

# NNLO predictions for top-quark pair production with leptonic final states

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# Top quarks at the LHC

The LHC performance is really good.

- large amount of top quark data.
- Observables (XS, differential distributions, mass,...) at % level precision

Top quark pair production is important:

- parameter estimation
- Standard Model precision measurements
- background for many physics searches for SM ...
- ... and beyond

Necessity of precise theory predictions for production and decay!

# $t\bar{t}$ in theory and experiment

## Experiment:

- Signature:  $b$ -jets, leptons, missing energy (depending on the decay channel)
- top-quarks are reconstructed from decay products
- Modeling extremely important
- measurements like  $t\bar{t}$  (differential) x-sections rely on extrapolation in fiducial volumes

## Theory

- theory of stable on-shell tops well under control: state of the art NNLO (+EW) → good modeling of reconstructed top data
- on-shell NWA and off-shell: up to now NLO
  - more realistic final state.
  - omit systematic uncertainties
  - spin information of top accessible!

# Theory - resonant top quark pair production

Stable onshell tops, spin summed:

- Total inclusive cross sections @ NNLO+NNLL accuracy

[Czakon, Fiedler, Mitov '13]

- Fully differential distributions @ NNLO

[Czakon, Fiedler, Heymes, Mitov '16]

- + EW corrections

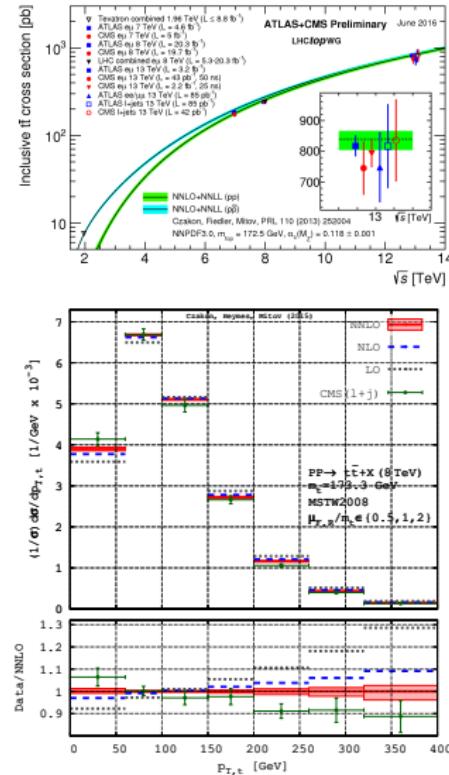
[Czakon, Heymes, Mitov, Pagani,

Tsinikos, Zaro '17]

Unstable tops + spin correlations:

- Approximate NNLO + NNLO decay

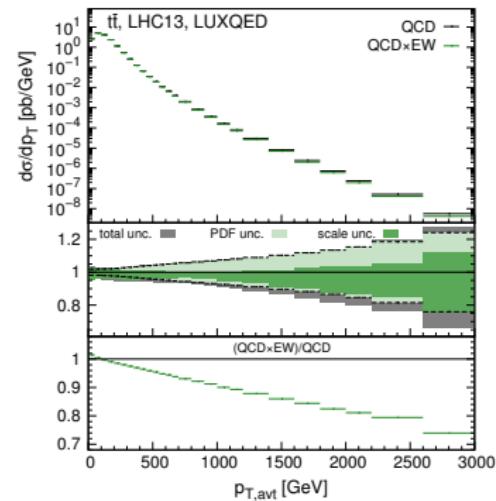
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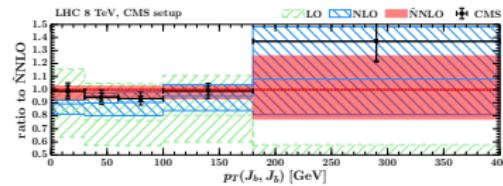
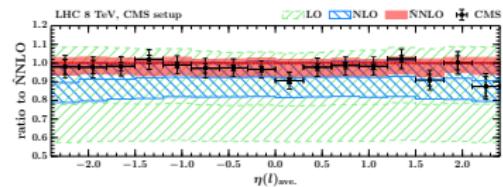
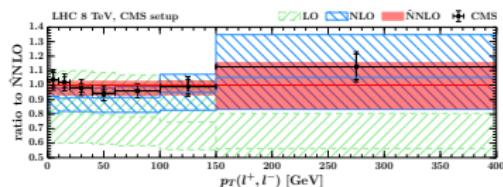
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Unstable tops + spin correlations:

