenological studies:
 - $pp \rightarrow Z+b\text{-jet}$
 - $pp \rightarrow tt + \text{decays}$
 - $pp \rightarrow W+c\text{-jet}$
 - $pp \rightarrow W+2\text{ b-jets}$

$$d_{ij}^{(F)} = d_{ij} \begin{cases} \mathcal{S}_{ij} & i,j \text{ is flavoured pair} \\ 1 & \text{else} \end{cases}$$

$$\mathcal{S}_{ij} = 1 - \theta(1 - x) \cos\left(\frac{\pi}{2}x\right) \quad \text{with} \quad x = \frac{k_{T,i}^2 + k_{T,j}^2}{2ak_{T,\text{max}}^2}$$

Thank you for your attention :)