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[Gao, Papanastasiou '17]

# Towards realistic final states at NNLO

Best: full off-shell NNLO  $\leftarrow$  not feasible yet

Here: Narrow-Width-Approximation at NNLO

## Necessary ingredients

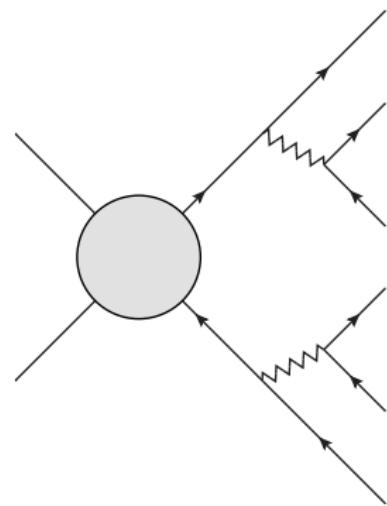
- Handling of real-radiation contribution:
  - facilitate cancellation of divergences between double-real, real-virtual, double-virtual contributions
  - difficult: double real radiation
  - $\rightarrow$  new implementation of STRIPPER algorithm
- Virtual matrix elements:
  - one-loop  $\rightarrow$  no problem here
  - two-loop production and decay matrix elements
  - polarization needed

# $t\bar{t}$ production and decay in NWA

Motivation:  $\Gamma_t \ll m_t$

## Narrow-Width-Approximation

- On-shell top-quarks
- Factorization of top-decay
- Separations of QCD corrections
- Keep spin correlations



## Polarized matrix elements

# $t\bar{t}$ production and decay at NNLO QCD in NWA

		Decay	LO	NLO	NNLO
		Production			
LO	LO		Standard NLO	[Bonciani'08] [Asatrian'08] [Beneke'08]	
NLO		Standard NLO	Standard NLO		
NNLO		[Long,Czakon,RP '17]			

# Polarised $t\bar{t}$ production amplitudes

Gluon channel

$$\mathcal{M} = \epsilon_{1\mu}(p_1)\epsilon_{2\nu}(p_2)M^{\mu\nu}$$

$M^{\mu\nu}$  is a rank-2 Lorentz tensor

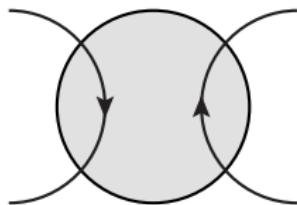
- Momentum conservation
- Transversality
- Equation of motion
- Parity conservation  $\rightarrow$  no  $\gamma_5$

8 independent structures

( $d = 4$  dimensions)

$$M^{\mu\nu} = \sum_{j=1}^8 M_j T_j^{\mu\nu}$$

Quark channel



- Two disconnected fermion lines
- Connection by gluons+loops

4 independent structures

$$\mathcal{M} = \sum_{i=1}^4 M_i T_i$$

with  $T_i \sim \bar{v}_2 \Gamma_j u_1 \bar{u}_3 \Gamma'_j v_4$

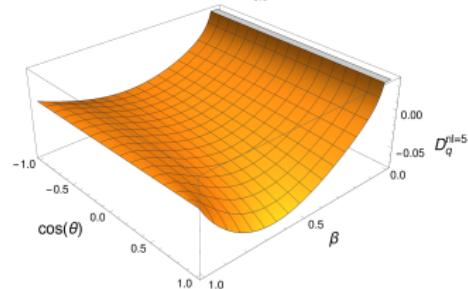
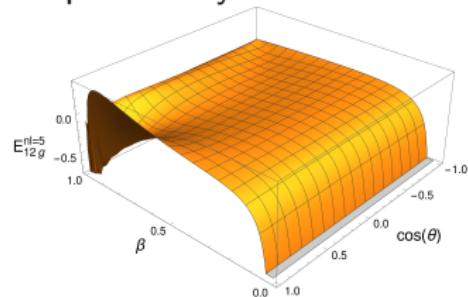
# Two loop polarised $t\bar{t}$ production amplitudes

projection method → scalar coefficients with scalar integrals

## Master integrals

- reduction of scalar integrals via in-house Laporta implementation
- new partially canonicalised
- numerical treatment of master with help of differential equation  
→ interpolation grid

spin-density coefficients:



- finite remainder functions
- full color and spin information

## Subtraction framework

# NNLO subtraction schemes

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## Handling real radiation contribution in NNLO calculations cancellation of infrared divergences

increasing number of available NNLO calculations with a variety of schemes

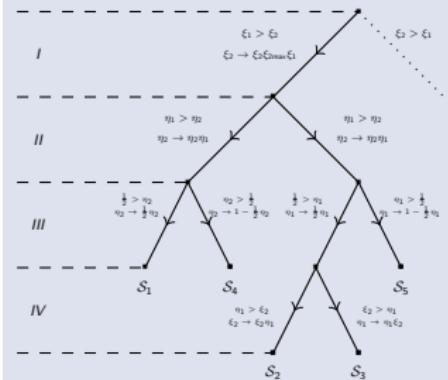
- **qT-slicing** [Catani, Grazzini, '07], [Ferrera, Grazzini, Tramontano, '11], [Catani, Cieri, DeFlorian, Ferrera, Grazzini, '12],  
[Gehrmann, Grazzini, Kallweit, Maierhofer, Manteuffel, Rathlev, Torre, '14-'15], [Bonciani, Catani, Grazzini, Sargsyan, Torre, '14-'15]
- **N-jettiness slicing** [Gaunt, Stahlhofen, Tackmann, Walsh, '15], [Boughezal, Focke, Giele, Liu, Petriello, '15-'16],  
[Boughezal, Campell, Ellis, Focke, Giele, Liu, Petriello, '15], [Campell, Ellis, Williams, '16]
- **Antenna subtraction** [Gehrman, GehrmanDeRidder, Glover, Heinrich, '05-'08], [Weinzierl, '08, '09],  
[Currie, Gehrman, GehrmanDeRidder, Glover, Pires, '13-'17], [Bernreuther, Bogner, Dekkers, '11, '14],  
[Abelof, (Dekkers), GehrmanDeRidder, '11-'15], [Abelof, GehrmanDeRidder, Maierhofer, Pozzorini, '14], [Chen, Gehrman, Glover, Jaquier, '15]
- **Colorful subtraction** [DelDuca, Somogyi, Troscanyi, '05-'13], [DelDuca, Duhr, Somogyi, Tramontano, Troscanyi, '15]
- **Sector-improved residue subtraction (STRIPPER)** [Czakon, '10, '11],  
[Czakon, Fiedler, Mitov, '13, '15], [Czakon, Heymes, '14] [Czakon, Fiedler, Heymes, Mitov, '16, '17],  
[Boughezal, Caola, Melnikov, Petriello, Schulze, '13, '14], [Boughezal, Melnikov, Petriello, '11], [Caola, Czernecki, Liang, Melnikov, Szafron, '14],  
[Bruchseifer, Caola, Melnikov, '13-'14], [Caola, Melnikov, Röntsch, '17]

# STRIPPER

## Outline of the scheme

- decomposition of phase space to disentangle overlapping singularities
- simple extraction of Laurent series in  $\epsilon$
- provides a general set of subtraction terms
- numerical treatment of integrated subtraction terms → numerical cancellation of  $\epsilon$  poles
- defined in  $d$ -dimensions → numerical evaluation not efficient  
⇒ four-dimensional formulation

## Triple collinear factorization



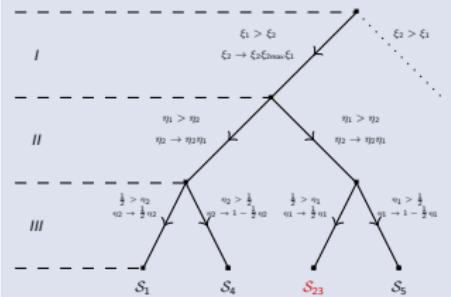
originally: 5 sub-sectors

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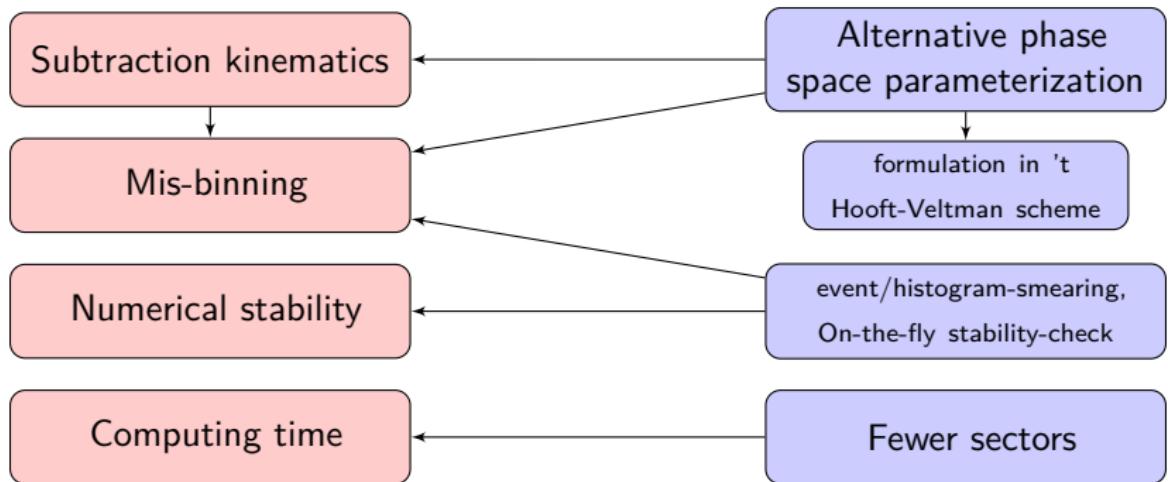
## Triple collinear factorization



Caola, Melnikov, Röntsch [hep-ph:1702.01352v1]

now: 4 sub-sectors

# How to improve the STRIPPER subtraction scheme?



# New phase space construction: Idea

## Goal

Phase space construction with a minimal # of subtraction kinematics

## Old construction

- Start with unresolved partons
  - Fill remaining phase space with Born configuration
- Non-minimal # kinematic configurations  
(e.g. single soft and collinear limits yield different configurations)

## New construction

- Start with Born configuration
- Add unresolved partons ( $u_i$ )
- Cleverly adjust Born configuration to accommodate the  $u_i$

# Consequences

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## Features

- Minimal number of subtraction kinematics
- Only one DU configuration  
→ pole cancellation for each Born phase space point
- Expected improved convergence of invariant mass distributions, since  $\tilde{q}^2 = q^2$

## Unintentional features

- Construction in lab frame
- Original construction of 't Hooft Veltman corrections [Czakon,Heymes'14] is spoiled

# NWA within STRIPPER

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## Implementation

- general (process-independent) STRIPPER implementation
  - new parameterization
  - new four-dimensional construction
- additional input: 1- and 2-loop finite remainder functions
- modifications for NWA:
  - onshell phase spaces
  - additional CS like dipole subtraction for decay part of NLOxNLO contributions (mixed subtractions)

$$pp \rightarrow t\bar{t} \rightarrow b\bar{b} ll' vv'$$

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differential cross section:

$$d\sigma = d\sigma_{t\bar{t}} \times \frac{d\Gamma_t}{\Gamma_t} \times \frac{d\Gamma_{\bar{t}}}{\Gamma_t}$$

decays - total width:

$$\Gamma_t = \Gamma(t \rightarrow bW^+) \sum_{ff'} \frac{\Gamma(W^+ \rightarrow ff')}{\Gamma_W}$$

decays - differential decays:

$$d\Gamma_t = d\Gamma(t \rightarrow bW^+) \sum_{f \in \{e, \mu\}} \frac{d\Gamma(W^+ \rightarrow f\nu_f)}{\Gamma_W}$$

# Consistent treatment of top width

Expansion in  $\alpha_s$ :

$$d\sigma_{t\bar{t}} = d\sigma_{t\bar{t}}^{(0)} + \alpha_s d\sigma_{t\bar{t}}^{(1)} + \alpha_s^2 d\sigma_{t\bar{t}}^{(2)}$$

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$$\Gamma_t = \Gamma_t^{(0)} + \alpha_s \Gamma_t^{(1)} + \alpha_s^2 \Gamma_t^{(2)}$$

Consistent expansion in  $\alpha_s$ :

$$d\sigma^{\text{LO}} \equiv d\sigma^{\text{LO} \times \text{LO}}$$

$$d\sigma^{\text{NLO}} = d\sigma^{\text{NLO} \times \text{LO}} + d\sigma^{\text{LO} \times \text{NLO}} - \frac{2\Gamma_t^{(1)}}{\Gamma_t^{(0)}} d\sigma^{\text{LO}}$$

$$d\sigma^{\text{NNLO}} = d\sigma^{\text{NNLO} \times \text{LO}} + d\sigma^{\text{NLO} \times \text{NLO}} + d\sigma^{\text{LO} \times \text{NNLO}}$$

$$- \frac{2\Gamma_t^{(1)}}{\Gamma_t^{(0)}} d\sigma^{\text{NLO}} + \left( \frac{3\Gamma_t^{(1)2}}{\Gamma_t^{(0)2}} - \frac{2\Gamma_t^{(0)}\Gamma_t^{(2)}}{\Gamma_t^{(0)2}} \right) d\sigma^{\text{LO}}$$

## Considerations:

- treatment ensures after full incl. integration:

$$\sigma = \sigma_{t\bar{t}} BR(W \rightarrow l\nu)$$

- practice: just rescaling lower order contributions

# First results

# Setup

## Setup: CMS

$m_t$	173.3 GeV
$m_W$	80.385 GeV
$m_Z$	91.1876 GeV
$\Gamma_W$	2.0928 GeV
$G_F$	$1.16379 \cdot 10^{-5}$ Gev $^2$

- comparison to approximate  $NN\hat{L}O$  calculation
- comparison to data provided by CMS [CMS '15]

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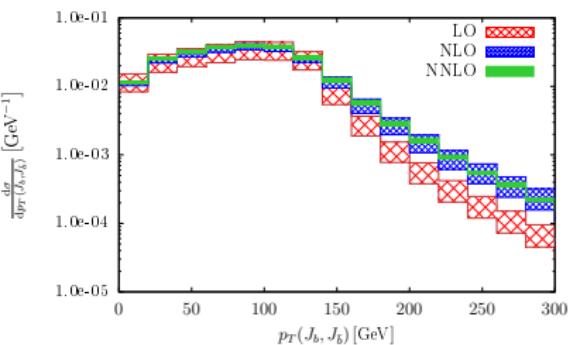
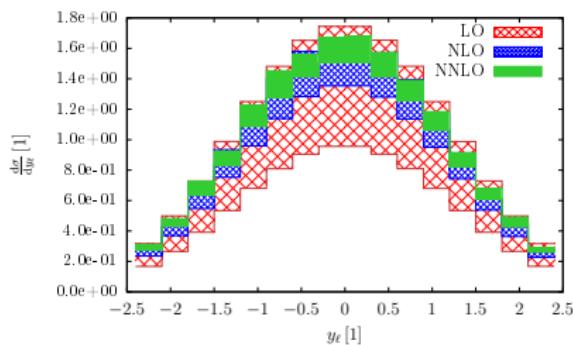
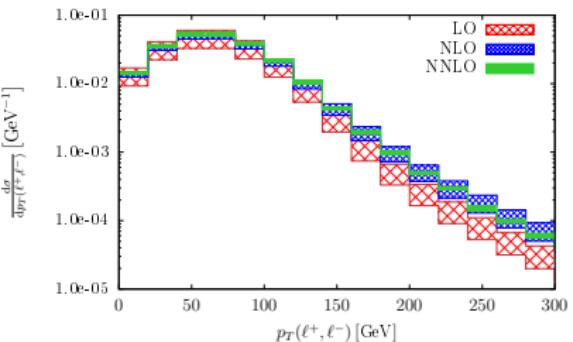
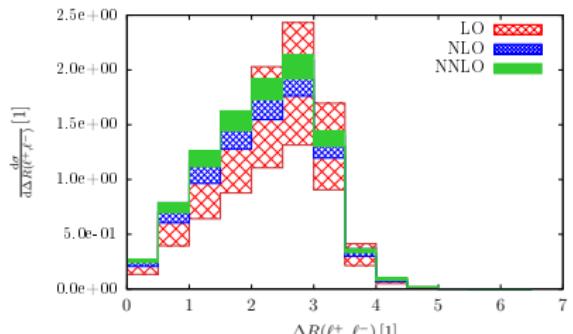
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## Caveat:

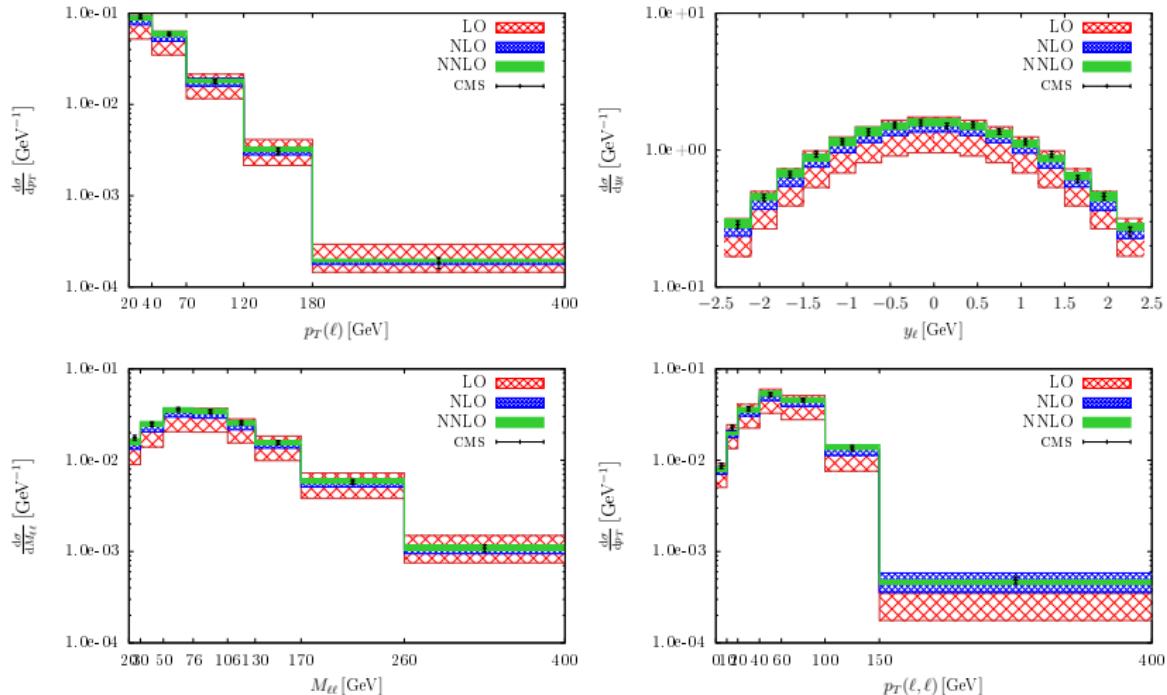
preliminary results!

# Differential distributions



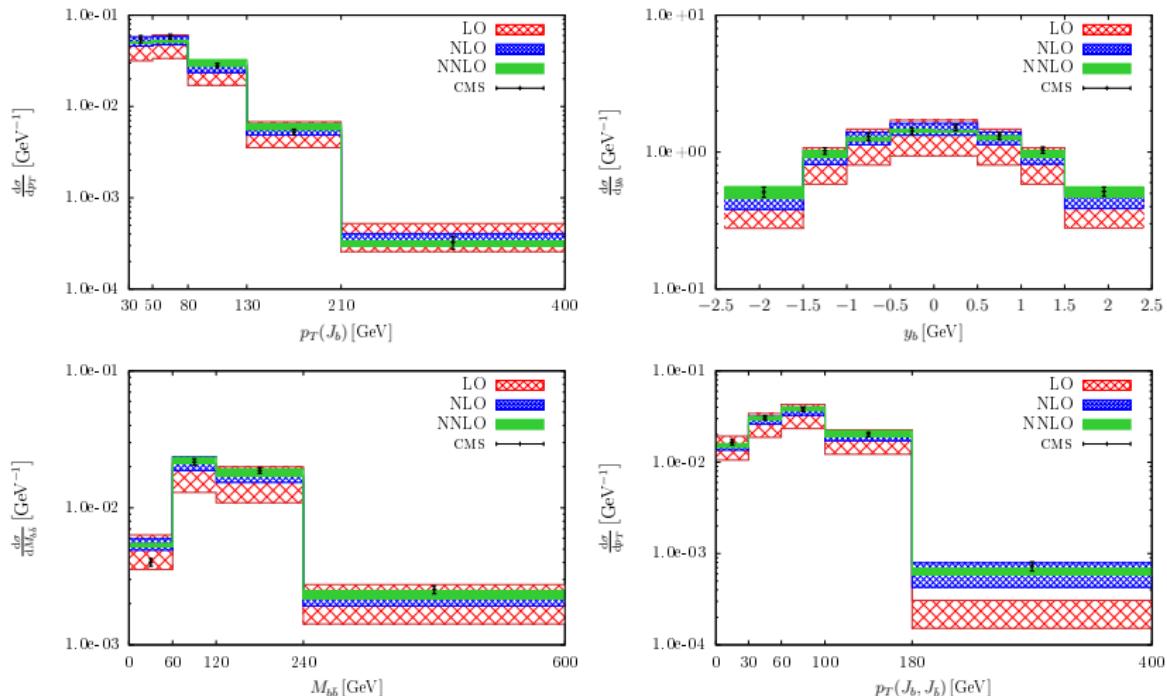
scale variations:  $\mu = \mu_R = \mu_F \in [m_t/2, 2m_t]$

# Comparison to CMS data - Leptons



scale variations:  $\mu = \mu_R = \mu_F \in [m_t/2, 2m_t]$

# Comparison to CMS data - $b$ -jets



scale variations:  $\mu = \mu_R = \mu_F \in [m_t/2, 2m_t]$

# Summary of progress

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## Summary

- STRIPPER: fully automated subtraction framework
- with Narrow-Width-Approximation implementation for  $t$  and leptonic  $W$  decays
- Polarized two-loop matrix elements
- first results for  $t\bar{t}$  with leptonic final states

## Outlook

- Phenomenological studies:
  - Spin correlations
  - fiducial cross sections
- hadronic  $W$ -decays → all-jet, lepton + jets channels

# Four dimensional formulation

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Treat resolved particles in 4 dimensions (momenta and polarisations)

- Avoid unnecessary  $\epsilon$ -orders of the matrix elements
- Avoid growth of dimensionality of phase space integrals

Make resolved phase space 4-dim. using measurement function, e.g.

$$F_n \rightarrow F_n \mathcal{N}^{-(n-1)\epsilon} \prod_{i=1}^{n-1} \delta^{(-2\epsilon)}(q_i)$$

This introduces errors of  $\mathcal{O}(\epsilon)$  in all contributions!

Needed: Separately finite single and double unresolved contributions

- using finiteness of NLO calculation
- shifting terms from single-unresolved to double-unresolved contributions
- corrections calculated in full generality